

Supawit

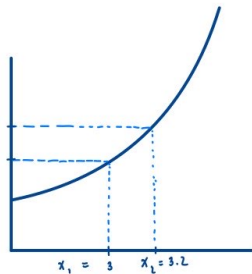
# 6304641498

HW Given  $y = 10 + \sqrt{x}$ ,

- a) Find the derivative  $f'(x)$ .  $f'(x) = \frac{1}{2} \cdot x^{-\frac{1}{2}}$  ↗ only positive part
- b) Fill in the table

Point	X	Y	$f'(x)$
	0	10	0
A	1	11	$\frac{1}{2}$
B	2	14	0.35
C	3	19	0.29

- c) Does the slope increase as  $x$  increase? no, it does not
- d) Approximate the change in Y when  $\Delta x = 0.2$  at  $y_2 = 11.79$   
 $x_1 = 3$ . Is the approximation under- or over-estimate?  
 estimate?  $\text{slope} \cdot \Delta x = \frac{\Delta y}{\Delta x} \approx 0.29 \cdot 0.2$   
 $\Delta y \approx 0.058$  — \*



Note: If the function  $f(x)$  is linear, the approximation is exact.

$$\begin{aligned}x_2 &= x_1 + \Delta x \\x_2 &= 3 + 0.2 \\x_2 &= 3.2\end{aligned}$$

$$f(3.2) = 10 + \sqrt{3.2}$$

$$f(3.2) = 11.79$$

$$y_2 = 11.79$$
 — \*

$$\therefore \text{real } \Delta y = y_2 - y_1 = 11.79 - 11.73 = 0.06$$
 — \*

$\therefore$  we conclude that approximation is underestimate compared to real  $\Delta y$  and