

Chapter 8 Price Elasticity of Supply

Price Elasticity of Supply is the percentage change of the quantity supplied per 1 percentage change in price

$$\eta_s = \frac{\% \Delta Q_s}{\% \Delta P} = \frac{\text{Percentage change of } Q_s}{\text{Percentage change of } P}$$

- η_s measures how sensitive the supply is to a change in price.

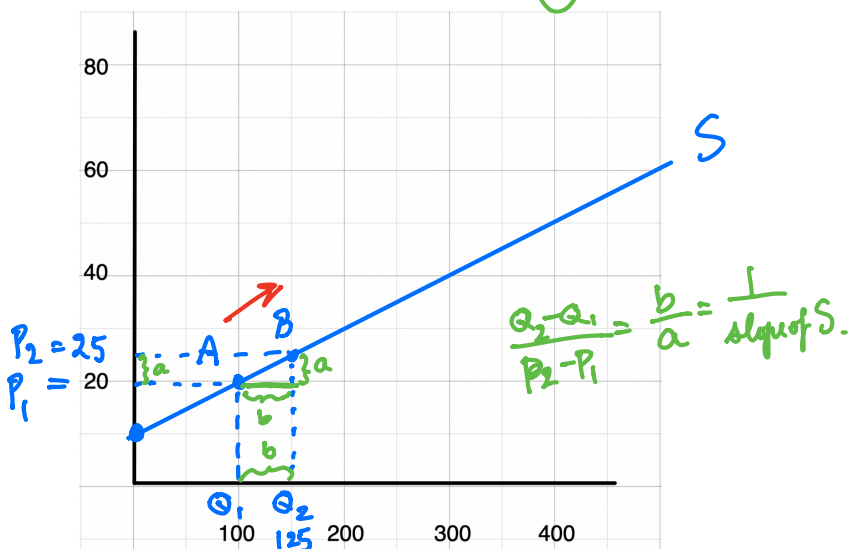
Example If the price increases by 10% ($\% \Delta P = 10\%$), the quantity supplied increases by 25% ($\% \Delta Q_s = 25\%$)

$$\eta_s = \frac{\% \Delta Q_s}{\% \Delta P} = \frac{25}{10} = 2.5$$

- Positive sign reflects the Law of Supply
- η_s does not have unit
- $\eta_s = 2.5$ means that if the price increases by 1%, the quantity supplied increases by 2.5%

Example

$$\text{Supply: } P = 10 + \frac{1}{10} Q_s$$



Consider two points, A and B on the supply

$$\begin{aligned} \downarrow A &= (100, 20), Q_1 = 100, P_1 = 20 \\ \downarrow B &= (150, 25), Q_2 = 150, P_2 = 25 \end{aligned}$$

From A → B,

$$\Delta Q_S = Q_2 - Q_1 = 150 - 100 = 50$$

$$\Delta P = P_2 - P_1 = 25 - 20 = 5.$$

$$\% \Delta Q_S = \frac{50}{100} = 50\% = \frac{Q_2 - Q_1}{Q_1}$$

$$\% \Delta P = \frac{5}{20} = 25\% = \frac{P_2 - P_1}{P_1}$$

$$\eta_S = \frac{\% \Delta Q_S}{\% \Delta P} = \frac{50\%}{25\%} = 2.$$

$$= \frac{(Q_2 - Q_1)/Q_1}{(P_2 - P_1)/P_1} = \left(\frac{Q_2 - Q_1}{P_2 - P_1} \right) \cdot \frac{P_1}{Q_1}$$

$$= \frac{1}{\text{slope of } S} \cdot \frac{P_1}{Q_1} = \frac{1}{1/10} \cdot \frac{20}{100} = 2.$$

- η_S from A to B is given by:

$$\eta_S = \frac{1}{\text{slope } Q_1} \frac{P_1}{Q_1}$$

where P_1 and Q_1 are price and quantity supplied at A.

- Is η_S the same for B → A?

$$\eta_S = \frac{\% \Delta Q_S}{\% \Delta P} = \frac{\frac{Q_1 - Q_2}{P_1 - P_2} \frac{P_2}{Q_2}}{\frac{P_1 - P_2}{P_1 - P_2} \frac{P_2}{Q_2}}$$

$\frac{1}{\text{slope of } S}$

- η_S from B → A is given by:

$$\eta_S = \frac{1}{\text{slope } Q_2} \frac{P_2}{Q_2} = \frac{1}{1/10} \cdot \frac{25}{150} = \frac{5}{3}$$

where P_2 and Q_2 are price and quantity supplied at B.

Arc Elasticity of Supply

From A → B, $\eta_S = \frac{1}{\text{slope } Q_1} \frac{P_1}{Q_1} = 2.$ ✓

From B → A, $\eta_S = \frac{1}{\text{slope } Q_2} \frac{P_2}{Q_2} = 1.67$ ✓

midpoint $\eta_S = 1.8$.

If we want to find, η_S between A and B (without specifying from where to where) we use

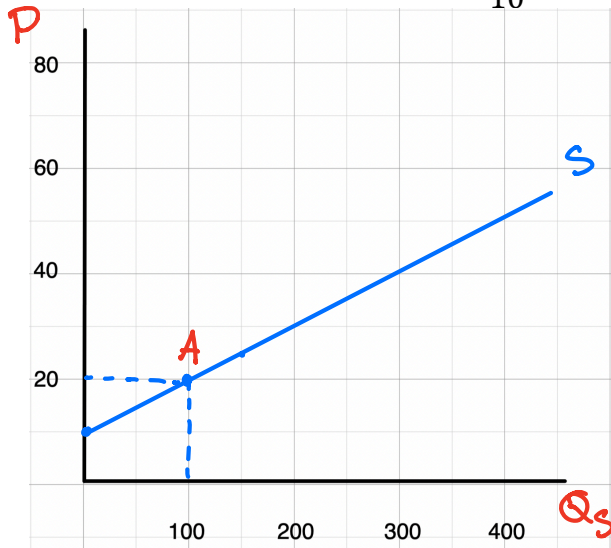
Average Price = $\bar{P} = \frac{P_1 + P_2}{2}$

Average Quantity = $\bar{Q} = \frac{Q_1 + Q_2}{2}$

$$\eta_s = \frac{1}{\text{Slope } \bar{Q}} \cdot \bar{P} = \frac{1}{\text{Slope } \bar{Q}} \cdot \frac{(P_1 + P_2)/2}{(Q_1 + Q_2)/2}$$

$$= \frac{1}{1/10} \cdot \frac{22.5}{125} = \frac{9}{5} = 1.8.$$

Supply: $P = 10 + \frac{1}{10} Q_s$ $\frac{1}{1/10} \cdot \frac{45}{250} = 1.8.$



This is called *Arc Elasticity by Midpoint method*.

Supply $P = 10 + \frac{1}{10} Q_s$

$Q_s = -100 + 10P$

Point Elasticity of Supply at a point $A = (Q_1, P_1) = (100, 20)$.

$$\eta_s = \left(\frac{1}{\text{Slope at A}} \right) \frac{P_1}{Q_1}$$

$$= \frac{1}{\frac{dP}{dQ_s}} \cdot \frac{P_1}{Q_1}$$

$$= \frac{dQ_s}{dP} \cdot \frac{P_1}{Q_1} = 10 \left(\frac{20}{100} \right) = 2$$

Handwritten notes: $\frac{dQ_s}{dP} = 10$, $\frac{dP}{dQ_s} = \frac{1}{10}$, $10 \left(\frac{20}{100} \right) = 2$, *slope of tangent line*

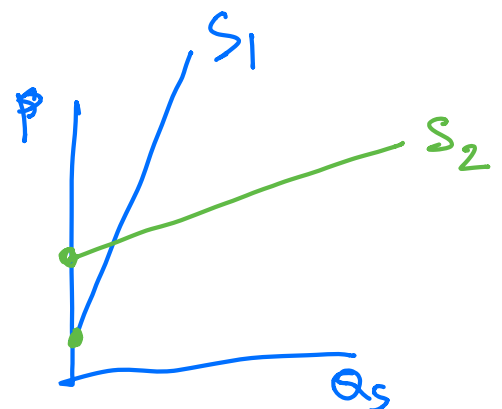
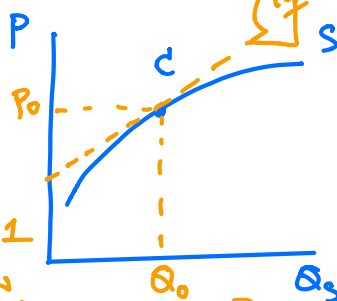
Elastic and Inelastic Supply

Supply is Elastic when $\eta_s > 1$
Supply is Inelastic when $\eta_s < 1$.

Supply has unit elasticity if $\eta_s = 1$

At C,

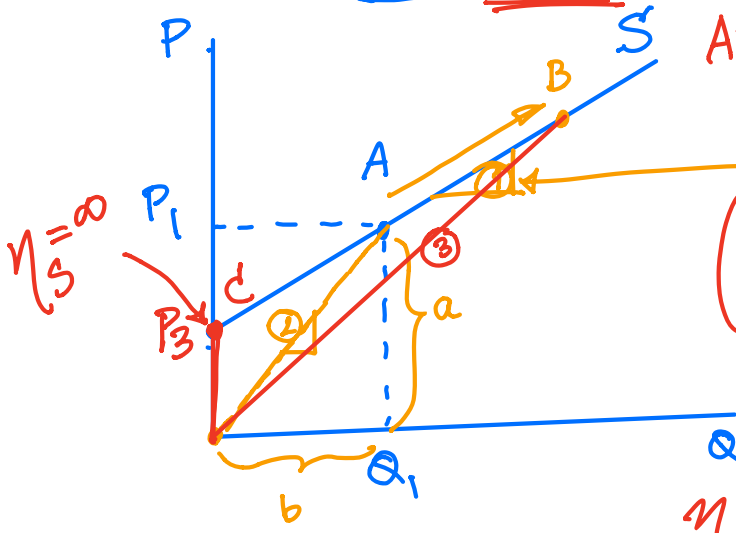
$$\eta_s = \frac{1}{(\text{slope of tangent line})} \cdot \frac{P_0}{Q_0}$$



always elastic.

Point Elasticity of along a Linear Supply Curve

1. η_s when Supply has positive intercept.



At A: $\eta_s = \frac{1}{\text{slope at A}} \cdot \frac{P_i}{Q_i}$
 $= \frac{(2)}{(1)} > 1$

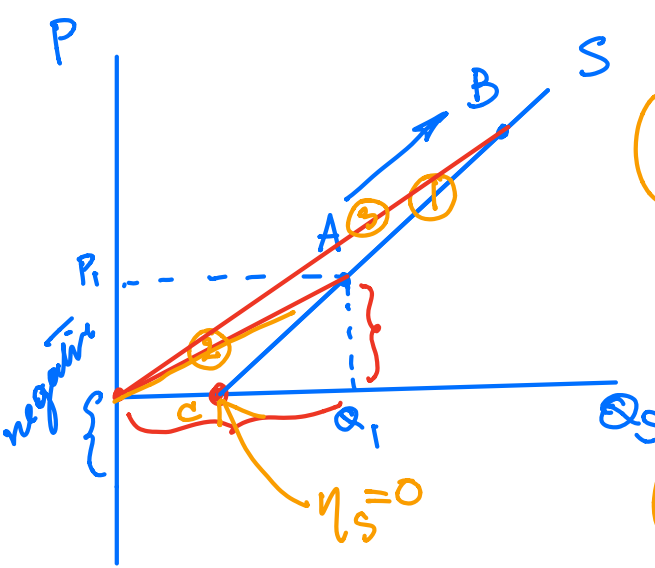
At B: $\frac{(3)}{(1)} > 1$

$(\eta_s)_A > (\eta_s)_B$

$\eta_s > 1$ and keeps decreasing as we move up the S curve

At C, $Q_s = 0$
 Price = P_3
 $\eta_s = \frac{1}{(\text{slope at C})} \cdot \frac{P_3}{0} = \infty$

2. η_s when Supply has negative intercept.



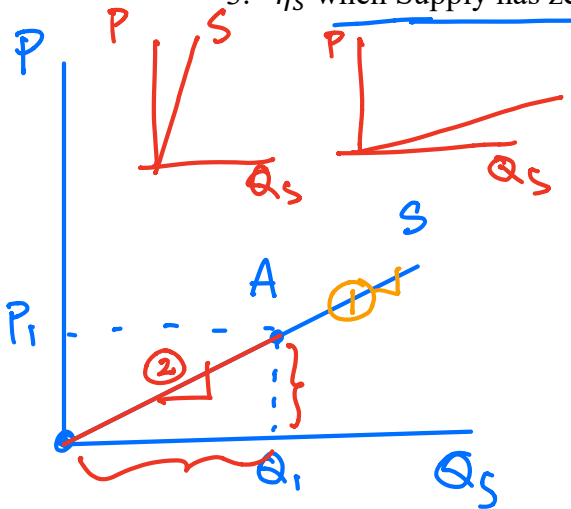
$(\eta_s)_A = \frac{1}{(\text{slope at A})} \cdot \frac{P_i}{Q_i}$
 $= \frac{(2)}{(1)} < 1$

η_s is always < 1 inelastic

$(\eta_s)_B = \frac{(3)}{(1)} < 1$

and η_s keeps increasing as we move up the S curve.

3. η_s when Supply has zero intercept.



$\eta_s = \frac{1}{\text{slope at A}} \cdot \frac{P_i}{Q_i}$
 $= \frac{(2)}{(1)} = 1$

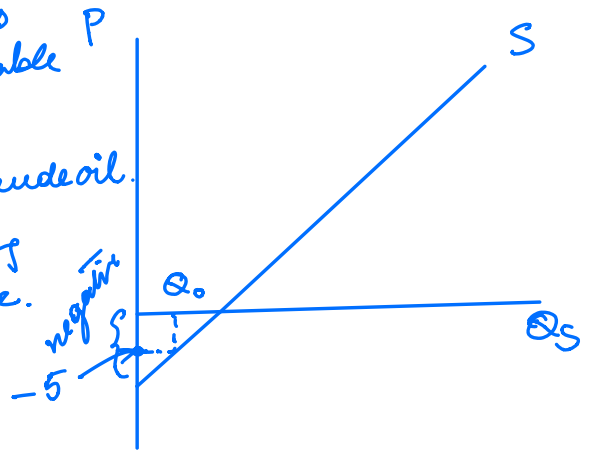
always $\eta_s = 1$.

At C, Price = 0, $Q_s = Q_0 > 0$
 $(\eta_s)_C = \frac{1}{(\text{slope of S at C})} \cdot \frac{0}{Q_0} = 0$

2 possible interpretations of S with neg intercept

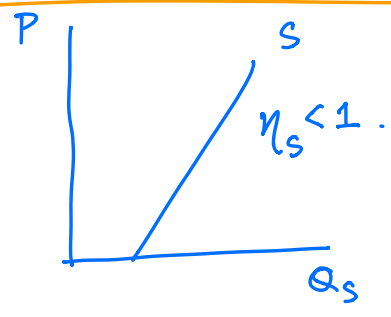
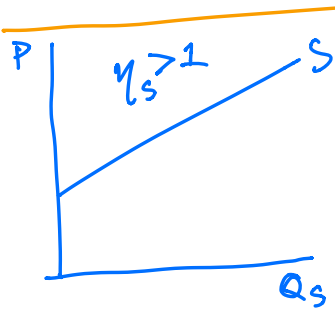
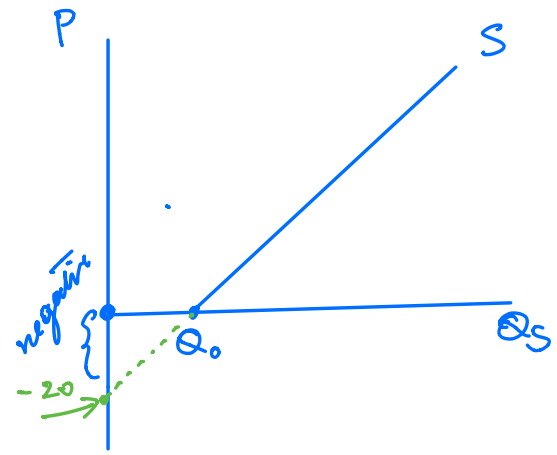
① price = -5 & sellers still are willing available to sell Q_0

- Example price of crude oil was negative during COVID-19 pandemic.

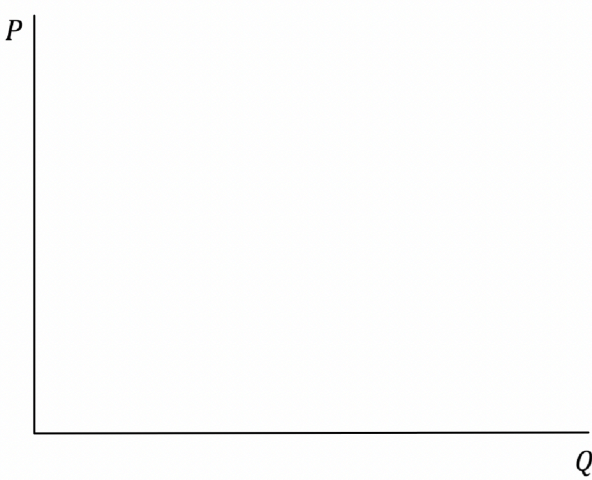


② At price = 0, $Q_S = Q_0$ but at price < 0, $Q_S = 0$.

Supply $P = -20 + \frac{1}{10} Q_S$.

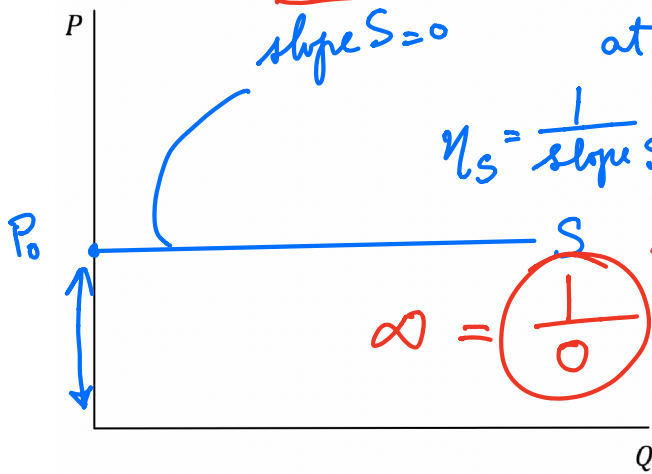


Point Elasticity of a Nonlinear Supply curve ✓



Extreme Cases

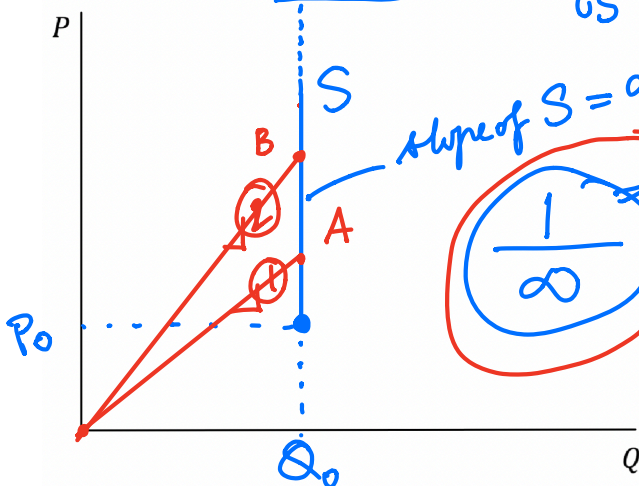
1. Supply is Perfectly Elastic - $\eta_S = \infty$ - S is horizontal.



at P_0 , Q_S is ∞ - as much as what is demanded by the market will be produced.
but at price $< P_0$, $Q_S = 0$

$$\eta_S = \frac{1}{\text{slope } S} \cdot \frac{P_0}{Q_0} = \infty$$

2. Supply is Perfectly Inelastic = $\eta_S = 0$



$\eta_S = \frac{1}{\text{slope of } S} \cdot \frac{P_0}{Q_0} = 0$
At price $\geq P_0$, $Q_S = Q_0$.
but at price $< P$, $Q_S = 0$.

