

Exercise 4
Keynesian Cross and Fiscal Policy

1. Answer the following questions.

1.1 Suppose Govt Multiplier is 5 and $\Delta G = 5$. Find ΔY .

1.2 Suppose Tax Multiplier is -3 and $\Delta Y = -9$. Find ΔT .

1.3 Suppose $\Delta Y = 10$ and $\Delta I = 2$. Find Investment Multiplier.

$$1.1 \quad \frac{\Delta Y}{\Delta G} = \text{Govt Mult}$$

$$\frac{\Delta Y}{5} = 5$$

$$\Delta Y = 25$$

$$1.2 \quad \frac{\Delta Y}{\Delta T} = \text{Tax Mult.}$$

$$\frac{-9}{\Delta T} = -3$$

$$\Delta T = 3$$

$$1.3 \quad \frac{\Delta Y}{\Delta I} = \frac{10}{2} = 5$$

2. From $Y = C + I + G$ where $C = C_0 + C_1(Y - T)$, find

2.1 Equilibrium Output Y^*

2.2 $\Delta Y / \Delta I$

2.3 $\Delta Y / \Delta G$

2.4 $\Delta Y / \Delta T$

2.5 Balanced-Budget Multiplier (BBM)

2.6 Explain what the BBM is.

2.1 $Y = AE$

$$Y = C_0 + C_1 Y - C_1 T + I + G$$

$$Y - C_1 Y = C_0 - C_1 T + I + G$$

$$Y(1 - C_1) = C_0 - C_1 T + I + G$$

$$Y = \frac{1}{1 - C_1} (C_0 - C_1 T + I + G)$$

2.2 $\frac{\Delta Y}{\Delta I} = \frac{1}{1 - C_1}$

2.3 $\frac{\Delta Y}{\Delta G} = \frac{1}{1 - C_1}$

2.4 $\frac{\Delta Y}{\Delta T} = \frac{-C_1}{1 - C_1} \rightarrow \text{MPC}$

2.5 $\Delta G = \Delta T$

$$\text{BBM} = G \text{ out. Mult.} + T \text{ ax Mult.}$$

$$= \frac{1}{1 - C_1} + \frac{C_1 - C_1}{1 - C_1}$$

$$= \frac{1 - C_1}{1 - C_1} = 1$$

2.6 A situation in financial planning or budgeting process where total planned spending Govt. Spending = tax
BBM tell us how Y^* change when both T & G increases by 1 units

3. Assume a closed economy with government. The country has the following components of aggregate expenditure.

$$C = 300 + 0.75(Y_d)$$

$$I = 50$$

$$G = 50$$

$$T = 50 \text{ (lump-sum tax)}$$

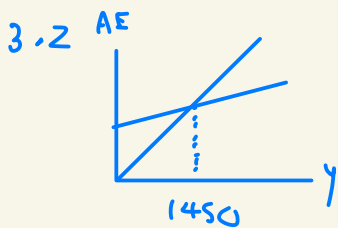
- 3.1 Use the $Y = AE$ (standard) approach to find the equilibrium output.
- 3.2 Draw the Keynesian Cross, and find the intercept on the vertical axis and the slope of the AE schedule.
- 3.3 Use the Leakage = Injection (or saving/investment) approach to find the equilibrium level of output.
(Hint: the equilibrium condition is $S + T = I + G$, with $Y_d = Y - T = C + S$)
- 3.4 Draw the saving/investment curve to show the equilibrium.
- 3.5 Suppose that the government decides to build more roads, raising government spending by 50 units, but this project is to be financed by the increase in net taxes of 50 units. Use the $Y = AE$ (standard) approach to find the new equilibrium output.
- 3.6 Use the Balanced-Budget Multiplier (BBM) derived from Question 2.5 to find the new equilibrium output.

$$3.1 \quad Y = AE = C + I + G$$

$$Y = 300 + 0.75Y - 375 + 50 + 50$$

$$0.25Y = 362.5$$

$$Y = 1450$$



$$C = a + bY$$

$$C = 300 + 0.75(Y_d)$$

$$\therefore \text{intercept} = 300$$

$$\text{slope} = 0.75$$

3.3 Leakage = Injection

$$S + T = I + G$$

$$S + 50 = 50 + 50$$

$$S = 50$$

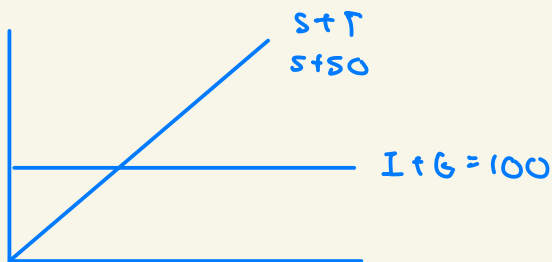
$$Y - T = C + S$$

$$Y - 50 = C + C_k(Y - 50) + S$$

$$Y = 362.5 + 0.75Y$$

$$Y = 1450$$

3.4



3.5 $Y = AE = C + I + G + (X - M)$

$$AE = 300 + 0.75(Y - 100) + 50 + 100$$

$$= 300 + 0.75Y + 75$$

$$0.25Y = 375$$

$$Y^* = 1500$$

3.6

$$\frac{\Delta Y}{\Delta G \& T} = 1$$

$$\frac{\Delta Y}{50} = 1$$

$$\Delta Y = 50$$

$$\therefore \text{new } Y^* = 1450 + 50$$

$$= 1500$$

4. From $Y = C + I + G + (X - M)$
where $C = C_0 + C_1(Y - T)$ and $M = M_0 + M_1(Y)$, find

4.1 Equilibrium Output Y^*

4.2 $\Delta Y / \Delta I$

4.3 $\Delta Y / \Delta G$

4.4 $\Delta Y / \Delta T$

4.5 Balanced-Budget Multiplier (BBM)

4.1 Equilibrium output Y^*

$$Y = C_0 + C_1 Y + I + G + X - M_0 - M_1 Y$$

$$Y(1 - C_1 + M_1) = C_0 - C_1 T + I + G + X - M_0$$

$$Y = \frac{1}{1 - C_1 + M_1} (C_0 - C_1 T + I + G + X - M_0)$$

4.2 $\Delta Y / \Delta I$

$$\frac{\Delta Y}{\Delta I} = \frac{1}{1 - C_1 + M_1}$$

4.3 $\Delta Y / \Delta G$

$$\frac{\Delta Y}{\Delta G} = \frac{1}{1 - C_1 + M_1}$$

4.4 $\Delta Y / \Delta T$

$$\frac{\Delta Y}{\Delta T} = - \frac{C_1}{1 - C_1 + M_1}$$

4.5 BBM

$$\text{BBM} = \frac{1 - C_1}{1 - C_1 + M_1}$$

5. Assume an open economy with government. The country has the following components of aggregate expenditure.

$$C = 200 + 0.7(Y_d)$$

$$I = 75$$

$$G =$$

$$75$$

$$T = 50$$

$$X = 50$$

$$M = 50 + 0.1Y$$

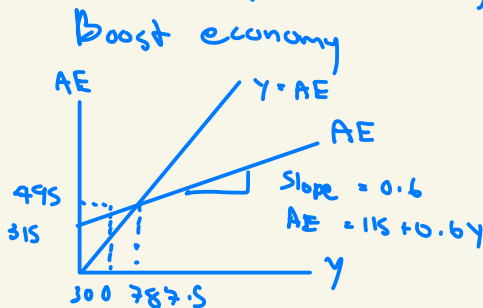
- 5.1 Use the $Y = AE$ approach to find the equilibrium. Is $Y = 300$ an equilibrium? If it is not, explain the adjustment process towards equilibrium.
- 5.2 Based on what you have derived in Question 4, calculate the investment, government spending, tax, and balanced-budget multipliers.
- 5.3 Interpret the value of each of the multipliers.
- Suppose that the full-employment output (Y_F) is 600;
- 5.4 What type of output gap is the economy currently experiencing?
- 5.5 Draw the Keynesian Cross. Identify its slope and intercept. Also, illustrate the output gap.
- Now, government wants to correct the output gap by moving the economy to the full-employment level, and is considering different policies.
(Hint: use the multipliers from Question 5.2 to answer the following questions)
- 5.6 If the government wants to adjust **only its spending (G)**, how much G should be changed?
- 5.7 If the government wants to adjust **only its net taxes (T)**, how much T should be changed?
- 5.8 If the government wants to boost **only investment (I)**, how much I should be changed?
- 5.9 If the government wants to implement a balanced-budget policy, what should the government do with G and T?

5.1 $Y = 200 + 0.7Y - 35 + 75 + 75 + 50 - 50 - 0.1Y$

$$0.4Y = 315$$

$$Y = 787.5$$

$Y = 300$ is not Y an Equilibrium. Income has to adjust towards equilibrium by business increase their production, Govt. raise, Govt. spending, reduce tax



$$AE > Y$$

S.2 invest multi. = $\frac{\Delta Y}{\Delta I} = \frac{787.5}{75} = 10.5$

gout. multi. = $\frac{\Delta Y}{\Delta G} = \frac{787.5}{75} = 10.5$

= $\frac{1}{1 - C_1 + M_1} = \frac{1}{1 - 0.6} = 2.5$

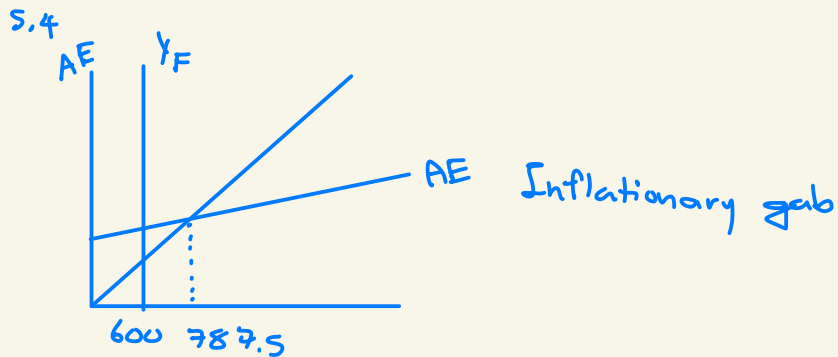
tax multi = $\frac{\Delta Y}{\Delta T} = \frac{787.5}{50} = 15.75$

= $\frac{-C_1}{1 - C_1 + M_1} = \frac{-0.7}{0.4} = -1.75$

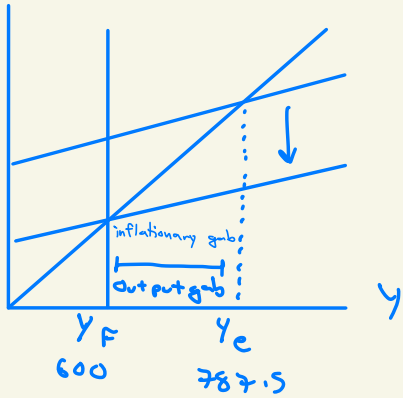
BBM = $10.5 + 15.75 = 26.25$

= $2.5 + (-1.75) = 0.75$

- S.3 invest multi. = if investment increase 1 unit, Y increase 2.5 units
 Gout. multi. = if Gout. spending increase 1 unit, Y increase 2.5 units
 tax multi. = if tax increase 1 units, Y decrease 1.75 units
 BBM multi. = if Gout. spending & tax both increase 1 unit, Y increase 0.75 units



5.5 AE



$$C = a + by$$

$$= 200 + 0.7(Y_d)$$

$$\text{intercept} = 200$$

$$\text{slope} = 0.7$$

$$AE = 315 + 0.6Y$$

$$\text{intercept} = 315$$

$$\text{slope} = 0.7$$

5.6

$$\frac{\Delta Y}{\Delta G} = 10.5$$

$$\frac{187.5}{\Delta G} = 10.5$$

$$\Delta G = 0.056 \text{ units}$$

(Govt should decrease G by 75)

$$\frac{\Delta Y}{\Delta G} = 2.5$$

$$\Delta Y = -187.5$$

$$\frac{-187.5}{\Delta G} = 2.5$$

$$\Delta G = -75$$

5.7

$$\frac{\Delta Y}{\Delta T} = 15.75$$

$$\frac{787.5}{\Delta T} = 15.75$$

$$\Delta T = 0.02 \text{ units}$$

$$\frac{\Delta Y}{\Delta T} = -1.75$$

$$\Delta Y = -187.5$$

$$\frac{-187.5}{\Delta T} = -1.75$$

$$\Delta T = 107.14$$

(Govt. should raise T)

$$5.8 \quad \frac{\Delta Y}{\Delta I} = 10.5$$

$$\frac{787.5}{\Delta I} = 10.5$$

$$\Delta I = 0.056 \text{ unit}$$

$$\Delta I = -1.5$$

$$5.9 \quad \frac{\Delta Y}{\text{BBM}} = 21.25$$

$$\frac{787.5}{\text{BBM}} = 21.25$$

$$\text{BBM} = 0.027 \text{ units}$$

$$\frac{\Delta Y}{\text{BBM}} = 0.75$$

$$\frac{187.5}{\text{BBM}} = 0.75$$

$$\text{BBM} = 250$$

Govt. will reduce Govt spending 250 units
reduce tax 250 units

6. Explain the role of Import as an automatic stabilizer. If the government wants to further stabilize the economy, is there anything that the government can do with its tax system? Explain.

- 6 • when the econ is bad, govt. has to decrease tax & import the people will have more income to spent domestically which can help boost economy during bad time
- when the econ is good, govt. has to increase tax & import the people will have less income to spent domestically which can help slow down economy during bad time

7. Let $S = -200 + 0.5Y$ and $I = 50$, be the saving function and investment.

7.1 Use the saving/investment approach to find the equilibrium output.

7.2 Find the equilibrium saving. (Hint: substitute Y^* into S)

Suppose people decide to save more, increasing autonomous saving by 100.

7.3 Use the saving/investment approach to find the new equilibrium output.

7.4 Find the new equilibrium saving. (Hint: substitute new Y^* into S)

7.5 Comment on your result.

7.1 $S = I$

$$-200 + 0.5Y = 50$$

$$Y^* = 500$$

7.2 $S^* = -200 + 0.5(500)$

$$S^* = 50$$

7.3 $S = -200 + 0.5Y + 100$

$$S' = -100 + 0.5Y$$

$$S' = I \rightarrow -100 + 0.5Y = 50$$

$$Y^* = 300$$

7.4 $S^* = -100 + 0.5(300)$

$$S^* = 50$$

