

## Capital Asset Pricing Model (CAPM)

CAPM: 
$$r_{jt} = \alpha_j + \beta_{j1}r_{mt} + \varepsilon_{jt}$$

. reg rj rm

Source	SS	df	MS	Number of obs	=	11,959
Model	11449.5344	1	11449.5344	F(1, 11957)	=	5988.94
Residual	22859.1346	11,957	1.91177842	Prob > F	=	0.0000
				R-squared	=	0.3337
				Adj R-squared	=	0.3337
Total	34308.669	11,958	2.86909759	Root MSE	=	1.3827

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
rm	.9947206	.0128536	77.39	0.000	.9695254 1.019916
_cons	.0084273	.0126552	0.67	0.505	-.0163789 .0332335

Fama & French: 
$$r_{jt} = \alpha_j + \beta_{j1}r_{mt} + \beta_{j2}r_{smbt} + \beta_{j3}r_{hmlt} + \varepsilon_{jt}$$

. reg rj rm smb hml

Source	SS	df	MS	Number of obs	=	11,959
Model	11681.1999	3	3893.73328	F(3, 11955)	=	2057.22
Residual	22627.4691	11,955	1.89272013	Prob > F	=	0.0000
				R-squared	=	0.3405
				Adj R-squared	=	0.3403
Total	34308.669	11,958	2.86909759	Root MSE	=	1.3758

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
rm	1.005554	.0128271	78.39	0.000	.9804104 1.030697
smb	.0371377	.0061189	6.07	0.000	.0251437 .0491318
hml	.0562866	.00609	9.24	0.000	.0443492 .068224
_cons	.0073088	.0125928	0.58	0.562	-.0173752 .0319928

- 1) There doesn't exist any Jensen Alpha.  
 In CAPM model, Alpha is insignificant (P-Value = 0.505).  
 In Fama & French model, Alpha is also insignificant (P-Value = 0.897)

- 2) To determine if portfolio f has the same risk as the market we should perform t-test. My hypothesis is  $H_0: \beta_1 = 1$

In CAPM, Portfolio J has the same risk as Market risk since, we failed to reject  $\beta_j = 1$  (P-Value is 0.6813)

```
. test rm=1
(1)  rm = 1

      F( 1, 11957) =    0.17
      Prob > F =    0.6813
```

In FF, Portfolio J has the same risk as Market risk since, we failed to reject  $\beta_j = 1$  (P-Value is 0.6651)

```
. test rm = 1
(1)  rm = 1

      F( 1, 11955) =    0.19
      Prob > F =    0.6651
```

3) From the Regression result of FF Model above, we could interpret that size premium is significant since we reject  $\beta_{smb}$  which has p-value of 0.000

4) From the Regression result of FF Model above, we could interpret that growth premium is significant since we reject  $\beta_{hml}$  which has p-value of 0.000

5) To test whether CAPM or FF model is more appropriate or should we eliminate SMB and HML. We could test our hypothesis  $H_0: \beta_{smb} = \beta_{hml} = 0$ .

```
. test smb hml
(1)  smb = 0
(2)  hml = 0

      F( 2, 11955) =    61.20
      Prob > F =    0.0000
```

We reject  $H_0$ , Thus  $\beta_{smb}$  and  $\beta_{hml}$  have significant impact on the model.

$$r_{jt} = \alpha_j + \gamma_j D_{jt} + \beta_{j1} r_{mt} + \beta_{j2} r_{smbt} + \beta_{j3} r_{hmlt} + \varepsilon_{jt} \quad (3)$$

```
. reg rj rm smb hml dl
```

Source	SS	df	MS	Number of obs	=	11,959
Model	11683.8263	4	2920.95657	F(4, 11954)	=	1543.31
Residual	22624.8427	11,954	1.89265875	Prob > F	=	0.0000
Total	34308.669	11,958	2.86909759	R-squared	=	0.3406
				Adj R-squared	=	0.3403
				Root MSE	=	1.3757

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
rm	1.005405	.0128275	78.38	0.000	.9802607 1.030549
smb	.0369291	.0061214	6.03	0.000	.0249302 .048928
hml	.0562495	.00609	9.24	0.000	.0443121 .0681868
dl	.05393	.045781	1.18	0.239	-.0358082 .1436682
_cons	.0028773	.0131425	0.22	0.827	-.0228842 .0286388

6) From the model, The effect on January is denoted by dl which has a P-value of 0.239. Thus, It is insignificant.

7) From the model, We could see that excess return on Market portfolio at time t, size premium and Value premium have positive relationship with the return from portfolio J. The overall F-test has P-value less than 0. Thus, This suggest that Rm, SMB, HML is enough to explain explanatory variables.

According to  $R^2$ , This model could explain dependent variable by 34.06% for individual test, rm, smb and hml are considered significant since P-value is 0.000 but dl which is dummy variable about January effect is considered insignificant. Thus, January effect might not happen in this case (P-value is 0.239 which is greater than 0.05).

8)

# Chan Test.

1

```
. reg rj rm smb hml
Source      SS          df         MS      Number of obs = 11,959
          22627.4691    11,955    1.89272013    F(3, 11955) = 2057.22
Model      11681.1999         3    3893.73328    Prob > F = 0.0000
Residual   22627.4691    11,955    1.89272013    R-squared = 0.3405
          34308.669    11,958    2.86909759    Adj R-squared = 0.3403
Total      34308.669    11,958    2.86909759    Root MSE = 1.3758

_____
rj          Coef.    Std. Err.    t    P>|t|    [95% Conf. Interval]
_____
rm          1.005554    .0128271    78.39    0.000    .9804104    1.030697
smb         .0371377    .0061189     6.07    0.000    .0251437    .0491318
hml         .0562866    .00609      9.24    0.000    .0443492    .068224
_cons      .0073088    .0125928     0.58    0.562    -.0173752    .0319928

. sca rss1=e(rss)
. sca n1=e(N)
```

2

```
. reg rj rm smb hml if d1== 0
Source      SS          df         MS      Number of obs = 10,974
          20936.975    10,970    1.90856654    F(3, 10970) = 1887.21
Model      10805.6192         3    3601.87308    Prob > F = 0.0000
Residual   20936.975    10,970    1.90856654    R-squared = 0.3404
          31742.5942    10,973    2.89279087    Adj R-squared = 0.3402
Total      31742.5942    10,973    2.89279087    Root MSE = 1.3815

_____
rj          Coef.    Std. Err.    t    P>|t|    [95% Conf. Interval]
_____
rm          1.008159    .0134224    75.11    0.000    .9818484    1.034469
smb         .0364768    .0064347     5.67    0.000    .0238636    .04909
hml         .0553364    .0063956     8.65    0.000    .0427998    .0678729
_cons      .0027652    .0131985     0.21    0.834    -.0231062    .0286367

. sca rss2=e(rss)
. sca n2=e(N)
```

3

```
. reg rj rm smb hml if d1== 1
Source      SS          df         MS      Number of obs = 985
          1686.17832    981    1.71883621    F(3, 981) = 169.11
Model      872.032797         3    290.677599    Prob > F = 0.0000
Residual   1686.17832    981    1.71883621    R-squared = 0.3409
          2558.21111    984    2.59980804    Adj R-squared = 0.3389
Total      2558.21111    984    2.59980804    Root MSE = 1.311

_____
rj          Coef.    Std. Err.    t    P>|t|    [95% Conf. Interval]
_____
rm          .9725647    .0435176    22.35    0.000    .8871664    1.057963
smb         .0402395    .0198549     2.03    0.043    .0012766    .0792024
hml         .0659675    .0199538     3.31    0.001    .0268104    .1051246
_cons      .0580564    .0421181     1.38    0.168    -.0245956    .1407084

. sca rss3=e(rss)
. sca n3=e(N)
```

4

```
. sca ChowTest = ((rss1-rss2-rss3)/4)/((rss2+rss3)/(n2+n3-2*4))
. sca list ChowTest
ChowTest = .56997206
```

According to Chan test, January and other month has the same structure with PP since, we failed to reject the  $H_0: d_1 = 0 \text{ and } \text{smb}d_1 = 0 \text{ and } \text{hml}d_1 = 0 \text{ and } \text{rmd}d_1 = 0$ . Therefore PP model and Model (4) should be estimated as 1 model.

## F-test

1

```
. g hmld1=hml*d1
. reg rj rm smb hml d1 rmd1 smbd1 hmld1
Source      SS          df         MS      Number of obs = 11,959
          22623.1533    11,951    1.89299249    F(7, 11951) = 881.86
Model      11685.5157         7    1669.35938    Prob > F = 0.0000
Residual   22623.1533    11,951    1.89299249    R-squared = 0.3406
          34308.669    11,958    2.86909759    Adj R-squared = 0.3402
Total      34308.669    11,958    2.86909759    Root MSE = 1.3759

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rj          Coef.    Std. Err.    t    P>|t|    [95% Conf. Interval]
_____
rm          1.008159    .0133675    75.42    0.000    .9819563    1.034361
smb         .0364768    .0064084     5.69    0.000    .0239153    .0490383
hml         .0553364    .0063695     8.69    0.000    .0428511    .0678216
d1         .0552912    .0461135     1.20    0.231    -.0350988    .1456811
rmd1       -.035594    .0475853    -0.75    0.454    -.1288689    .0576808
smbd1      .0037628    .0217997     0.17    0.863    -.0389682    .0464937
hmld1      .0106311    .0218876     0.49    0.627    -.0322721    .0535344
_cons      .0027652    .0131445     0.21    0.833    -.0230002    .0285307
```

2

```
test d1 smbd1 hmld1 rmd1

( 1) d1 = 0
( 2) smbd1 = 0
( 3) hmld1 = 0
( 4) rmd1 = 0
```

F( 4, 11951) = 0.57  
 Prob > F = 0.6844

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