

EE325 homework 6

Chapter 6 question 3

i.) Take the derivative of $\hat{rdintens}$ with respect to sales and set it equal to 0:

$$0 = 0.0003 - 0.000000014 \text{ sales}$$

$$0.000000014 \text{ sales} = 0.0003$$

$$\text{Sales} = 0.0003 / 0.000000014$$

$$\text{Sales} = 21,428.5714$$

The marginal effect of sales then becomes negative when sales = 21,428.57

ii.) The t-statistic on $\hat{\beta}_{\text{sales}^2}$ is (note: $\hat{\beta}_{\text{sales}^2}$ is beta hat sales squared)

$$-0.0000000070 - 0 / 0.0000000037 = -1.89$$

From the t-statistic the outcome is $|t| < 1.96$ which means that sales^2 is not significant at 5% significance level. Therefore we should not keep the quadratic form

iii.) $\hat{rdintens} = 2.613 + 0.0003 \text{ sales} - 0.000000007 \text{ sales}^2$

$$= 2.613 + 0.0003 (1000 * \text{salesbil}) - 0.000000007(1000)^2 (\text{salesbil})^2$$

$$= 2.613 + 0.3 \text{ salesbil} - 0.0072 \text{ salesbil}^2$$

$$se(\hat{\beta}^j) = \hat{\sigma} / [SST_j(1 - R^2)]^{1/2}$$

Rescaling sales will have no effect on $\hat{\sigma}$ or R^2 since it does not change the fit of the regression. It will, however, affect SST_{sales} , SST_{sales^2} and the standard error.

Note: $\hat{\beta}^j$ is read as beta hat j and R^2 is R squared

iv.) The equation in iii.) is more easy to interpret because of the fewer zeros.

Chapter 7 question 1

i.) Coefficient on male is 87.75, so a man is estimated to sleep one and one-half hours more per week than a comparable woman. This is significant at the 1% level.

ii.) The coefficient estimate on totwrk is negative and significant at the 1% level. One more hour of work is associated with 0.163(60) or about 9.8 minutes less sleep.

iii.) The null we are interested in testing here is that the coefficients on age and age^2 are jointly zero. So, we will test the F-test $H: \beta_{\text{age}} = \beta_{\text{age}^2} = 0$

$$F = (R^2_{ur} - R^2_{r}) / q(1 - R^2_{ur}) / (n - k - 1)$$

Note: β_{age^2} is read as beta age squared

Chapter 7 question 8

i.) $\log(\text{wage}) = \beta_0 + \beta_1 \text{usage} + \beta_2 \text{educ} + \beta_3 \text{exper} + \beta_4 \text{female} + u$

ii.) $\log(\text{wage}) = \beta_0 + \beta_1 \text{usage} + \beta_2 \text{educ} + \beta_3 \text{exper} + \beta_4 \text{female} + \beta_5 \text{usage} \cdot \text{female} + u$

Test hypothesis: $H_0: \beta_5 = 0$ and $H_1: \beta_5 \text{ not equal } 0$

iii.) $\log(\text{wage}) = \beta_0 + \beta_1 \text{light} + \beta_2 \text{moderate} + \beta_3 \text{heavy} + \beta_4 \text{educ} + \beta_5 \text{exper} + \beta_6 \text{female} + u$

In this model, non-user is the omitted category.

iv.) The null hypothesis is $H_0: \beta_1 = \beta_2 = \beta_3 = 0$.

So this is going to be an F-test on $q = 3$ restrictions.

We are also going to have degrees of freedom $df = n - 6 - 1$ for a sample of size n , since we have 6 independent variables in the unrestricted model.

So we would be obtaining a critical value from the $F_{q, n-7}$ distribution

v.) There may be omitted variables for marijuana usage and wage.

Chapter 7 question 11

Note: β^j is read as beta hat j

R^2_{ur} is R squared ur

R^2_r is R squared r

i.) The coefficient for male is 3.83 this can be interpreted as the expected difference in class score between male and female is 3.83.

The 95% confidence interval for β_{male}

$$= [\beta^j - 1.96 \text{ s.e.}(\beta^j), \beta^j + 1.96 \text{ s.e.}(\beta^j)]$$

$$= 3.83 - 1.96(0.74), 3.83 + 1.96(0.74)$$

$$= 2.3786, 5.2084$$

ii.) $H_0: \beta_{\text{male}} = 0$ $H_a: \beta_{\text{male}} \cdot \text{colgpa} = 0$

$$F = \frac{[(R^2_{ur} - R^2_r)/q]}{[(1 - R^2_{ur})/(n-k-1)]}$$

$$= \frac{[(0.348 - 0.329)/2]}{(1 - 0.348)/(856-3-1)}$$

$$= 13.09$$

$F_{2854} = 13.09$ this is more than 3.01, we can reject H_0 that there is no gender difference in score at 5% significance level.

Computer exercise C4

i.) I think hspc will be negative

ii.)

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. reg colgpa hsize hsizeq hspc sat female athlete
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Source	SS	df	MS	Number of obs	=	4,137
Model	524.819305	6	87.4698842	F(6, 4130)	=	284.59
Residual	1269.37637	4,130	.307355053	Prob > F	=	0.0000
				R-squared	=	0.2925
				Adj R-squared	=	0.2915
Total	1794.19567	4,136	.433799728	Root MSE	=	.5544

colgpa	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
hsize	-.0568543	.0163513	-3.48	0.001	-.0889117 -.0247968
hsizeq	.0046754	.0022494	2.08	0.038	.0002654 .0090854
hspc	-.0132126	.0005728	-23.07	0.000	-.0143355 -.0120896
sat	.0016464	.0000668	24.64	0.000	.0015154 .0017774
female	.1548814	.0180047	8.60	0.000	.1195826 .1901802
athlete	.1693064	.0423492	4.00	0.000	.0862791 .2523336
_cons	1.241365	.0794923	15.62	0.000	1.085517 1.397212

Holding other factors fixed, an athlete is predicted to have a GPA about 0.169 points higher than a nonathlete.

The t statistic is $0.169/0.042 = 4.02$, which is more than 1.96 showing that it is statistically significant at 5% level of significance.

iii.)

```
. reg colgpa hsize hsizeq hspc female athlete
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Source	SS	df	MS	Number of obs	=	4,137
Model	338.217123	5	67.6434247	F(5, 4131)	=	191.92
Residual	1455.97855	4,131	.35245184	Prob > F	=	0.0000
				R-squared	=	0.1885
				Adj R-squared	=	0.1875
Total	1794.19567	4,136	.433799728	Root MSE	=	.59368

colgpa	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
hsize	-.0534038	.0175092	-3.05	0.002	-.0877313 -.0190763
hsizeq	.0053228	.0024086	2.21	0.027	.0006007 .010045
hspc	-.0171365	.0005892	-29.09	0.000	-.0182916 -.0159814
female	.0581231	.0188162	3.09	0.002	.0212333 .095013
athlete	.0054487	.0447871	0.12	0.903	-.0823582 .0932556
_cons	3.047698	.0329148	92.59	0.000	2.983167 3.112229

With sat dropped from the model, the coefficient on athletes becomes about 0.0054 (se 0.0448), which is not statistically significant.

This happens because we do not control for SAT scores, and athletes score lower on average than nonathletes.

Part (ii) shows that, once we account for SAT differences, athletes do better than nonathletes. Even if we do not control for SAT scores, there is no difference.

iv.)

```
. gen male = female == 0
. gen nonathlete = athlete == 0
. gen maleathlete = male*athlete

. gen malenonathlete = male*nonathlete

. gen femaleathlete = female*athlete

. reg colgpa hsize hsizesq hsperc sat femaleathlete maleathlete malenonathlete
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Source	SS	df	MS	Number of obs	=	4,137
Model	524.821272	7	74.9744674	F(7, 4129)	=	243.88
Residual	1269.3744	4,129	.307429015	Prob > F	=	0.0000
				R-squared	=	0.2925
				Adj R-squared	=	0.2913
Total	1794.19567	4,136	.433799728	Root MSE	=	.55446

colgpa	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
hsize	-.0568006	.0163671	-3.47	0.001	-.0888889	-.0247124
hsizesq	.0046699	.0022507	2.07	0.038	.0002573	.0090825
hsperc	-.0132114	.000573	-23.06	0.000	-.0143349	-.012088
sat	.0016462	.0000669	24.62	0.000	.0015151	.0017773
femaleathlete	.1751106	.0840258	2.08	0.037	.0103748	.3398464
maleathlete	.0128034	.0487395	0.26	0.793	-.0827523	.1083591
malenonathlete	-.1546151	.0183122	-8.44	0.000	-.1905168	-.1187133
_cons	1.39619	.0755581	18.48	0.000	1.248055	1.544324

The coefficient on femaleathlete shows that colgpa is predicted to be about 0.175 points higher for a female athlete than a female nonathlete, other variables in the equation fixed.

The hypothesis that there is no difference between female athletes and female nonathletes is testing by using the t statistic on femath.

t = 2.08, which is statistically significant at the 5% level against a two-sided alternative.

v.)

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. gen femalesat = female*sat
. reg colgpa hsize hsizeq hsperc sat femaleathlete maleathlete malenonathlete femalesat
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Source	SS	df	MS	Number of obs	=	4,137
Model	524.873728	8	65.609216	F(8, 4128)	=	213.37
Residual	1269.32195	4,128	.307490781	Prob > F	=	0.0000
				R-squared	=	0.2925
				Adj R-squared	=	0.2912
Total	1794.19567	4,136	.433799728	Root MSE	=	.55452

colgpa	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
hsize	-.0568198	.0163688	-3.47	0.001	-.0889114 -.0247282
hsizeq	.0046773	.002251	2.08	0.038	.0002641 .0090904
hsperc	-.0132236	.0005738	-23.04	0.000	-.0143487 -.0120986
sat	.001624	.0000858	18.93	0.000	.0014558 .0017922
femaleathlete	.1779989	.0843247	2.11	0.035	.0126771 .3433207
maleathlete	.0652958	.1361172	0.48	0.631	-.2015674 .3321589
malenonathlete	-.0990198	.1358427	-0.73	0.466	-.3653447 .1673051
femalesat	.0000539	.0001306	0.41	0.680	-.0002021 .00031
_cons	1.364334	.1079746	12.64	0.000	1.152646 1.576023

Its coefficient is about 0.00005 and its t statistic is about 0.40. There is very little evidence that the effect of sat differs by gender.