

# FN312 Investment

## Lecture 9 The Term Structure of Interest Rates

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# Outline

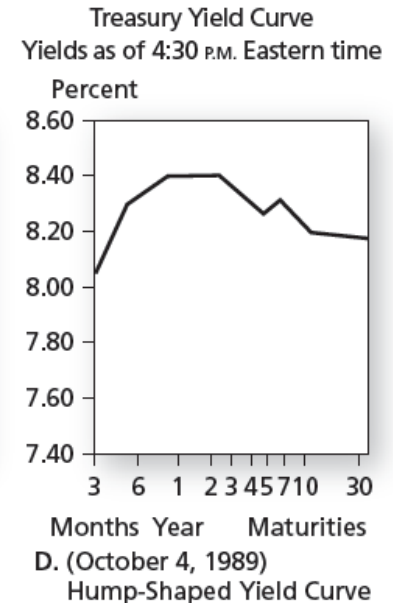
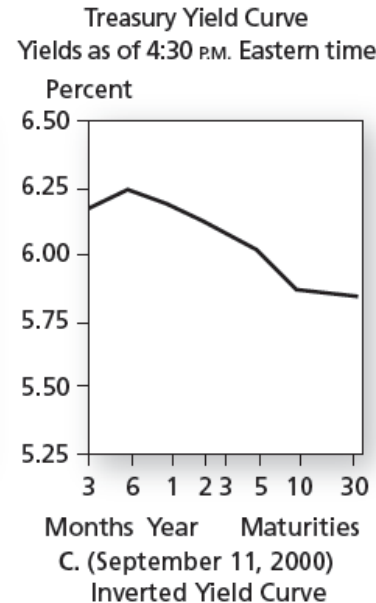
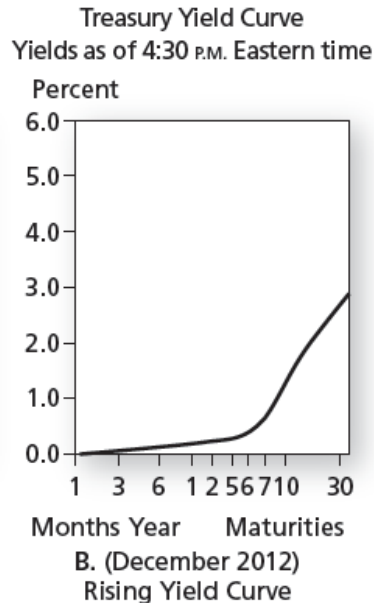
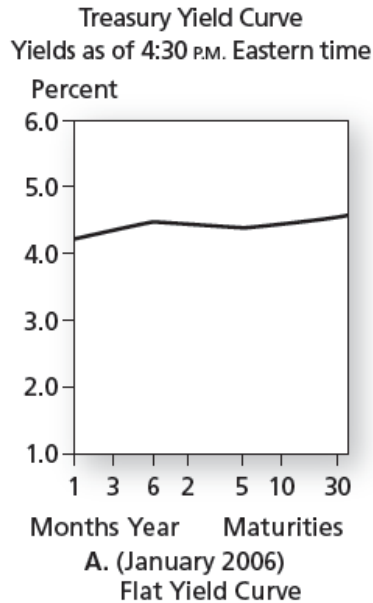
- The Yield Curve
- The Yield Curve and Future Interest Rates  
*(Yield Curve Under Certainty)*
- Interest Rate Uncertainty and Forward Rates
- Theories of Term Structure

Reading:  
Chapter 15

# The Yield Curve

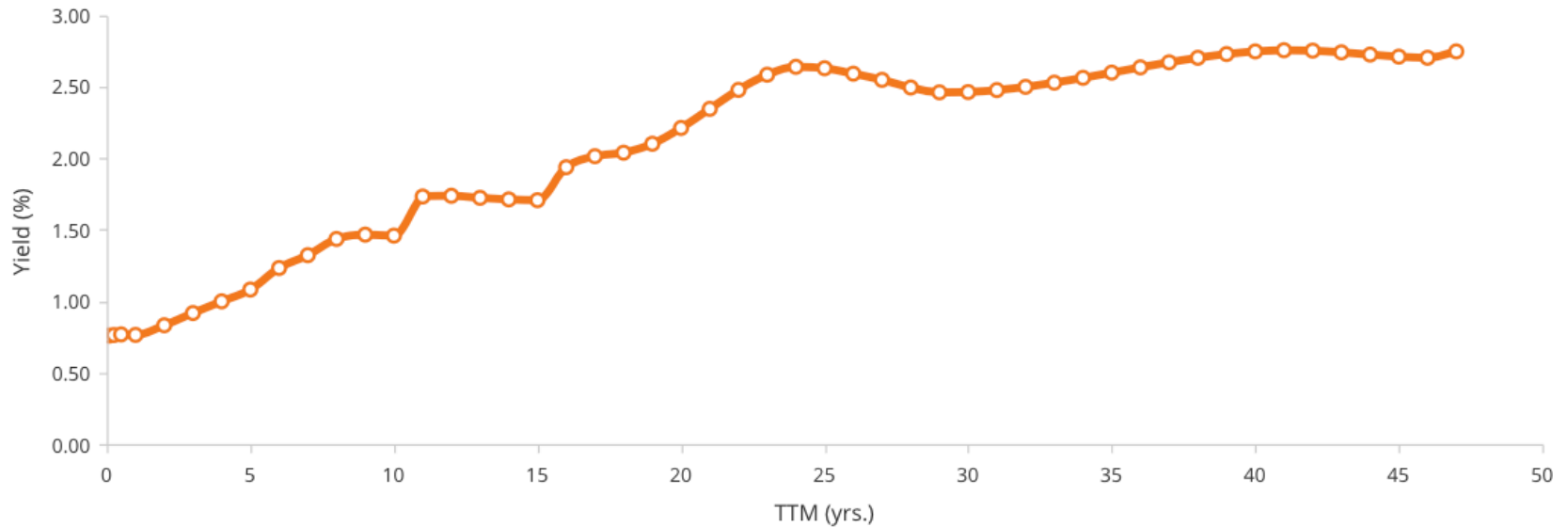
# The Yield Curve

- The yield curve displays the relationship between YTM and time to maturity
- Information on expected future short-term rates can be implied from the yield curve



# ThaiBMA Zero Coupon Yield Curve

ThaiBMA Zero Coupon Yield Curve  
as of Monday, March 30, 2020



30/03/2020


**Corporate Bond Yield Curve (Based on TTM ) as of 30 March 2020**

Export to Excel

Group	Averaged Spread (bp)			Standard Deviation (bp)			Averaged Maturity		
	<= 3 Yrs.	3 - 5 Yrs.	> 5 Yrs.	<= 3 Yrs.	3 - 5 Yrs.	> 5 Yrs.	<= 3 Yrs.	3 - 5 Yrs.	> 5 Yrs.
AAA	51.534149	95.364281	90.901228	20.422105	43.719392	12.264387	1.416327	4.160730	6.224200
AA	64.218871	88.352238	127.187882	40.870169	27.971279	27.500264	1.552054	3.915525	7.947677
A	79.779096	110.984949	143.938694	39.991232	39.547453	38.864430	1.392266	3.855825	8.105622
BBB	196.977724	275.639880	333.470930	47.877255	38.387682	50.847349	1.439524	3.868914	5.305479

**Corporate Bond Yield Curve (Based on Duration ) as of 30 March 2020**

Export to Excel

Group	Averaged Spread (bp)			Standard Deviation (bp)			Averaged Maturity		
	<= 3 Yrs.	3 - 5 Yrs.	> 5 Yrs.	<= 3 Yrs.	3 - 5 Yrs.	> 5 Yrs.	<= 3 Yrs.	3 - 5 Yrs.	> 5 Yrs.
AAA	51.801641	100.392322	91.877112	20.438278	27.801772	17.438578	1.438904	5.249771	7.609589
AA	64.995067	93.871648	133.630535	40.834550	26.592841	25.870294	1.633294	4.306544	8.402896
A	80.925123	114.354598	152.205665	40.402980	39.637731	37.120021	1.452697	4.228980	8.565720
BBB	199.159881	288.250804		48.873841	46.010477		1.486692	4.209694	

**Remark :**

1. Each rating group includes all signs. For example, AA group consists of rating AA+, AA and AA-.
2. Averaged Spread is simple average of spreads.
3. Blank means there is no bonds in the criteria.
4. Averaged averaged maturity means the average of average maturities of all bonds in the criteria.
5. Averaged maturity of each bond is calculated from:  $\text{sum}(\text{principal} * \text{time}) / \text{sum}(\text{principals})$

# Interpreting the Term Structure

- The yield curve reflects expectations of future interest rates
  - The forecasts are clouded by liquidity premiums
  - An upward sloping curve could indicate:
    - Rates are expected to rise
- and/or*
- Investors require large liquidity premiums to hold long term bonds

# Interpreting the Term Structure

- The yield curve is a good predictor of the business cycle
  - Long term rates tend to rise in anticipation of economic expansion
  - Inverted yield curve may indicate that interest rates are expected to fall and signal a recession

# Yield Curve: Bond Pricing

- Yields on different maturity bonds are not all equal
- Consider each bond cash flow as a stand-alone zero-coupon bond
- **Bond stripping and bond reconstitution offer opportunities for arbitrage**
- The value of the bond should be the sum of the values of its parts

# Prices and Yields to Maturities on Zero-Coupon Bonds (\$1,000 Face Value)

Maturity (years)	Yield to Maturity (%)	Price
1	5%	\$952.38 = \$1,000/1.05
2	6	\$890.00 = \$1,000/1.06 <sup>2</sup>
3	7	\$816.30 = \$1,000/1.07 <sup>3</sup>
4	8	\$735.03 = \$1,000/1.08 <sup>4</sup>

# Example 1: Zero Price or Face Value > Coupon Bond

Face (Zero)	1000	Sold at (CB)	800
C Rate	5%	\$50	
N =	5		

Step1: Buy

GAIN (Loss)=

Step2: Sell

NET

Total

## Example 2: Zero Price or Face Value < Coupon Bond

Face (Zero)	1000	Sold at (CB)	1200
C Rate	5%	\$50	
N =	5		

Step1: Buy

GAIN (Loss)=

Step2: Sell Strip

NET

Total

# Valuing Coupon Bonds

- Value a 3-year, 10% coupon bond using discount rates from the TABLE:

*(1) Solving price from the YTM given:*

$$\text{Price} = \frac{\$100}{1.05} + \frac{\$100}{1.06^2} + \frac{\$1100}{1.07^3} = \$1082.17$$

*(2) Solving YTM of the coupon bonds:*

$$\text{YTM} = 6.88\%$$

>> which is less than the 3-year rate of 7% ... *So ?*

# Bond Pricing: Two Types of Yield Curves

## Pure Yield Curve

- Uses stripped or zero-coupon Treasuries
- May differ significantly from the on-the-run yield curve

## On-the-Run Yield Curve

- Uses recently-issued coupon bonds selling at or near par
- The one typically published by the financial press

# The Yield Curve and Future Interest Rates

*(Yield Curve Under Certainty)*

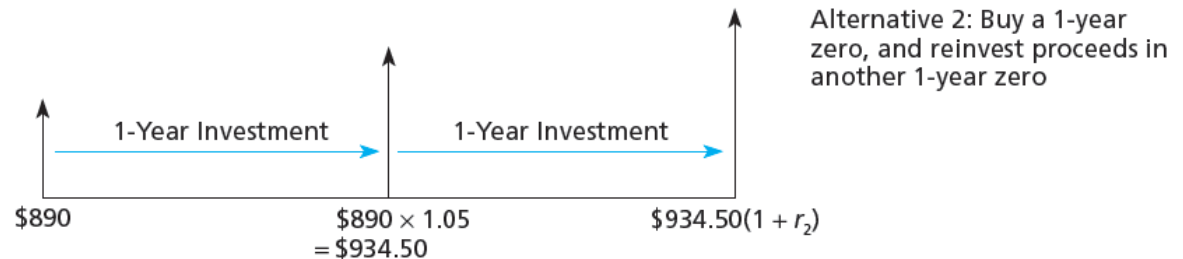
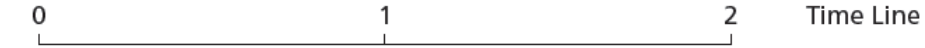
# The Yield Curve and Future Interest Rates (1)

- Yield Curve Under Certainty

- Suppose you want to invest for 2 years
  - Buy and hold a 2-year zero

OR

- Rollover a series of 1-year bonds
- Equilibrium requires that both strategies provide the same return



# The Yield Curve and Future Interest Rates (2)

- Yield Curve Under Certainty
  - Buy and hold vs. rollover:

$$(1 + y_2)^2 = (1 + r_1) \times (1 + r_2)$$
$$1 + y_2 = [(1 + r_1)(1 + r_2)]^{.5}$$

- $(r_2)$  is just enough to make rolling over a series of 1-year bonds equal to investing in the 2-year bond

*From previous example:*

# The Yield Curve and Future Interest Rates (3)

- Yield Curve Under Certainty
  - **Short rate**
    - The rate for a given maturity (e.g. one year) at different points in time
  - **Spot rate**
    - = the geometric average of its component short rates
    - The rate that prevails today for a given maturity

## Example (2)

13. Prices of zero-coupon bonds reveal the following pattern of forward rates:

Year	Forward Rate
1	5%
2	7
3	8

In addition to the zero-coupon bond, investors also may purchase a 3-year bond making annual payments of \$60 with par value \$1,000.

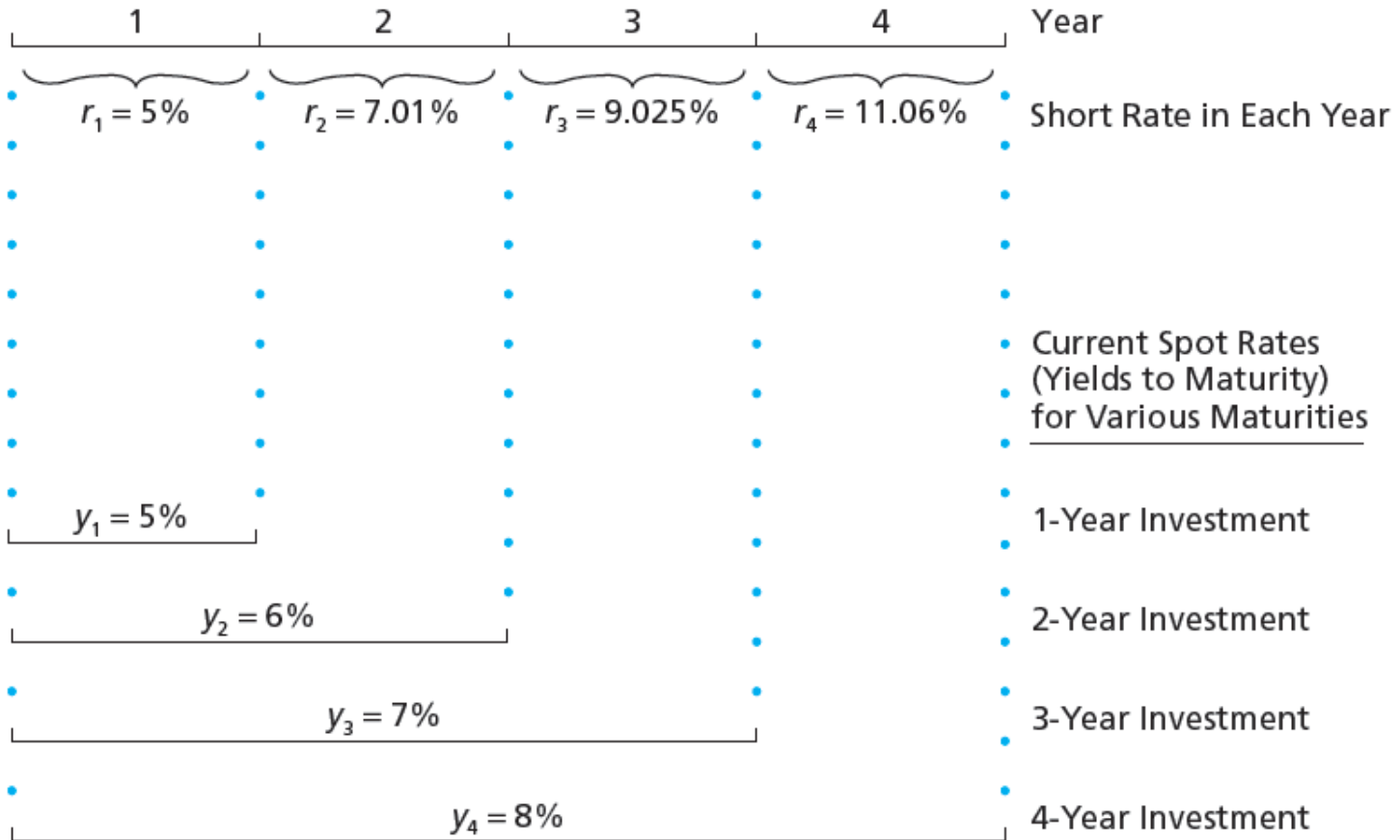
- What is the price of the coupon bond?
- What is the yield to maturity of the coupon bond?
- Under the expectations hypothesis, what is the expected realized compound yield of the coupon bond?
- If you forecast that the yield curve in one year will be flat at 7%, what is your forecast for the expected rate of return on the coupon bond for the 1-year holding period?

# The Yield Curve and Future Interest Rates (4)

## Short Rates and Yield Curve Slope

- When next year's short rate,  $r_2 > r_1$ , the yield curve slopes up
- May indicate rates are expected to rise
- When next year's short rate,  $r_2 < r_1$ , the yield curve slopes down
- May indicate rates are expected to fall

# Short Rates versus Spot Rates



# The Yield Curve and Future Interest Rates (5)

- Forward rates

$$(1 + y_n)^n = (1 + y_{n-1})^{n-1} \times (1 + f_n)$$

$$(1 + f_n) = \frac{(1 + y_n)^n}{(1 + y_{n-1})^{n-1}}$$

- $f_n$  = One-year forward rate for period  $n$
- $y_n$  = Yield for a security with a maturity of  $n$

# Forward Rates: Example

- The forward interest rate is a forecast of a future short rate
- Rate for 4-year maturity = 8%
- Rate for 3-year maturity = 7%

## Forward Rates: Example (2)

7. The following is a list of prices for zero-coupon bonds of various maturities.
- Calculate the yield to maturity for a bond with a maturity of (i) one year; (ii) two years; (iii) three years; (iv) four years.
  - Calculate the forward rate for (i) the second year; (ii) the third year; (iii) the fourth year.

Maturity (years)	Price of Bond
1	\$943.40
2	898.47
3	847.62
4	792.16

# Interest Rate Uncertainty and Forward Rates

# Interest Rate Uncertainty and Forward Rates (1)

- Suppose that today's rate is 5% and the *expected* short rate for the following year is  $E(r_2) = 6\%$ . The value of a 2-year zero is:
  
  
  
  
  
  
  
  
  
  
- The value of a 1-year zero is:

## Interest Rate Uncertainty and Forward Rates (2)

- The investor wants to invest for 1 year

*Option1:* Buy the 2-year bond today and plan to sell it at the end of the first year for  $\$1000/1.06 = \$943.40$

OR

*Option2:* Buy the 1-year bond today and hold to maturity

... So?

- What if next year's interest rate differs from 6%?
  - The actual return on the 2-year bond is UNCERTAIN!

## Interest Rate Uncertainty and Forward Rates (3)

- Investors require a risk premium to hold a longer-term bond
- This LIQUIDITY PREMIUM compensates short-term investors for the uncertainty about future prices

# Theories of Term Structure

# Theories of Term Structure

## (1) The Expectations Hypothesis Theory

- Observed long-term rate is a function of today's short-term rate and expected future short-term rates
- The forward rate equals the market consensus expectation of the future short interest rate
  - $f_n = E(r_n)$  and LIQUIDITY PREMIUMS ARE ZERO!

Recall that:  $(1 + y_2)^2 = (1 + r_1) \times (1 + r_2)$

# The Expectations Hypothesis Theory: Example

9. Consider the following \$1,000 par value zero-coupon bonds:

Bond	Years to Maturity	YTM(%)
A	1	5%
B	2	6
C	3	6.5
D	4	7

According to the expectations hypothesis, what is the market's expectation of the yield curve one year from now? Specifically, what are the expected values of next year's yields on bonds with maturities of (a) one year? (b) two years? (c) three years?

# Theories of Term Structure

## (2) Liquidity Preference Theory

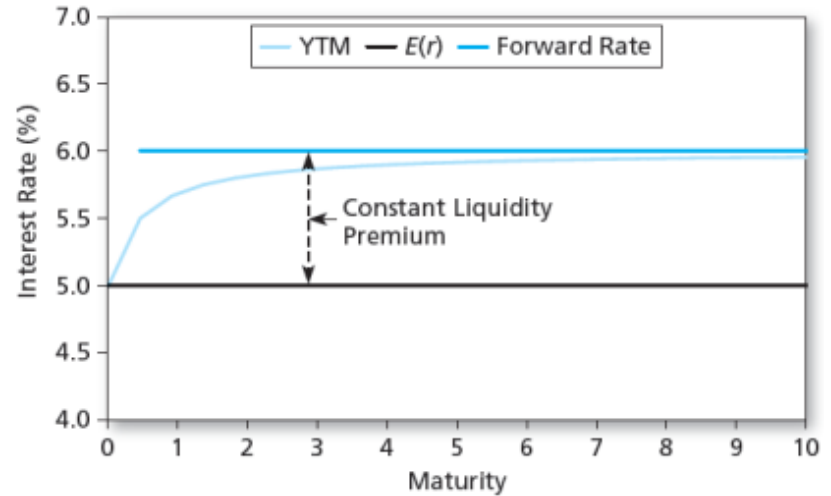
- Long-term bonds are riskier  $\Rightarrow f_n > E(r_n)$
- The excess of  $f_n$  over  $E(r_n)$  is the **LIQUIDITY PREMIUM!**
- The yield curve has an upward bias built into the long-term rates because of the liquidity premium

# Yield Curve Examples

## Panel A:

Constant Expected Short Rate  
Constant Liquidity Premium

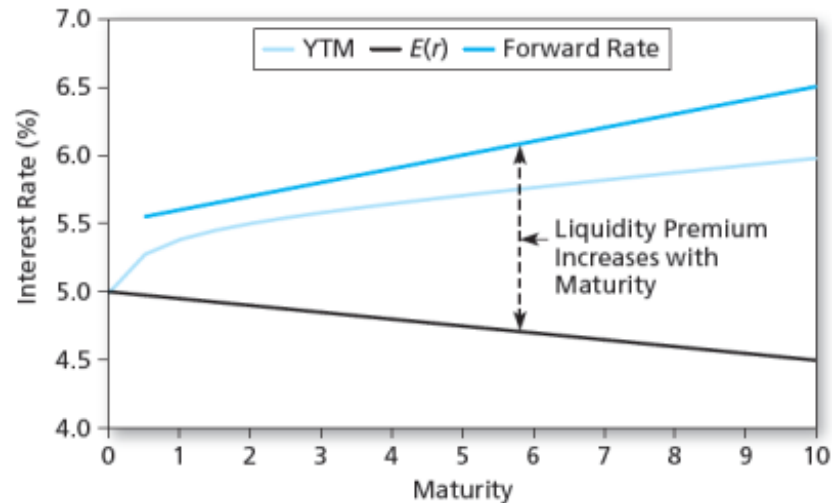
A



## Panel B:

Declining Expected Short Rate  
Increasing Liquidity Premiums

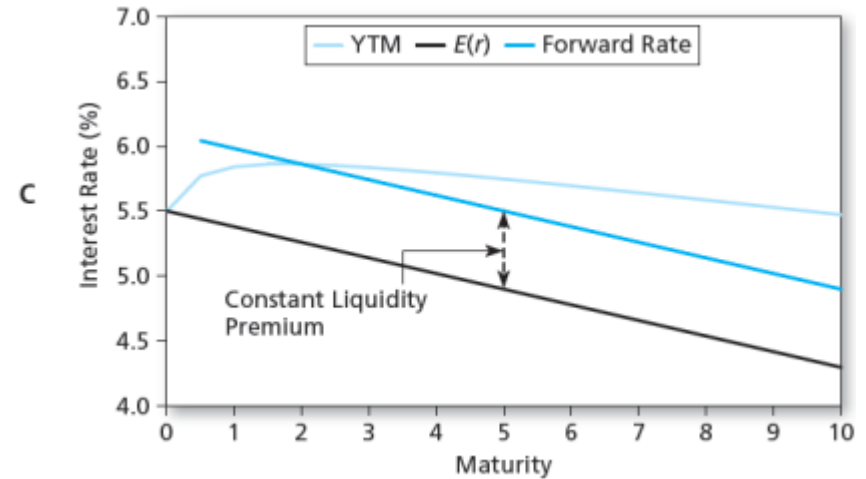
B



# Yield Curve Examples

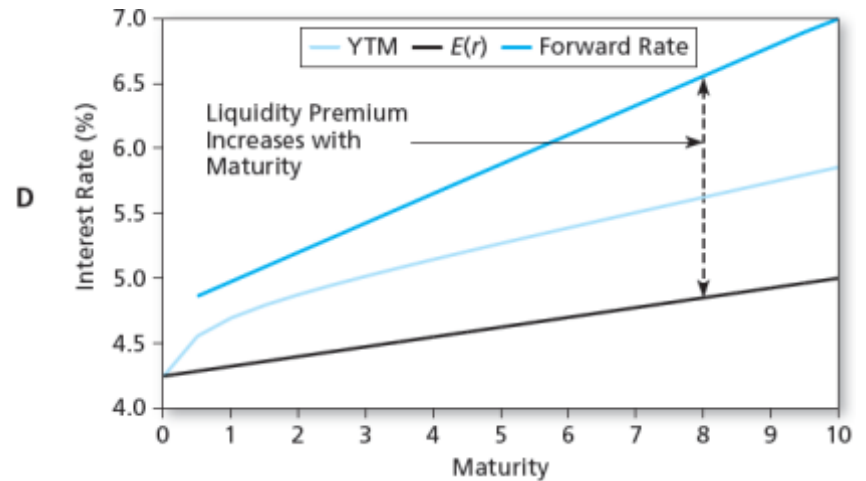
## Panel C:

Declining Expected Short Rate  
Constant Liquidity Premiums



## Panel D:

Increasing Expected Short Rates  
Increasing Liquidity Premiums



Question?