

Today.

- Review consumer's U-max problem

→ Utility & BC.
→ (X^*, Y^*) .

- Decomposition of income effect and substitution effect, when a price changes.

- Applications :

- ① Giffen
- ② Subsidy
- ③ Vouchers
- ④ Labour Mkt.
- ⑤ Inter-temporal consumption.

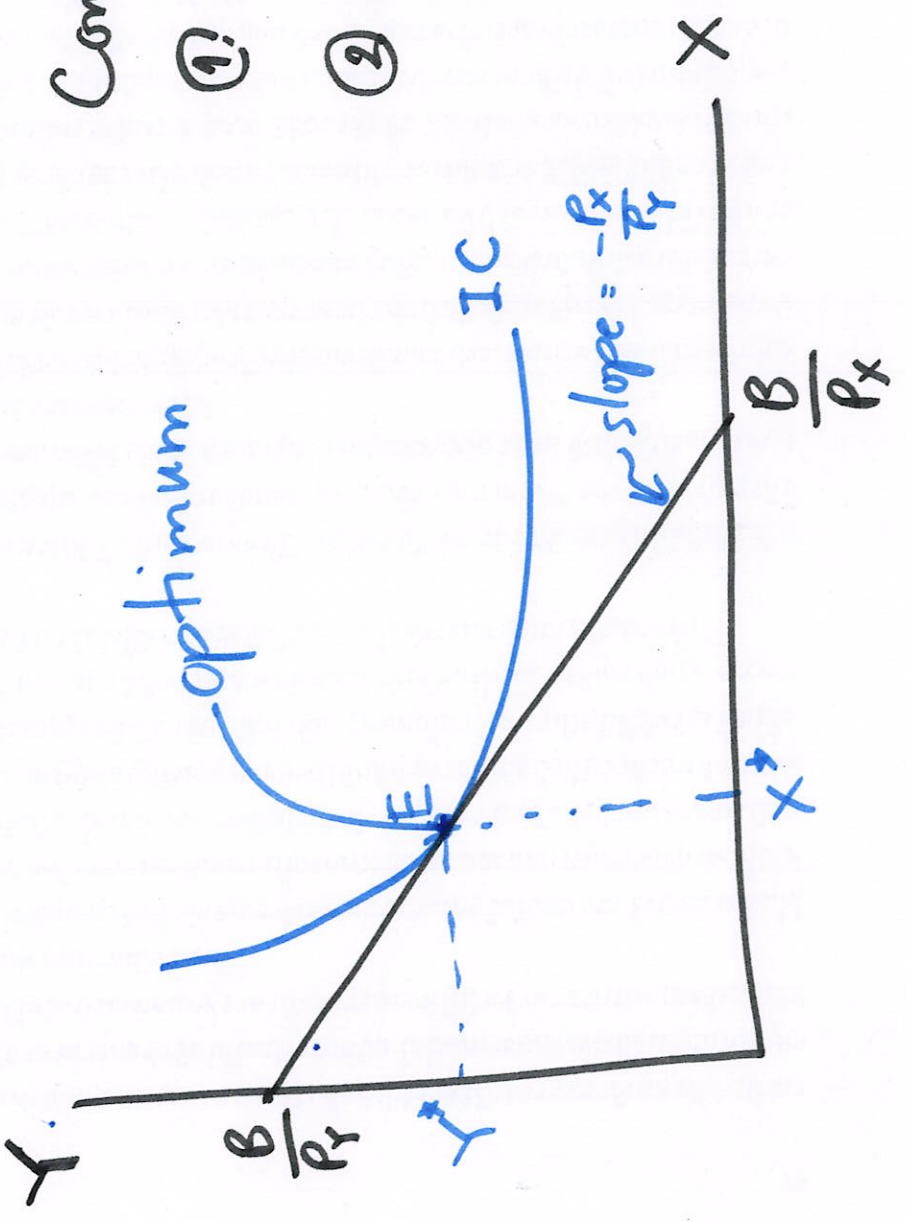
Utility - maximization Problem

$$\text{Max } U(X, Y)$$

$$\text{s.t. } P_x \cdot X + P_y \cdot Y = B$$

$$P_y \cdot Y = B - P_x \cdot X$$

$$Y = \frac{B}{P_y} - \frac{P_x}{P_y} \cdot X$$



Conditions for U-max:

- ① $P_x \cdot X^* + P_y \cdot Y^* = B$
 - ② slope of IC = slope of BC
- $$|MRS| = \left| \frac{P_x}{P_y} \right|$$

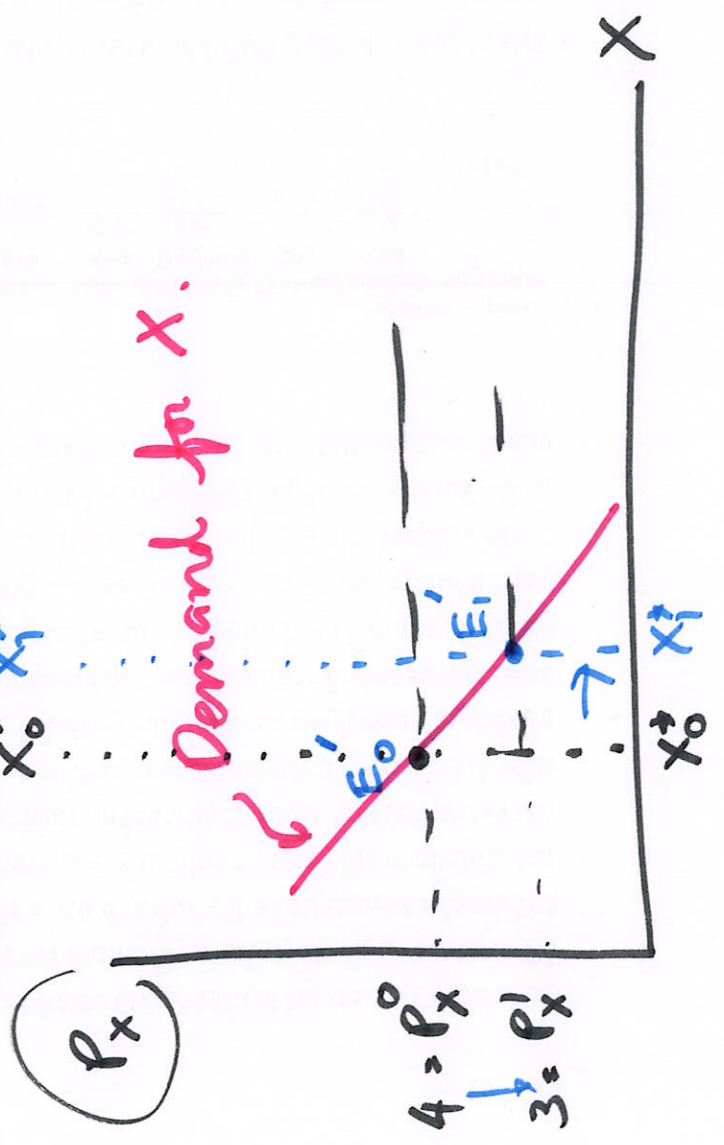
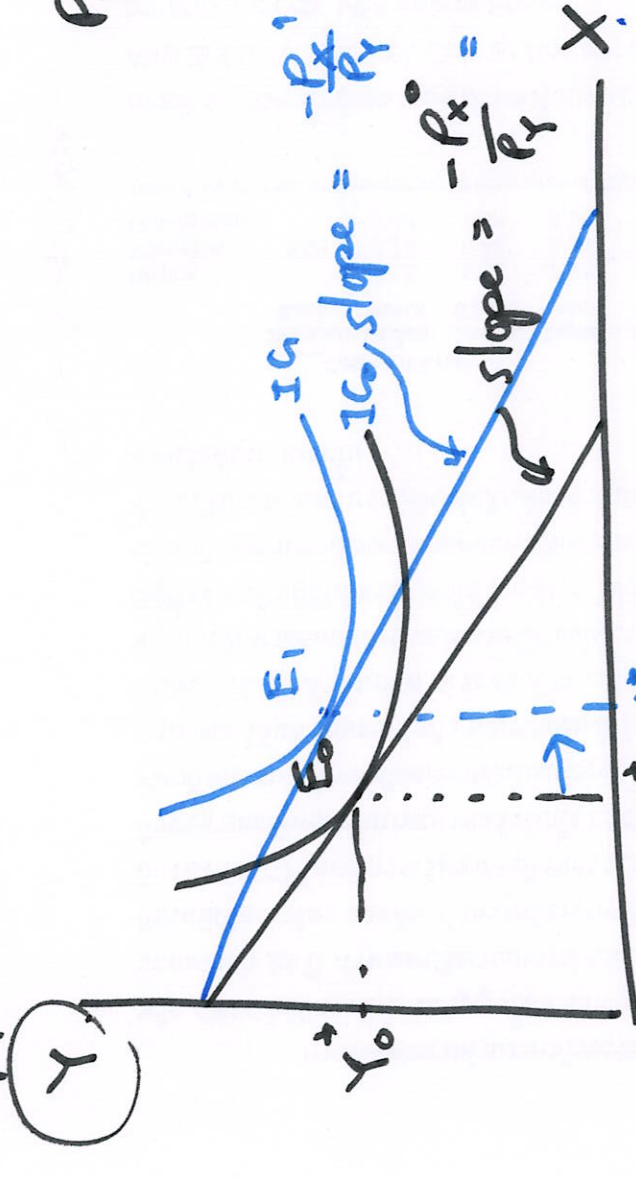
where $MRS = - \frac{MU_x}{MU_y}$

Suppose $P_x \downarrow$, ceteris paribus

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$P_x^1 < P_x^0$

3 → 4

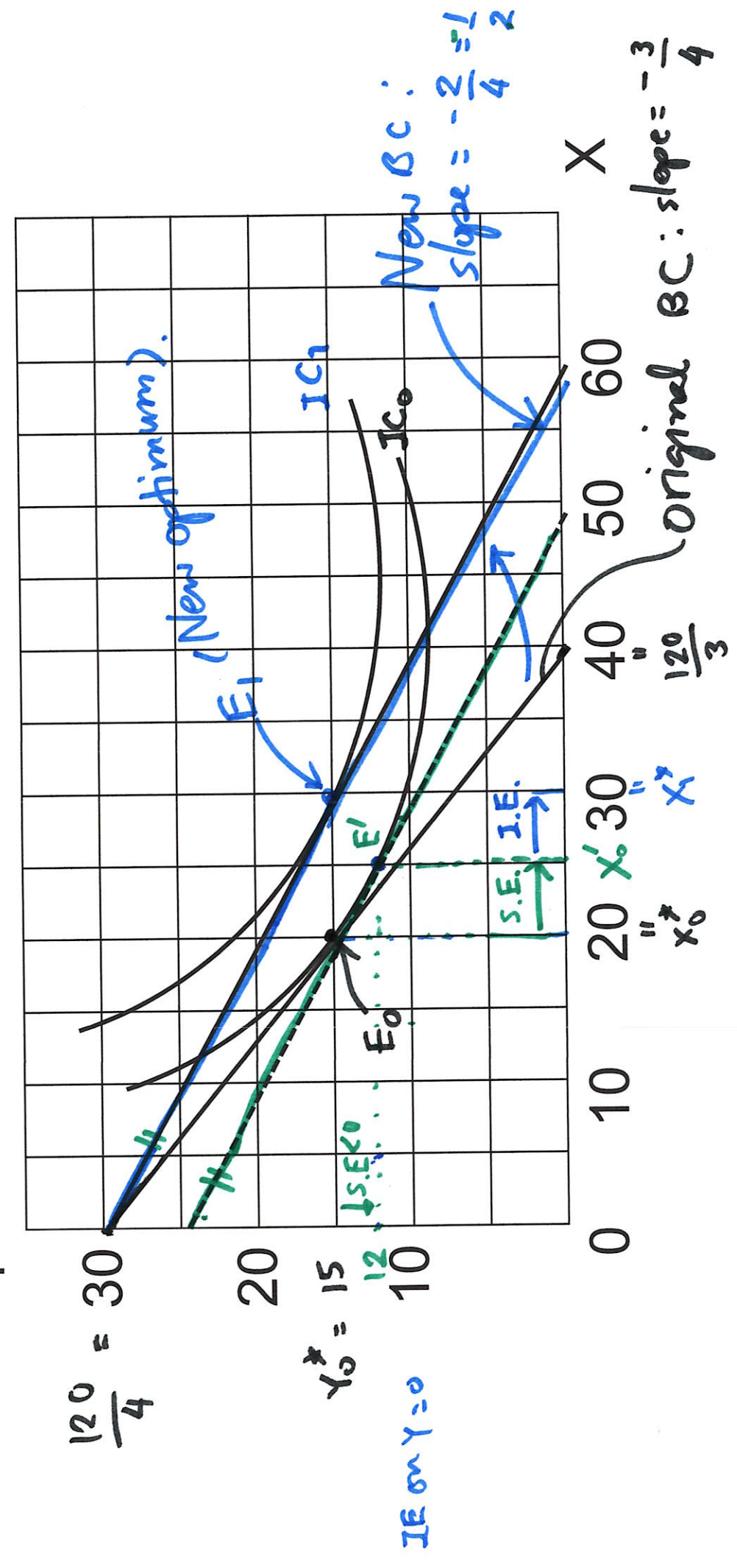


Substitution Effect = $X'_0 - X_0 > 0$
 Income effect = $X_1^* - X_0^* > 0$

Graph

Original Bx
 New Px

• Suppose $P_x = \$3$, $P_y = \$2$, $P_x = \$4$, and $B = 120$.



Giffen Good.

Application 1

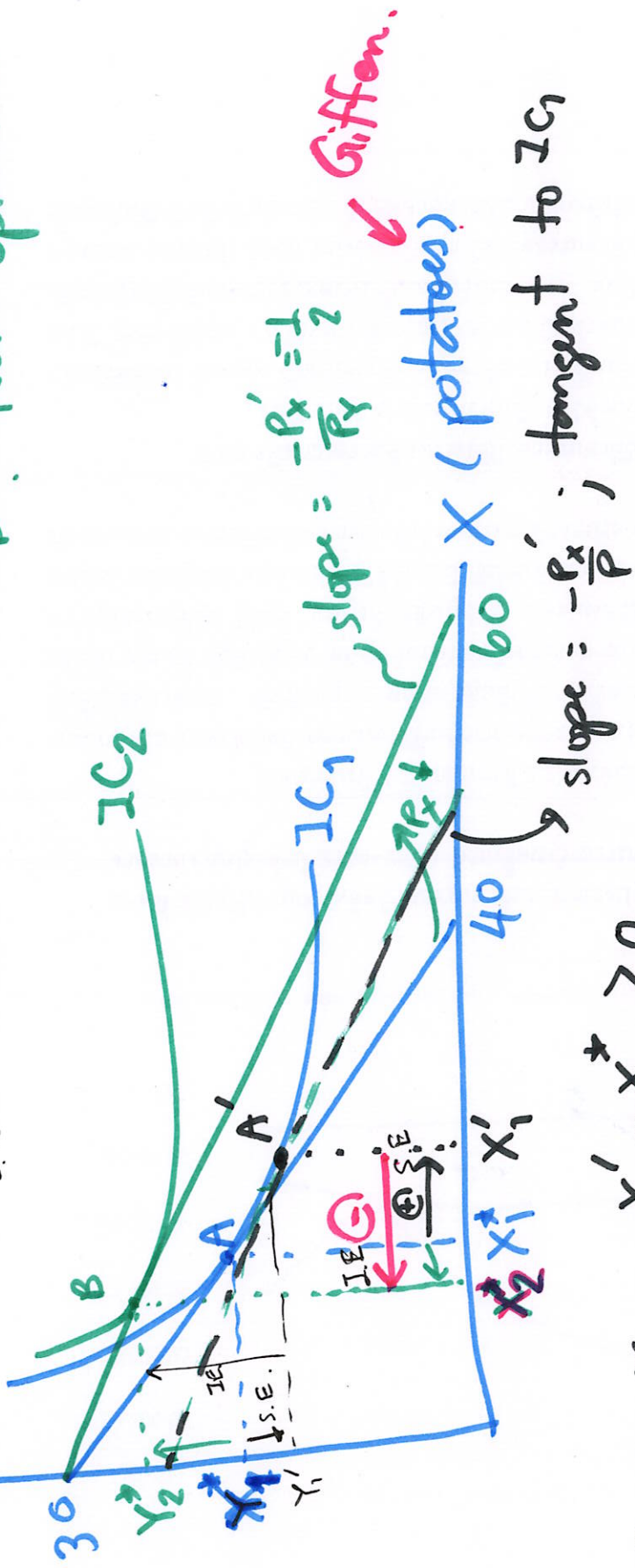
- Giffen goods are goods at which quantity demanded decreases when its price is lower.
 - Giffen good is a special case of inferior good.
- ↳ Possible when income effect is greater than substitution effect.

Assume 2 goods: Potatoes (X) & Meat (Y)

Suppose $P_x = 3$, $P_y = 4$, $B = 120$.
 ↳ $P'_x = 2$

Y (Meat)

S.E. on Y: $Y_1' - Y_1^* < 0$
 I.E. on Y: $Y_2^* - Y_1' > 0$



Giffen.

A : Original optimum.
 B : New optimum

S.E. on X = $X_1' - X_1^* > 0$

I.E. on X = $X_2^* - X_1' < 0$

Total effect = $X_2^* - X_1^* < 0$

$P_x \downarrow \Rightarrow X^* \downarrow$

b/c $IE < SE$ \oplus

slope = $-\frac{P_x'}{P'}$; tangent to IC_2

slope = $-\frac{P_x}{P} = -\frac{1}{2}$