Assignment 1
Assigned on Apr 9th, 2022. Due date Saturday, May 7th, 2022 before midnight.

Instructions

(1) Please read the instruction carefully.
(2) Please read each question carefully and answer the questions straightforwardly. Always provide economic reasons at lease a paragraph for your analysis, or a graph when necessary, even when the question does not indicate so.
(3) Handing and submitting assignments are only available via BE Moodle.

Answering the questions and preparing answer sheets

(1) Answers are to be handwritten, in either digital or analog form, in a blank canvas or any clean paper. Make sure that your handwriting is clearly visible and readable.
(2) There is no need to rewrite the question. Just indicate the question number clearly for each of the answer, such as 1.a).
(3) Default decimal point is 4.
(4) Choose precise wordings, especially when you want to interpret the meaning of a test, confidence interval, or coefficients.
(5) When done, for the digital case, collage all the pages into a single PDF file. For those who write on sheets of paper, take photo of all pages then convert all of them into a single PDF file as well.
(6) Name your PDF file as StudentID_YourNickname, such as 640123456_Bo.

Submitting your answers

(1) Make sure your file does not exceed 10MB. This is the maximum file size for BE Moodle upload.
(2) Login to BE Moodle, head into the course, then the assignment topic.
(3) Choose your file to submit. Done. There will be timestamp for your upload date and time, so please make sure to not submit later than that.

Question 1. (12 points) Economic model of Crime.

1.a) Based on the regression results provided, write out the estimated coefficients in the form of regression equation (1.1). Interpret the estimated coefficients associated with *avgsen*. Based on Model (1.1), test whether the average sentence served from prior convictions has an impact on the number of arrests in the current year (1986). Show your work. (Use α = 0.05) Interpret a-ñ test individual β_2

1.b) What is the overall significance of the regression from Model (1.1) and Model (1.2)? What test do you use? (Use α = 0.01)

1.c) If we are interested in testing whether "ethnic background and legal income" has an impact on the number of arrests in the current year (1986), what kind of null/alternative hypothesis would we be testing? Perform the test and discuss your finding. (Use α = 0.05)

Estimate the model (1.1) reports in the Table 1.1

$$narr86_i = \beta_1 + \beta_2 pcnv_i + \beta_3 avgsen_i + \beta_4 tottime_i + \beta_5 ptime86_i + \beta_6 qemp86_i + u_i \qquad \textbf{(1.1)}$$

Table 1.1

Source	SS	df	MS	Number of obs	=	2,725
				F(5, 2719)	=	24.29
Model	85.9532425	5	17.1906485	Prob > F	=	0.0000
Residual	1924.39391	2,719	.707757967	R-squared	=	0.0428
				Adj R-squared	=	0.0410
Total	2010.34716	2,724	.738012906	Root MSE	=	.84128

narr86	Coefficient	Std. err.	t	P>|t|	[95% conf.	interval]
pcnv	-.1512246	.040855	Omitted for the purpose of this exam			
avgsen	-.0070487	.0124122				
tottime	.0120953	.0095768				
ptime86	-.0392585	.0089166				
qemp86	-.1030909	.0103972				
_cons	.7060607	.0331524				

1.a narr 86 = .7060607 - .1512246 pcnv - .0070487 avgsen + .0120953 tottime
- .0392585 ptime 86 - .1030909 qemp 86

the number of arrests in the current year (1986) decrease 1 time when the average sentence served from prior convictions increase .0070487 month.

$H_0: \beta_3 = 0$

$H_1: \beta_3 \neq 0$

$$t\text{-cal} = \frac{-.0070487 - 0}{.0124122} = -0.5679$$

∴ t-cal fall in fail to reject H_0, the average sentence served from prior convictions is not significant inpact to the number of arrests in the current year (1986) at $\alpha = 0.05$

1.b Model 1.1

$H_0: \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = 0$

H_1 : otherwise

$$F = \frac{R^2/k-1}{(1-R^2)/n-k} = \frac{.0428/5}{(1-.0428)/2719} = 24.3153$$

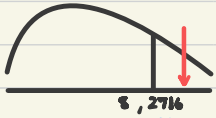
Fcal > Fcri reject H_0, at least one β is not equal to 0 at 99% confidence. level.

Model 1.2

$H_0: \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = \beta_7 = \beta_8 = \beta_9 = 0$

H_1 : otherwise

$$F = \frac{R^2/k-1}{(1-R^2)/n-k} = \frac{.0723/8}{(1-.0723)/2716} = 26.4588$$



Fcal > Fcri reject H_0, at least one β is not equal to 0 at 99% confidence. level.

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Estimate the model (1.2) reports in the Table 1.2

$$narr86_i = \beta_1 + \beta_2 pcnv_i + \beta_3 avgsen_i + \beta_4 tottime_i + \beta_5 ptime86_i + \beta_6 qemp86_i + \beta_4 inc86_i + \beta_5 black_i + \beta_6 hispan_i + u_i \quad \textbf{(1.2)}$$

where

$narr86_i$	= the number of arrests in the current year (1986)
$pcnv_i$	= the proportion of prior arrests that led to a conviction
$avgsen_i$	= the average sentence served from prior convictions (in months)
$tottime_i$	= months spent in prison since age 18 prior to 1986
$ptime86_i$	= months spent in prison in 1986
$qemp86_i$	= the number of quarters that the man was legally employed in 1986
$inc86_i$	= legal income, 1986, (hundred dollars)
$black_i$	= 1 if black ethnic background
$hispan_i$	= 1 if Hispanic ethnic background

Table 1.2

Source	SS	df	MS		
Model	145.390104	8	18.173763	Number of obs	= 2,725
Residual	1864.95705	2,716	.686655763	F(8, 2716)	= 26.47
				Prob > F	= 0.0000
				R-squared	= 0.0723
				Adj R-squared	= 0.0696
Total	2010.34716	2,724	.738012906	Root MSE	= .82865

narr86	Coefficient	Std. err.	t	P>|t|	[95% conf. interval]
pcnv	-.1332344	.0403502			
avgsen	-.0113177	.0122401			
tottime	.0120224	.0094352			
ptime86	-.0408417	.008812			
qemp86	-.0505398	.0144397			
inc86	-.0014887	.0003406			
black	.3265035	.0454156			
hispan	.1939144	.0397113			
_cons	.5686855	.0360461			

Omitted for the purpose of this exam

1.C Individual test

$H_0 : \beta_7 = 0$

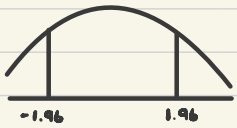
$H_1 : \beta_7 \neq 0$ (significant)

$$t\text{-cal} = \frac{-.0014887 - 0}{.0003406} = -4.3708$$

$H_0 : \beta_8 = 0$

$H_1 : \beta_8 \neq 0$

$$t\text{-cal} = \frac{.3265035 - 0}{.04541156} = 7.1892$$



$H_0 : \beta_9 = 0$

$H_1 : \beta_9 \neq 0$

$$t\text{-cal} = \frac{.1939144 - 0}{.0397113} = 4.8831$$

∴ t-cal fall in reject H_0, legal income (1986), black ethnic background, and Hispanic ethnic background have significant impact on the number of arrests in 1986.

Question 2. (12 points) Dummy variables and interaction terms.

Using the Thailand labor force survey (LFS) in quarter 2 of 2019 and 2020, employees log of wage is modeled as follows. (Number of observations is 97,878 in total)

$$\ln wage_i = \beta_1 + \beta_2 civil_i + \beta_3 year_i + \beta_4 civil_i \cdot year_i + u_i$$

where $\ln wage_i$ = natural logarithmic scale of monthly wage

$civil_i$ = 1; civil servant and state employee

= 0; otherwise

$year_i$ = 1; year 2020

= 0; otherwise (2019)

This model is also known as Difference-in-Differences (DiD) and its intention is to capture the effect of COVID-19 since March of 2020 on different types of employment. During the pandemic, we assume that civil servant and state employee's wage is not reduced (control group) while others', namely employees in private firms or freelance, etc., is suspected to be reduced (treatment group). The estimation result is shown below with standard errors in parentheses. Answer the following questions.

$$\widehat{\ln wage_i} = 9.1748 + 0.587\ civil_i - 0.0336\ year_i + 0.0444\ civil_i \cdot year_i + u_i$$
$$(0.0035)\quad (0.0072)\quad (0.005)\quad (0.0102)$$

2.a) Test all the parameters individually if each of them is significantly different from zero of not.

2.b) How much on average does a civil servant and state employee earns more or less than the others disregarding the year?

2.c) How much on average does the pandemic affect wage overall?

$\alpha_1 = 0$, $\alpha_2 = 0$ $\alpha_1 \alpha_2 = 1$

2.d) Are the control group and the treatment group better-off or worse-off during the pandemic. Discuss each group separately, show your work and explain with economic reasons according to the intention of this model.

2.a Individual test

$H_0: \beta_1 = 0$ $\quad$ $t\text{-cal} = \frac{9.1748 - 0}{.0035} = 2621.3714$

$H_1: \beta_1 \neq 0$

$H_0: \beta_2 = 0$ $\quad$ $t\text{-cal} = \frac{0.587 - 0}{.0072} = 81.5278$

$H_1: \beta_2 \neq 0$

$H_0: \beta_3 = 0$ $\quad$ $t\text{-cal} = \frac{-.0336 - 0}{.005} = -6.72$

$H_1: \beta_3 \neq 0$

$H_0: \beta_4 = 0$ $\quad$ $t\text{-cal} = \frac{.0444 - 0}{.0102} = 4.3529$

$H_1: \beta_4 \neq 0$

∴ t cal fall in reject H_0, all parameters are significantly different from 0 at 0.05

2.b

in parentheses. Answer the following questions.

$$\widehat{\ln wage_i} = 9.1748 + 0.587\ civil_i - 0.0336\ year_i + 0.0444\ civil_i \cdot year_i + u_i$$
$$(0.0035)\quad (0.0072)\qquad (0.005)\qquad (0.0102)$$

civil = 1

year = 1 (2020)

= 0 (2019)

2020

$\widehat{\ln wage} = 9.1748 + .587 - .0336 + .0444$

$= 9.7726$

$\widehat{wage} = e^{9.7726}$

$= 17,546.2784$ Baht

2019

$\widehat{\ln wage} = 9.1748 + .587 - .0336(0) + .0444(1)(0)$

$= 9.7618$

$= 17357.8477$ Baht

∴ the average wage of civil servant and state employee in 2020 is higher than 2019 by 188.4302 Baht

2.c not civil servant & state employee in 2020

civil = 0 $\ln \widehat{wage} = 9.1748 - .0036$

year = 1 $= 9.1412$

$\widehat{wage} = e^{9.1412}$

$= 9,331.9568$ Baht

not civil servant and state employee in 2019

civil = 0 $\ln \widehat{wage} = 9.1748$

year = 0 $\widehat{wage} = e^{9.1748}$

$= 9,650.8377$ Baht

∴ the average wage of others fell from 2019 to 2020 by 318.8809 Baht

2.d According to 2.C, the pandemic affect normal citizens who are not civil servant and state employee from the average wage in 2020 is lower than 2019 by 318.8809 ฿. Because the pandemic cause to close in Business, it make people will not receive any welfare from firm and fire. In another case, the average wage of civil servant & state employee in 2020 increase from 2019. As this group may receive any welfare from government.

Question 3. (8 points) Multicollinearity.

As cheese ages, several chemical processes take place that determine the taste of the final product. The data given pertain to concentrations of various chemicals in a sample of 30 mature cheddar cheeses and subjective measure of taste for each sample.

Estimate the model (3.1) reports in the Table 3.1

$$Taste = \beta_0 + \beta_1 acetic + \beta_2 h2s + \beta_3 lactic + u \qquad \textbf{(3.1)}$$

Where $Taste$ = Measures of taste for each sample

$acetic$ = The natural logarithm of concentration of acetic

$h2s$ = The natural logarithm of concentration of hydrogen sulfide

$lactic$ = Lactic

Table 3.1

Source	SS	df	MS			
Model	5020.64468	3	1673.54823	Number of obs	=	30
Residual	2642.24237	26	101.624706	F(3, 26)	=	16.47
Total	7662.88705	29	264.237485	Prob > F	=	0.0000
				R-squared	=	0.6552 high
				Adj R-squared	=	0.6154
				Root MSE	=	10.081

taste	Coefficient	Std. err.	t	P>|t|	[95% conf.	interval]
acetic	1.538645	3.000501				
h2s	3.915242	1.153106				
lactic	18.80235	8.342614				
_cons	-34.13491	15.67628				

Omitted for the purpose of this exam

table r

	acetic	h2s	lactic
acetic	1.0000		
r_{23} h2s	0.2700	1.0000	
r_{24} lactic	0.3607	0.6448	1.0000

r_{34}

Variable	VIF	1/VIF
lactic	1.83	0.546648
h2s	1.72	0.582609
acetic	1.15	0.867477
Mean VIF	1.57	

taste = - 34.1349 + 1.5386 acetic + 3.9152 h2S + 18.8024 lactic

3.a $H_0 : \beta_2 = 0$ $\quad$ $t\text{-cal} = \frac{1.5386 - 0}{3.0005}$

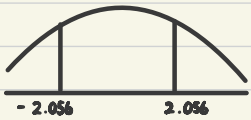
$H_1 : \beta_2 \neq 0$

$= .5128$

$H_0 : \beta_3 = 0$ $\quad$ $t\text{-cal} = \frac{3.9152 - 0}{1.1531}$

$H_1 : \beta_3 \neq 0$

$= 3.3954$



$H_0 : \beta_4 = 0$ $\quad$ $t\text{-cal} = \frac{18.8024 - 0}{8.3426}$

$H_1 : \beta_4 \neq 0$

$= 2.2538$

∴ Both β_3 and β_4 are significant from reject Ho. However, β_2 is not significant.

From table r, r_{23} and r_{24} are low while r_{34} is moderate.

low VIF and high TOL

$TOL = \frac{1}{VIF} = 0.6369$ (high)

3.b The OLS estimators are unbiased. But unbiasedness is a multisample or repeated sampling property. Colinearity does not destroy the property of minimum variance. All linear unbiased estimators, the OLS estimators have minimum variance - they are efficient. But this does not mean the variance of an OLS estimator will necessarily be small. As a result, it is still be BLUE.

3.a) Is there evidence of multicollinearity in the data? How do you know? Explain your answers in detail and state the critical value for hypothesis testing to receive full points.

3.b) What is the property of BLUE? If there is the multicollinearity problem, is the OLS estimators still retain the property of BLUE? If not, which properties are violated?

Question 4. (8 points) Heteroscedasticity.

The data on U.S. inflation rates (%) and unemployment rates (%), 1948-2006

Estimate the model (4.1) reports in the Table 4.1

$$Inf_t = \beta_1 + \beta_2 unem_t + u_t \qquad \textbf{(4.1)}$$

where Inf_t = inflation rates (%)

$unem_t$ = unemployment rates (%)

Table 4.1

Source	SS	df	MS	Number of obs	=	59
				F(1, 57)	=	3.85
Model	32.3284496	1	32.3284496	Prob > F	=	0.0545
Residual	478.096987	57	8.38766644	R-squared	=	0.0633
				Adj R-squared	=	0.0469
Total	510.425437	58	8.80043856	Root MSE	=	2.8961

inf	Coefficient	Std. err.	t	P>|t|	[95% conf. interval]
unem	.5054734	.2574699	Omitted for the purpose of this exam		
_cons	1.010847	1.491583			

White's general test statistic: 1.0266 Chi-sq (2)

Breusch-Pagan / Cook-Weisberg test for heteroskedasticity

chi2(1) = 1.12 LM

Answer the following questions.

4.a) Interpret the intercept and slope coefficients.

4.b) According to the test statistics given after Table 4.1 below, is there any sufficient evidence to conclude that there is heteroscedasticity problem? Show your work on the hypothesis testing. (Use $\alpha = 0.05$)

4.c) Given your test results in a), do the OLS estimators still retain the property of BLUE? If not, which properties are violated?

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4.a β_1 : When the unemployment equal to 0 %, the inflation equal to 1.010847 %.

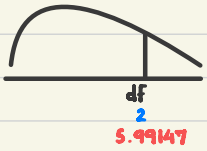
β_2 : If the unemployment rates increase 1%, Inflation rates will increase .50547341 %.

4.b H_0 : Homoscedastic

H_1 : Heteroscedasticity

White test

$\hat{u} = \alpha_1 + \alpha_2 \text{ unem} + \alpha_3 \text{ unem}^2$



$LM = n \cdot R^2 = 1.0266$

$LM_{cal} < \chi^2$

it fall in fail to reject H_0, so it is homoscedasticity.

Breusch - Pagon

$LM = n \cdot R^2_{k-1} = 1.12$

4c since we cannot reject the null hypothesis in 4b, therefore, we can make sure that BLUE property is not violated.