

HW#2 Due Jan 20, 2022

HW Given $y = 10 + \sqrt{x}$,

- a) Find the derivative $f'(x)$.
 b) Fill in the table

| Point | X | Y | $f'(x)$ |
|-------|---|--------|---------|
| | 0 | 10 | - |
| A | 1 | 11 | 1 |
| B | 2 | 11.414 | 0.407 |
| C | 3 | 11.732 | 0.577 |

- c) Does the slope increase as x increases?
 d) Approximate the change in Y when $\Delta x = 0.2$ at $x_1 = 3$. Is the approximation under- or over-estimate?

a) $\text{slope} = \frac{dy}{dx} = f'(x) = \frac{1}{\sqrt{x}}$

c) No, the slope decrease as x increase, slope > 0

d) Approximate

$$\begin{aligned} \Delta y &\approx f'(x) \Delta x \\ \Delta y &\approx f'(3)(0.2) \\ \Delta y &\approx 0.1154 \end{aligned}$$

Real

$$\begin{aligned} x_1 &= 3 \\ x_2 &= 3.2, \quad y_1 = 11.732 \end{aligned}$$

$$\begin{aligned} y_2 &= f(3.2) \\ &= 10 + \sqrt{3.2} \\ &= 11.789 \end{aligned}$$

$$\begin{aligned} \Delta y &= y_2 - y_1 \\ &= 0.057 \end{aligned}$$

Ans The approximation is over estimate