Seemingly Unrelated Regression (SUR) Models

```
set obs 400
mat C=(1,0.9\0.9,1)
corr2data u1 u2, n(400) means(0 0) sds(8 9) corr(C)
g x1=rnormal(1,10)
g x2=rnormal(2,20)
g x3=rnormal(-1,10)
g x4=rnormal(3,10)
g y1=1+0.1*x1+0.2*x2+u1
g y2=2+0.1*x3+0.2*x4+u2
```

```
. reg y1 x1 x2
      Source |       SS           df       MS      Number of obs   =       400
-------------+----------------------------------   F(2, 397)       =     49.77
       Model |  6396.30768         2  3198.15384   Prob > F        =    0.0000
    Residual |  25510.4448       397  64.2580474   R-squared       =    0.2005
-------------+----------------------------------   Adj R-squared   =    0.1964
       Total |  31906.7525       399  79.9667982   Root MSE        =    8.0161

------------------------------------------------------------------------------
          y1 |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
          x1 |   .1223002   .0428067     2.86   0.005     .0381441    .2064563
          x2 |   .1940088   .0198093     9.79   0.000     .1550646     .232953
       _cons |   .9955992   .4032669     2.47   0.014     .2027936    1.788405
------------------------------------------------------------------------------

. reg y2 x3 x4
      Source |       SS           df       MS      Number of obs   =       400
-------------+----------------------------------   F(2, 397)       =     11.62
       Model |  1880.45146         2   940.22573   Prob > F        =    0.0000
    Residual |  32120.5595       397  80.9082104   R-squared       =    0.0553
-------------+----------------------------------   Adj R-squared   =    0.0505
       Total |   34001.011       399  85.2155664   Root MSE        =    8.9949

------------------------------------------------------------------------------
          y2 |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
          x3 |   .0331711   .0439497     0.75   0.451    -.0532321    .1195743
          x4 |   .2248807   .0481634     4.67   0.000     .1301936    .3195679
       _cons |   1.907247   .4633147     4.12   0.000     .9963895    2.818104
------------------------------------------------------------------------------

. sureg (y1 x1 x2) (y2 x3 x4)

Seemingly unrelated regression
--------------------------------------------------------------------------
Equation             Obs   Parms        RMSE    "R-sq"       chi2        P
--------------------------------------------------------------------------
y1                   400       2     7.98606    0.2005     514.34   0.0000
y2                   400       2    8.975366    0.0523     122.98   0.0000
--------------------------------------------------------------------------
------------------------------------------------------------------------------
             |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
y1           |
          x1 |   .1239373   .0187545     6.61   0.000     .0871791    .1606955
          x2 |   .1926824   .0086663    22.23   0.000     .1756968    .2096681
       _cons |   .9967315   .3997738     2.49   0.013     .2131893    1.780274
-------------+----------------------------------------------------------------
y2           |
          x3 |   .0811216   .0192349     4.22   0.000     .0434218    .1188213
          x4 |   .2068554   .0210995     9.80   0.000     .1655012    .2482097
       _cons |    1.97418   .4507025     4.38   0.000     1.090819     2.85754
------------------------------------------------------------------------------
```

Example:

Study on trading value of three different groups of investors including individual, institution, and foreign investors. The models are as follows:

$$QLN_t = \beta_{10} + \beta_{11}SET_t + \beta_{12}PE_t + \beta_{13}DY_t + \beta_{14}DUM_t + \varepsilon_{1t}$$
$$QLI_t = \beta_{20} + \beta_{21}SET_t + \beta_{22}PE_t + \beta_{23}DY_t + \beta_{24}DUM_t + \beta_{25}DJ_t + \beta_{26}IB_t + \varepsilon_{2t}$$
$$QF_t = \beta_{30} + \beta_{31}SET_t + \beta_{32}PE_t + \beta_{33}DY_t + \beta_{34}DUM_t + \beta_{35}FX_t + \beta_{36}IB_t + \varepsilon_{3t}$$

The disturbance terms $\varepsilon_{1t}, \varepsilon_{2t}$, and ε_{3t} are assumed to be correlated.

OLS:

```
. reg3 (qln set pe dy dum) (qli set dj ib pe dy dum) (qf set fx ib pe dy dum), o
Multivariate regression
----------------------------------------------------------------------
Equation          Obs  Parms        RMSE    "R-sq"     F-Stat        P
----------------------------------------------------------------------
qln                84      4    5047.675    0.4640      17.10   0.0000
qli                84      6    1826.843    0.2180       3.58   0.0021
qf                 84      6    5802.913    0.4669      11.24   0.0000
----------------------------------------------------------------------
------------------------------------------------------------------------------
             |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
qln          |
         set |  -345.1613   48.03645    -7.19   0.000    -439.8026     -250.52
          pe |  -534.6304    168.594    -3.17   0.002    -866.7938    -202.467
          dy |  -2115.715   539.4979    -3.92   0.000    -3178.632   -1052.797
         dum |  -3718.633   1984.562    -1.87   0.062    -7628.613    191.3469
       _cons |   12337.82   3805.531     3.24   0.001     4840.173    19835.47
-------------+----------------------------------------------------------------
qli          |
         set |  -48.97907    18.3963    -2.66   0.008    -85.22341   -12.73473
          dj |   135.2776   59.33954     2.28   0.024     18.36695    252.1882
          ib |   88.29653   67.38561     1.31   0.191    -44.46645    221.0595
          pe |  -182.7578   83.29688    -2.19   0.029    -346.8691   -18.64644
          dy |  -917.2405    392.641    -2.34   0.020    -1690.821   -143.6602
         dum |  -628.3281   860.6836    -0.73   0.466    -2324.045    1067.389
       _cons |   3089.883   1839.067     1.68   0.094    -533.4418    6713.207
-------------+----------------------------------------------------------------
qf           |
         set |   376.5217   55.84303     6.74   0.000     266.4999    486.5436
          fx |    102.815   218.4466     0.47   0.638    -327.5679    533.1979
          ib |  -98.88969   210.3643    -0.47   0.639    -513.3488    315.5695
          pe |   751.3749   273.1862     2.75   0.006     213.1441    1289.606
          dy |   3042.807   1235.314     2.46   0.014     608.9934     5476.62
         dum |   3324.652   3827.915     0.87   0.386    -4217.098     10866.4
       _cons |  -18891.85   8782.692    -2.15   0.033    -36195.49   -1588.212
------------------------------------------------------------------------------
```

SUR:

```
. reg3 (qln set pe dy dum) (qli set dj ib pe dy dum) (qf set fx ib pe dy dum), sur
Seemingly unrelated regression
----------------------------------------------------------------------
Equation          Obs  Parms        RMSE    "R-sq"       chi2        P
----------------------------------------------------------------------
qln                84      4    4895.142    0.4640      72.72   0.0000
qli                84      6     1797.71    0.1739      18.59   0.0049
qf                 84      6    5563.745    0.4653      76.49   0.0000
----------------------------------------------------------------------
------------------------------------------------------------------------------
             |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
```

```
qln          |
         set |  -345.1613   46.58486    -7.41   0.000    -436.4659   -253.8566
          pe |  -534.6304   163.4993    -3.27   0.001    -855.0831   -214.1776
          dy |  -2115.715   523.1951    -4.04   0.000    -3141.158   -1090.271
         dum |  -3718.633   1924.592    -1.93   0.053    -7490.764    53.49775
       _cons |   12337.82   3690.534     3.34   0.001     5104.508    19571.13
-------------+----------------------------------------------------------------
qli          |
         set |   -36.4466   16.72057    -2.18   0.029    -69.21832   -3.674872
          dj |   11.63355   15.65562     0.74   0.457    -19.05089      42.318
          ib |   115.9576   61.82175     1.88   0.061    -5.210785     237.126
          pe |  -199.5312   78.51039    -2.54   0.011    -353.4088    -45.6537
          dy |  -1040.228    365.219    -2.85   0.004    -1756.044   -324.4121
         dum |  -1001.492   802.6055    -1.25   0.212     -2574.57    571.5858
       _cons |    3753.84   1719.156     2.18   0.029     384.3559    7123.324
-------------+----------------------------------------------------------------
qf           |
         set |    380.311   52.87754     7.19   0.000      276.673    483.9491
          fx |   3.099417   18.89913     0.16   0.870     -33.9422    40.14104
          ib |  -118.3508   64.30475    -1.84   0.066    -244.3858    7.684168
          pe |   736.5373   193.5326     3.81   0.000     357.2204    1115.854
          dy |   3165.703   677.6422     4.67   0.000     1837.549    4493.857
         dum |   4714.671   2238.532     2.11   0.035     327.2284    9102.113
       _cons |  -16243.51   4380.287    -3.71   0.000    -24828.71   -7658.301
------------------------------------------------------------------------------
```

<u>Alternative Command for SUR:</u>

```
. sureg (qln set pe dy dum) (qli set dj ib pe dy dum) (qf set fx ib pe dy dum)

Seemingly unrelated regression
----------------------------------------------------------------------
Equation          Obs  Parms        RMSE    "R-sq"       chi2        P
----------------------------------------------------------------------
qln                84      4    4895.142    0.4640      72.72   0.0000
qli                84      6     1797.71    0.1739      18.59   0.0049
qf                 84      6    5563.745    0.4653      76.49   0.0000
----------------------------------------------------------------------

------------------------------------------------------------------------------
             |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
qln          |
         set |  -345.1613   46.58486    -7.41   0.000    -436.4659   -253.8566
          pe |  -534.6304   163.4993    -3.27   0.001    -855.0831   -214.1776
          dy |  -2115.715   523.1951    -4.04   0.000    -3141.158   -1090.271
         dum |  -3718.633   1924.592    -1.93   0.053    -7490.764    53.49775
       _cons |   12337.82   3690.534     3.34   0.001     5104.508    19571.13
-------------+----------------------------------------------------------------
qli          |
         set |   -36.4466   16.72057    -2.18   0.029    -69.21832   -3.674872
          dj |   11.63355   15.65562     0.74   0.457    -19.05089      42.318
          ib |   115.9576   61.82175     1.88   0.061    -5.210785     237.126
          pe |  -199.5312   78.51039    -2.54   0.011    -353.4088    -45.6537
          dy |  -1040.228    365.219    -2.85   0.004    -1756.044   -324.4121
         dum |  -1001.492   802.6055    -1.25   0.212     -2574.57    571.5858
       _cons |    3753.84   1719.156     2.18   0.029     384.3559    7123.324
-------------+----------------------------------------------------------------
qf           |
         set |    380.311   52.87754     7.19   0.000      276.673    483.9491
          fx |   3.099417   18.89913     0.16   0.870     -33.9422    40.14104
          ib |  -118.3508   64.30475    -1.84   0.066    -244.3858    7.684168
          pe |   736.5373   193.5326     3.81   0.000     357.2204    1115.854
          dy |   3165.703   677.6422     4.67   0.000     1837.549    4493.857
         dum |   4714.671   2238.532     2.11   0.035     327.2284    9102.113
       _cons |  -16243.51   4380.287    -3.71   0.000    -24828.71   -7658.301
------------------------------------------------------------------------------
```

Simultaneous-Equation Models

Example: Klien's Model I

System equations model that frequently used is simultaneous equations model. A well know macroeconometrics model is Klien's (1950) Model I, which has the following equations form:

$$C_t = \alpha_0 + \alpha_1 P_t + \alpha_2 P_{t-1} + \alpha_3 \left(W_t^P + W_t^G\right) + \varepsilon_{1t} \quad \text{(Consumption)},$$

$$I_t = \beta_0 + \beta_1 P_t + \beta_2 P_{t-1} + \beta_3 K_{t-1} + \varepsilon_{2t} \quad \text{(Investment)},$$

$$W_t^P = \gamma_0 + \gamma_1 X_t + \gamma_2 X_{t-1} + \gamma_3 A_t + \varepsilon_{3t} \quad \text{(Private wages)},$$

$$X_t = C_t + I_t + G_t \quad \text{(equilibrium demand)},$$

$$P_t = X_t - T_t - W_t^P \quad \text{(private profits)},$$

$$K_t = K_{t-1} + I_t \quad \text{(capital stock)},$$

where C_t = Consumption at time *t*
I_t = Investment at time *t*
W_t^P = Private wages at time *t*
X_t = Total demand at time *t*
P_t = Private profits at time *t*
K_t = Capital stock at time *t*
G_t = Government nonwage spending at time *t*
T_t = Indirect business taxes plus net exports at time *t*
W_t^G = Government wage bill at time *t*
A_t = Time trend measured as years from 1931

Endogenous variables are all variables on the left hand side including consumption (C_t), investment (I_t), and private wages (W_t^P). Exogenous variables include government nonwage spending (G_t), indirect business taxes plus net exports (T_t), government wage will (W_t^G), and time trend (A_t). However, there are also predetermined variables including total demand (X_t), private profit (P_t), and capital stock from last year (K_{t-1}). This system model consists of 3 behavior equation and 1 equilibrium condition, and 2 identities. This simultaneous model is a dynamic model for a small economy. Klein (1950) estimated this model using data from 1921 to 1941.

The model is estimated using the data from 1921 to 1941. Methods of estimation include Ordinary Least Squares (OLS), Two Stages Least Squares: 2SLS, (Three stage Least squares: 3SLS, and Iterative Three Stages Least Squares: I3SLS.

```
. tsset year
        time variable:  year, 1920 to 1941
                delta:  1 unit

. g w = wg+wp
. g k = k1+i
. g yr=year-1931
. g p1 = l.p1
. g x1 = l.x

. reg c p p1 w
      Source |       SS       df       MS              Number of obs =      21
-------------+------------------------------           F(  3,    17) =  292.71
       Model |  923.549937     3  307.849979           Prob > F      =  0.0000
    Residual |  17.8794524    17  1.05173249           R-squared     =  0.9810
-------------+------------------------------           Adj R-squared =  0.9777
       Total |  941.429389    20  47.0714695           Root MSE      =  1.0255
------------------------------------------------------------------------------
           c |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
           p |   .1929343   .0912102     2.12   0.049     .0004977     .385371
          p1 |   .0898847   .0906479     0.99   0.335    -.1013658    .2811351
           w |   .7962188   .0399439    19.93   0.000     .7119444    .8804931
       _cons |    16.2366   1.302698    12.46   0.000     13.48815    18.98506
------------------------------------------------------------------------------

. reg3 (c p p1 w), 2sls inst(t wg g yr p1 x1 k1)
Two-stage least-squares regression
----------------------------------------------------------------------
Equation             Obs   Parms        RMSE    "R-sq"     F-Stat        P
----------------------------------------------------------------------
c                     21       3    1.135659    0.9767     225.93   0.0000
----------------------------------------------------------------------

------------------------------------------------------------------------------
           c |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
c            |
           p |   .0173022   .1312046     0.13   0.897    -.2595153    .2941197
          p1 |   .2162338   .1192217     1.81   0.087    -.0353019    .4677696
           w |   .8101827   .0447351    18.11   0.000        .7158    .9045654
       _cons |   16.55476   1.467979    11.28   0.000     13.45759    19.65192
------------------------------------------------------------------------------
Endogenous variables:  c p w
Exogenous variables:   t wg g yr p1 x1 k1
------------------------------------------------------------------------------

. reg p t wg g yr p1 x1 k1
      Source |       SS       df       MS              Number of obs =      21
-------------+------------------------------           F(  7,    13) =    8.82
       Model |  294.248018     7  42.0354311           Prob > F      =  0.0004
    Residual |  61.9500944    13  4.76539188           R-squared     =  0.8261
-------------+------------------------------           Adj R-squared =  0.7324
       Total |  356.198112    20  17.8099056           Root MSE      =   2.183

------------------------------------------------------------------------------
           p |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
           t |  -.9230977   .4337595    -2.13   0.053    -1.860178    .0139827
          wg |  -.0796076   2.533823    -0.03   0.975      -5.5536    5.394385
           g |   .4390162   .3911427     1.12   0.282    -.4059962    1.284029
          yr |   .3194049   .7781286     0.41   0.688     -1.36164    2.000449
          p1 |   .8025008   .5188558     1.55   0.146     -.318419    1.923421
          x1 |   .0220002   .2821641     0.08   0.939    -.5875783    .6315787
          k1 |  -.2161035   .1191134    -1.81   0.093    -.4734323    .0412253
       _cons |   50.38438   31.63026     1.59   0.135    -17.94863    118.7174
------------------------------------------------------------------------------
```

```
. predict phat
(option xb assumed; fitted values)
(1 missing value generated)

. reg w t wg g yr p1 x1 k1
      Source |       SS       df       MS              Number of obs =      21
-------------+------------------------------           F(  7,    13) =   51.15
       Model |  1101.80519     7  157.400741           Prob > F      =  0.0000
    Residual |  40.0071584    13  3.07747372           R-squared     =  0.9650
-------------+------------------------------           Adj R-squared =  0.9461
       Total |  1141.81235    20  57.0906174           Root MSE      =  1.7543

------------------------------------------------------------------------------
           w |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
           t |  -.6041532   .3485755    -1.73   0.107    -1.357205    .1488984
          wg |   .5562761   2.036218     0.27   0.789    -3.842705    4.955257
           g |   .8662196    .314328     2.76   0.016     .1871552    1.545284
          yr |   .7135829   .6253155     1.14   0.274    -.6373292    2.064495
          p1 |   .8719211   .4169601     2.09   0.057    -.0288665    1.772709
          x1 |   .0953288   .2267512     0.42   0.681    -.3945374    .5851951
          k1 |  -.1229518   .0957213    -1.28   0.221     -.329745    .0838415
       _cons |   43.43552   25.41854     1.71   0.111    -11.47789    98.34894
------------------------------------------------------------------------------

. predict what
(option xb assumed; fitted values)
(1 missing value generated)

. reg c phat p1 what

      Source |       SS       df       MS              Number of obs =      21
-------------+------------------------------           F(  3,    17) =   73.65
       Model |  874.172577     3  291.390859           Prob > F      =  0.0000
    Residual |  67.2568126    17  3.95628309           R-squared     =  0.9286
-------------+------------------------------           Adj R-squared =  0.9160
       Total |  941.429389    20  47.0714695           Root MSE      =   1.989

------------------------------------------------------------------------------
           c |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
        phat |   .0173023   .2297973     0.08   0.941    -.4675275    .5021322
          p1 |   .2162337   .2088099     1.04   0.315    -.2243166    .6567841
        what |   .8101827   .0783509    10.34   0.000     .6448768    .9754886
       _cons |   16.55476    2.57108     6.44   0.000     11.13025    21.97926
------------------------------------------------------------------------------
```

All equations can be estimated in one single command in `reg3` as follows:

OLS:

```
reg3 (c p p1 w) (i p p1 k1) (wp x x1 yr), ols
Multivariate regression
----------------------------------------------------------------------
Equation          Obs  Parms        RMSE    "R-sq"     F-Stat        P
----------------------------------------------------------------------
c                  21      3     1.02554    0.9810   292.7075   0.0000
i                  21      3    1.009447    0.9313   76.87538   0.0000
wp                 21      3    .7671466    0.9874   444.5687   0.0000
----------------------------------------------------------------------

------------------------------------------------------------------------------
             |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
c            |
           p |   .1929343   .0912102     2.12   0.039     .0098223    .3760464
          p1 |   .0898847   .0906479     0.99   0.326    -.0920987     .271868
           w |   .7962188   .0399439    19.93   0.000      .716028    .8764095
       _cons |    16.2366   1.302698    12.46   0.000     13.62133    18.85188
-------------+----------------------------------------------------------------
i            |
           p |   .4796356   .0971146     4.94   0.000       .28467    .6746012
          p1 |   .3330387   .1008592     3.30   0.002     .1305554     .535522
          k1 |  -.1117947   .0267276    -4.18   0.000    -.1654525   -.0581369
       _cons |   10.12579   5.465546     1.85   0.070    -.8467492    21.09833
-------------+----------------------------------------------------------------
wp           |
           x |   .4394769   .0324076    13.56   0.000      .374416    .5045378
          x1 |     .14609   .0374231     3.90   0.000       .07096      .22122
          yr |   .1302452   .0319103     4.08   0.000     .0661826    .1943077
       _cons |   1.497043   1.270031     1.18   0.244    -1.052651    4.046737
------------------------------------------------------------------------------
```

2SLS:

```
reg3 (c p p1 w) (i p p1 k1) (wp x x1 yr), 2sls nodfk inst(t wg g yr p1 x1 k1)

Two-stage least-squares regression
----------------------------------------------------------------------
Equation          Obs  Parms        RMSE    "R-sq"     F-Stat        P
----------------------------------------------------------------------
c                  21      3    1.135659    0.9767   279.0941   0.0000
i                  21      3    1.307149    0.8849   50.89437   0.0000
wp                 21      3    .7671548    0.9874    524.005   0.0000
----------------------------------------------------------------------

------------------------------------------------------------------------------
             |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
c            |
           p |   .0173022   .1180494     0.15   0.884    -.2196919    .2542963
          p1 |   .2162338    .107268     2.02   0.049     .0008844    .4315833
           w |   .8101827   .0402497    20.13   0.000      .729378    .8909874
       _cons |   16.55476   1.320793    12.53   0.000     13.90316    19.20636
-------------+----------------------------------------------------------------
i            |
           p |   .1502219   .1732292     0.87   0.390    -.1975503    .4979941
          p1 |   .6159434   .1627853     3.78   0.000     .2891382    .9427486
          k1 |  -.1577876   .0361262    -4.37   0.000    -.2303141   -.0852612
       _cons |   20.27821   7.542704     2.69   0.010     5.135599    35.42082
-------------+----------------------------------------------------------------
wp           |
           x |   .4388591   .0356319    12.32   0.000     .3673251    .5103931
          x1 |   .1466739   .0388361     3.78   0.000     .0687071    .2246406
```

```
         yr |   .1303956    .029141     4.47   0.000     .0718927    .1888985
      _cons |   1.500296   1.147779     1.31   0.197    -.8039674    3.804559
------------------------------------------------------------------------------
Endogenous variables:  c p w i wp x
Exogenous variables:   t wg g yr p1 x1 k1
------------------------------------------------------------------------------
```

<u>3SLS</u>:

```
reg3 (c p p1 w) (i p p1 k1) (wp x x1 yr), 3sls inst(t wg g yr p1 x1 k1)

Three-stage least squares regression
----------------------------------------------------------------------
Equation          Obs  Parms        RMSE    "R-sq"       chi2        P
----------------------------------------------------------------------
c                  21      3    .9443305    0.9801   864.5909   0.0000
i                  21      3    1.446736    0.8258   162.9808   0.0000
wp                 21      3    .7211282    0.9863   1594.751   0.0000
----------------------------------------------------------------------
------------------------------------------------------------------------------
             |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
c            |
           p |   .1248904   .1081291     1.16   0.248    -.0870387    .3368194
          p1 |   .1631439   .1004382     1.62   0.104    -.0337113    .3599992
           w |    .790081   .0379379    20.83   0.000      .715724    .8644379
       _cons |   16.44079   1.304549    12.60   0.000     13.88392    18.99766
-------------+----------------------------------------------------------------
i            |
           p |  -.0130791   .1618962    -0.08   0.936    -.3303898    .3042316
          p1 |   .7557238   .1529331     4.94   0.000     .4559805    1.055467
          k1 |  -.1948482   .0325307    -5.99   0.000    -.2586072   -.1310893
       _cons |   28.17785   6.793768     4.15   0.000     14.86231    41.49339
-------------+----------------------------------------------------------------
wp           |
           x |   .4004919   .0318134    12.59   0.000     .3381388     .462845
          x1 |    .181291   .0341588     5.31   0.000     .1143411    .2482409
          yr |    .149674   .0279352     5.36   0.000      .094922    .2044261
       _cons |   1.797216   1.115854     1.61   0.107    -.3898181    3.984251
------------------------------------------------------------------------------
Endogenous variables:  c p w i wp x
Exogenous variables:   t wg g yr p1 x1 k1
------------------------------------------------------------------------------
```

<u>I3SLS</u>:

```
reg3 (c p p1 w) (i p p1 k1) (wp x x1 yr), 3sls ireg3 inst(t wg g yr p1 x1 k1)
Iteration 1:   tolerance =  .37125491
..
Iteration 24:   tolerance =  7.049e-07

Three-stage least squares regression, iterated
----------------------------------------------------------------------
Equation          Obs  Parms        RMSE    "R-sq"       chi2        P
----------------------------------------------------------------------
c                  21      3    .9565088    0.9796   970.3072   0.0000
i                  21      3    2.134327    0.6209   56.77951   0.0000
wp                 21      3    .7782334    0.9840   1312.188   0.0000
----------------------------------------------------------------------
------------------------------------------------------------------------------
             |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
c            |
           p |   .1645096   .0961979     1.71   0.087    -.0240348    .3530539
          p1 |   .1765639   .0901001     1.96   0.050    -.0000291    .3531569
           w |   .7658011   .0347599    22.03   0.000     .6976729    .8339294
       _cons |   16.55899   1.224401    13.52   0.000     14.15921    18.95877
-------------+----------------------------------------------------------------
```

```
i            |
           p |  -.3565316   .2601568    -1.37   0.171    -.8664296    .1533664
          p1 |   1.011299   .2487745     4.07   0.000     .5237098    1.498888
          k1 |     -.2602   .0508694    -5.12   0.000    -.3599022   -.1604978
       _cons |   42.89629   10.59386     4.05   0.000     22.13271    63.65987
-------------+----------------------------------------------------------------
wp           |
           x |   .3747792   .0311027    12.05   0.000     .3138191    .4357394
          x1 |   .1936506   .0324018     5.98   0.000     .1301443     .257157
          yr |   .1679262   .0289291     5.80   0.000     .1112263    .2246261
       _cons |   2.624766   1.195559     2.20   0.028     .2815124    4.968019
------------------------------------------------------------------------------
Endogenous variables:  c p w i wp x
Exogenous variables:   t wg g yr p1 x1 k1
------------------------------------------------------------------------------
```

<u>Hausman Test</u>:

```
. reg c p w p1

      Source |       SS       df       MS              Number of obs =      21
-------------+------------------------------           F(  3,    17) =  292.71
       Model |  923.549937     3  307.849979           Prob > F      =  0.0000
    Residual |  17.8794524    17  1.05173249           R-squared     =  0.9810
-------------+------------------------------           Adj R-squared =  0.9777
       Total |  941.429389    20  47.0714695           Root MSE      =  1.0255

------------------------------------------------------------------------------
           c |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
           p |   .1929343   .0912102     2.12   0.049     .0004977     .385371
           w |   .7962188   .0399439    19.93   0.000     .7119444    .8804931
          p1 |   .0898847   .0906479     0.99   0.335    -.1013658    .2811351
       _cons |    16.2366   1.302698    12.46   0.000     13.48815    18.98506
------------------------------------------------------------------------------

. estimates store ols

. ivregress 2sls c p1 (p w=t wg g yr p1 x1 k1)
Instrumental variables (2SLS) regression               Number of obs =      21
                                                       Wald chi2(3)  =  837.28
                                                       Prob > chi2   =  0.0000
                                                       R-squared     =  0.9767
                                                       Root MSE      =  1.0218

------------------------------------------------------------------------------
           c |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
           p |   .0173022   .1180494     0.15   0.883    -.2140704    .2486748
           w |   .8101827   .0402497    20.13   0.000     .7312947    .8890707
          p1 |   .2162338    .107268     2.02   0.044     .0059925    .4264752
       _cons |   16.55476   1.320793    12.53   0.000     13.96605    19.14346
------------------------------------------------------------------------------
Instrumented:  p w
Instruments:   p1 t wg g yr x1 k1

. estimates store twostage

. hausman twostage ols

                 ---- Coefficients ----
             |      (b)          (B)            (b-B)     sqrt(diag(V_b-V_B))
             |    twostage       ols         Difference          S.E.
-------------+----------------------------------------------------------------
           p |    .0173022     .1929343       -.1756322        .0749424
           w |    .8101827     .7962188        .0139639         .004952
          p1 |    .2162338     .0898847        .1263492         .057353
------------------------------------------------------------------------------
```

```
      b = consistent under Ho and Ha; obtained from ivregress
      B = inconsistent under Ha, efficient under Ho; obtained from regress

Test:  Ho:  difference in coefficients not systematic

              chi2(3) = (b-B)'[(V_b-V_B)^(-1)](b-B)
                      =        8.81
            Prob>chi2 =      0.0319
            (V_b-V_B is not positive definite)
```