

HW Given  $y = 10 + \sqrt{x}$ ,

- Find the derivative  $f'(x)$ .
- Fill in the table

Point	X	Y	$f'(x)$
	0	10	0
A	1	11	0.5
B	2	11.414	0.35
C	3	11.732	0.29

- Does the slope increase as  $x$  increase?
- Approximate the change in  $Y$  when  $\Delta x = 0.2$  at  $x_1 = 3$ . Is the approximation under- or over-estimate?

$$\begin{aligned} a) \quad y &= 10 + \sqrt{x} \rightarrow x^{\frac{1}{2}} \\ f'(x) &= 0 + \frac{1}{2} x^{-\frac{1}{2}} \\ &= \frac{1}{2\sqrt{x}} \end{aligned}$$

c) No because slope and  $x$  have negative relationship

d) For real  $\Delta Y$

$$\Rightarrow \Delta Y = Y_2 - Y_1$$

$$= (10 + \sqrt{3 \cdot 2}) - (10 + \sqrt{3}) = 0.0568$$

$\therefore 0.0577 > 0.0568$ ,  
which mean the approximation is over-estimate

For approximation

$$\Rightarrow \Delta y = f'(x) \cdot \Delta x$$

$$= \frac{1}{2\sqrt{3}} \cdot 0.2 = 0.0577$$