

Question 1: Montegut Manufacturing produces a product for which the annual demand is 10,000 units. Production averages 100 units per day, while demand is 40 units per day. Holding costs are \$2.00 per unit per year, and setup cost is \$200.00.

- (a) If the firm wishes to produce this product in economic batches, what size batch should be used?
- (b) What is the maximum inventory level?
- (c) How many order cycles are there per year?
- (d) What are the total annual holding and setup costs?

Data:

D = 10,000 units

p = 100 units/day

d = 40 units/day

H = \$2 per unit/per year

S = \$200

- (a) If the firm wishes to produce this product in economic batches, what size batch should be used?

Find EPQ [Economic Production Quantity]

$$EPQ = Q^* = \sqrt{\frac{2DS}{H(1-\frac{d}{p})}} = \sqrt{\frac{(2)(10,000)(200)}{2(1-\frac{40}{100})}} = 1825.7419 \approx 1826 \text{ units}$$

- (b) What is the maximum inventory level?

Maximum Inventory Level:

$$= (\text{total produced during the production run}) - (\text{total used during the production run})$$

$$= (p \cdot t) - (d \cdot t)$$

However, Q = total produced = p • t ; t = $\frac{Q}{p}$

$$= (p \cdot \frac{Q}{p}) - (d \cdot \frac{Q}{p})$$

$$= Q (1 - \frac{d}{p})$$

$$= 1825.7419(1 - \frac{40}{100})$$

$$\approx 1096 \text{ units}$$

- (c) How many order cycles are there per year?

$$\text{Number(\#) of Order Cycles} = \frac{D}{Q} = \frac{10,000}{1825.7419} = 5.4772 \text{ cycles per year}$$

(d) What are the total annual holding and setup costs?

(1) Total annual holding cost = (average inventory level) • (holding cost per unit per year)

$$\begin{aligned} \text{Since, average inventory level} &= \frac{\text{maximum level}}{2} \\ &= \frac{\text{maximum level}}{2} \cdot 2 \\ &= \frac{1095.44519}{2} \cdot 2 \\ &= \$ 1095.45 \end{aligned}$$

$$\begin{aligned} \text{(2) Total annual setup cost} &= \frac{D}{Q} \cdot S \\ &= \frac{10,000}{1825.7419} \cdot (200) \\ &= \$ 1095.45 \end{aligned}$$

Question 2: The annual demand, ordering cost, and the annual inventory carrying cost rate for a certain item are D= 600 units, S= \$20/order and I = 30% of item price. Price is established by the following schedule. What should the order quantity be in order to minimize the total annual cost?

Quantity	1 to 49	50 to 249	250 and up
Price	\$5.00 per unit	\$4.50 per unit	\$4.10 per unit

From question given that D = 600 units

$$S = \$20 \times 0.3 = \$6$$

Price range	Initial price (1 to 49)	Discount price 1 (50 to 249)	Discount price 2 250 and up
Price per unit (P)	\$5	\$4.5	\$4.1
$Q^* = \frac{\sqrt{2DS}}{IP}$	126.49 units	133.33 units	139.69 units
Order quantity	Infeasible	133.33 units	250 units
Annual set up cost $= \frac{D}{Q} S$	-	\$90	\$48
Annual holding cost = $\frac{Q}{2} IP$	-	\$90	\$153.75
Unit cost	-	\$2700	\$2460
Total cost (T)	-	\$2880	\$2661.75

In order to minimize the annual cost, the firm should order 250 units which cost \$4.10 per unit.

Question 3: Central University uses \$123,000 of a particular toner cartridge for laser printers in the student computer labs each year. The purchasing director of the university estimates the ordering cost at \$45 and thinks that the university can hold this type of inventory at an annual storage cost of 22% of the purchase price. How many months' supply should the purchasing director order at one time to minimize the total annual cost of purchasing and carrying?

Data:

$$D = \$123,000$$

$$I = 0.22 \text{ (22\%)}$$

$$S = \$45$$

Unit = Dollars (\$)

$$\text{Unit Price}(P) = 1 \text{ Unit/dollar}$$

Calculate EOQ [Economic Order Quantity]:

$$\text{EOQ} = Q^* = \sqrt{\frac{2DS}{IP}} = \sqrt{\frac{(2)(123,000)(45)}{(0.22)(1)}} = 7093.53 \approx 7094 \text{ units}$$

Converting one-year usage to one-month usage:

$$\frac{D}{12} = \frac{123,000}{12} = \$10,250$$

Month's usage:

$$\frac{Q^*}{\frac{D}{12}} = \frac{7,094}{10,250} = 0.69 \text{ month } (\approx 3 \text{ weeks})$$

Order Cycles:

$$\frac{D}{Q} = \frac{123,000}{7,094} = 17.34 \text{ orders}$$

The purchasing director of the Central University should order at 0.69 month (or ≈ 3 weeks) to minimize the total annual cost of purchasing and carrying.

Question 4: The soft goods department of a large department store sells 175 units per month of a certain large bath towel. The unit cost of a towel to the store is \$2.50 and the cost of placing an order has been estimated to be \$12.00. The store uses an inventory carrying charge of $I = 27\%$ per year.

At first the problem has given

Annual demand in units for the inventory item (D) = 175 units X 12 months = 2,100 units

Holding or carrying cost per unit per year (H) = \$2.5 per unit X 0.27 = \$0.675 per unit (Need to multiplied 2.5 by 0.27 because the store inventory carrying charge $I = 27\%$ per year)

Setup or ordering cost for each order (S) = \$12 per unit

Determine

(a) The optimal order quantity

To find optimal order quantity is to find EOQ or Q^*

$$Q^* = \sqrt{\frac{2DS}{H}} = \sqrt{\frac{2 \times 2100 \times 12}{2.5 \times 0.27}} = \sqrt{\frac{50,400}{0.675}} = 273.25 \text{ units}$$

So the optimal order quantity is 273.25 units

(b) The order frequency

To find order frequency is to find expected number of orders per annual (N)

$$\text{The order frequency} = N = \frac{\text{Demand}}{\text{Order quantity}} = \frac{D}{Q^*}$$

$$N = \frac{2100}{273.25} = 7.685 \text{ or around 8 orders per year}$$

In one year, the soft goods department need to order 8 orders per year.

(c) The annual holding and setup cost

At first find Annual holding cost

Annual holding cost = (Average inventory level) X (Holding cost per unit per year)

$$= \left(\frac{\text{order quantity}}{2} \right) \text{ X Holding cost per unit per year}$$

$$= \left(\frac{Q}{2} \right) \text{ X H}$$

$$= \left(\frac{273.25 \text{ units}}{2} \right) \text{ X } (2.5 \text{ X } 0.27)$$

$$= 136.625 \text{ units X } \$0.675$$

$$= \$92.222$$

Annual holding cost is \$92.222

Annual setup cost = $\left(\frac{\text{annual demand}}{\text{Number of units in each order}} \right)$ X (Setup or order cost per order)

$$= \left(\frac{D}{Q} \right) \text{ X S}$$

$$= \left(\frac{2100 \text{ units}}{273.25 \text{ units}} \right) \text{ X } \$12$$

$$= 7.685 \text{ X } \$12$$

$$= \$92.223$$

Annual setup cost is \$92.223

If, through automation of the purchasing process, the ordering cost can be cut to \$4.00, what will be

(d) The new economic order quantity

To find new economic order quantity is find the optimal order quantity when ordering cost (S) is change to \$4.00

$$\text{Find } Q^* = \sqrt{\frac{2DS}{H}} = \sqrt{\frac{2 \text{ X } 2100 \text{ X } 4}{2.5 \text{ X } 0.27}} = \sqrt{24888.88} = 157.762 \text{ units}$$

So new economic order quantity is 157.762 units

(e) The order frequency

$$\text{The order frequency} = N = \frac{\text{Demand}}{\text{Order quantity}} = \frac{D}{Q^*}$$

$$N = \frac{2100}{157.762} = 13.311 \text{ orders per year}$$

In one year, the soft goods department need to order 14 orders per year

(f) Annual holding and setup cost

At first find Annual holding cost

Annual holding cost = (Average inventory level) X (Holding cost per unit per year)

$$= \left(\frac{\text{order quantity}}{2} \right) \times \text{Holding cost per unit per year}$$

$$= \left(\frac{Q}{2} \right) \times H$$

$$= \left(\frac{157.76 \text{ units}}{2} \right) \times (2.5 \times 0.27)$$

$$= 78.881 \times \$0.675$$

$$= \$53.245$$

Annual holding cost is \$53.245

Annual setup cost = $\left(\frac{\text{annual demand}}{\text{Number of units in each order}} \right) \times (\text{Setup or order cost per order})$

$$= \left(\frac{D}{Q} \right) \times S$$

$$= \left(\frac{2100 \text{ units}}{157.76 \text{ units}} \right) \times \$4$$

$$= \$53.245$$

Annual setup cost is \$53.245

Question 5: A firm that make electronic circuits has been ordering a certain raw material 250 ounces at a time. The firm estimates that carrying cost is $I = 30\%$ per year, and that ordering cost is about \$20 per order. The current price of the ingredient is \$200 per ounce. The assumption of the basic EOQ model are thought to apply. For what value of annual demand is their action optimal?

From the problem given that $Q^* = 250$ ounces at a time

$$H = \$200 \times 0.30 = \$60 \text{ per unit per year}$$

$$S = \$20 \text{ per order}$$

Annual demand that is there is their action optimal is to find D

Base on EOQ model : $Q^* = \sqrt{\frac{2DS}{H}}$

$$= \sqrt{\frac{2 \times D \times 20}{200 \times 0.30}}$$

$$250 = \sqrt{\frac{40D}{60}}$$

$$250^2 = \left(\sqrt{\frac{40D}{60}} \right)^2$$

$$62,500 = \frac{40D}{60}$$

$$3,750,000 = 40D$$

$$D = 93,750$$

So, the annual demand is 93,750 units for the inventory item.

Question 6:

A printing company estimates that it will require 1,000 reams of a certain type of paper in a given period. The cost of carrying one unit in inventory for that period is 50 cents. The company buys the paper from a wholesaler in the same town, sending its own truck to pick up the orders at a fixed cost of \$20.00 per trip. Treating this cost as the order cost,

- (a) What is the optimum number of reams to buy one time?
- (b) How many times should lots of this size bought during this period?
- (c) What is the minimum cost (holding and set up) of maintaining inventory on this item for period?
- (d) Of this total cost, how much is carrying cost and how much is ordering cost?

(a) The optimum number of reams to buy at one time = economic order quantity (EOQ)

$$EOQ = Q^* = \sqrt{\frac{2DS}{H}}$$

D = annual demand in units for the inventory system

S = setup/ordering cost for each order

H = holding/carrying cost per unit per year

$$Q^* = \sqrt{\frac{(2)(1000)(20)}{0.5}}$$

$$Q^* = 282.84$$

$$Q^* \approx 283 \text{ units}$$

(b) Expected number of orders = N

$$N = \frac{D}{Q}$$

$$N = \frac{1000}{282.84}$$

$$N = 3.54$$

$$N \approx 4 \text{ orders per year}$$

(c) The minimum cost of maintaining inventory on this item for the period = total cost (TC)

TC = carrying cost + setup cost

$$TC = 70.71 + 70.71$$

$$TC = \$141.42$$

(d) Carrying cost = $\left(\frac{Q}{2}\right)(H)$

$$\text{Carrying cost} = \left(\frac{282.84}{2}\right)(0.5)$$

$$\text{Carrying cost} = \$70.71$$

$$\text{Setup cost} = \left(\frac{D}{Q}\right)(S)$$

$$\text{Setup cost} = \left(\frac{1000}{282.84}\right)(20)$$

$$\text{Setup cost} = \$70.71$$

Members:

Saranya Thirati 6204641119

Naturang Changjai 6204641184

Krit Pituckrachai 6204641598

Kritpatsorn Thatsanasuwan 6204641762