

HW#5 Due February 25, 2021

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3. Suppose the price elasticity of demand for heating oil is 0.2 in the short run and 0.7 in the long run.
- If the price of heating oil rises from \$1.80 to \$2.20 per gallon, what happens to the quantity of heating oil demanded in the short run? In the long run? (Use the midpoint method in your calculations.)
 - Why might this elasticity depend on the time horizon?

7. Suppose that your demand schedule for pizza is as follows:

Price	Quantity Demanded (income = \$20,000)	Quantity Demanded (income = \$24,000)
\$8	40 pizzas	50 pizzas
10	32	45
12	24	30
14	16	20
16	8	12

- Use the midpoint method to calculate your price elasticity of demand as the price of pizza increases from \$8 to \$10 if (i) your income is \$20,000 and (ii) your income is \$24,000.
- Calculate your income elasticity of demand as your income increases from \$20,000 to \$24,000 if (i) the price is \$12 and (ii) the price is \$16.

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$$\eta_D \text{ in short run} = 0.2$$

$$\eta_D \text{ in long run} = 0.7$$

If the price of heating oil rises from \$1.80 to \$2.20 per gallon,

$$\% \Delta P = \frac{P_1 - P_0}{P} \cdot 100\%$$

$$= \frac{2.20 - 1.80}{\left(\frac{2.20 + 1.80}{2}\right)} \cdot 100\%$$

$$= \frac{0.4}{2} \cdot 100 = 20\%$$

$$\eta_D \text{ for short run} = 0.2$$

$$0.2 = \frac{\% \Delta Q_D}{\% \Delta P}$$

$$0.2 = \frac{\% \Delta Q_D}{20\%}$$

$$4\% = \% \Delta Q_D$$

$\therefore Q_D$ will decrease 4% in short run.

$$\eta_D \text{ for long run} = 0.7$$

$$0.7 = \frac{\% \Delta Q_D}{\% \Delta P}$$

$$0.7 = \frac{\% \Delta Q_D}{20\%}$$

$$14\% = \% \Delta Q_D$$

$\therefore Q_D$ will decrease 14% in long run.

b) The elasticity depends on the time horizon because there can be more substitutes as the time changes. More substitutes lead to more elasticity.

⑦ a) If income is \$20000, $P = -\frac{1}{4}Q_D + 18$ at (40, 8) and (32, 10).

If income is \$24000, $P = -\frac{2}{5}Q_D + 18$ at (50, 8) and (45, 10)

Price elasticity of demand by midpoint method

i) If income is 20000, $P = 8$ and $Q_D = 40$
 $P = 10$ and $Q_D = 32$

$$\begin{aligned}\eta_D &= \frac{1}{\text{slope}} \cdot \frac{\bar{P}}{\bar{Q}_D} \\ &= \frac{1}{-1/4} \cdot \frac{(8+10)/2}{(40+32)/2} \\ &= -4 \cdot \frac{18/2}{72/2} \\ &= -4 \cdot \frac{1}{4} \\ &= -1\end{aligned}$$

ii) If income is 24000, $P = 8$ and $Q_D = 50$
 $P = 10$ and $Q_D = 45$

$$\begin{aligned}\eta_D &= \frac{1}{\text{slope}} \cdot \frac{\bar{P}}{\bar{Q}_D} \\ &= \frac{1}{-2/5} \cdot \frac{(8+10)/2}{(50+45)/2} \\ &= -\frac{5}{2} \cdot \frac{18}{95} \\ &= -\frac{9}{19} \approx -0.47\end{aligned}$$

b) Income elasticity of demand as income increases from \$20000 to \$24000

i) The price is \$12, the income elasticity of demand is

$$\begin{aligned}\eta_I &= \frac{\% \Delta Q_D}{\% \Delta I} \\ &= \frac{30-24}{24} \cdot 100 \\ &= \frac{24000-20000}{20000} \cdot 100 \\ &= \frac{6}{24} = \frac{5}{4} = 1.25\end{aligned}$$

ii) The price is \$16, the income elasticity of demand is

$$\begin{aligned}\eta_I &= \frac{\% \Delta Q_D}{\% \Delta I} \\ &= \frac{12-8}{8} \cdot 100 \\ &= \frac{24000-20000}{20000} \cdot 100 \\ &= \frac{4}{8} \cdot 100 = \frac{5}{2} = 2.5 \quad \# \end{aligned}$$