



B.E. International Program

Faculty of Economics, Thammasat University



EE 320 Introductory Mathematical Economics (Section 046402)

Semester 1/2013

Practice Problem 6

(Optimization problem – 1 independent variable)

1. Find the local extreme points for:

a) $f(x) = x^3 e^x$ b) $g(x) = x^2 2^x$

2. Exercise 9.2 question 1 in Chiang and Wainwright (2005)

3. Exercise 9.4 questions 3 and 6 in Chiang and Wainwright (2005)

4. For the following functions, (i) find the critical values, (ii) test for concavity to determine relative maxima or minima, (iii) check for inflection points, and (4) evaluate the function at the critical value and inflection points.

a) $f(x) = x^3 - 18x^2 + 96x - 80$

b) $f(x) = -x^3 + 6x^2 + 15x - 32$

c) $f(x) = (2x - 7)^3$

(Questions 5 – 7 are from Sydsaeter and Hammond, 2008)

5. Suppose that

$$R(Q) = 10Q - \frac{Q^2}{1000}, \quad C(Q) = 5000 + 2Q, \quad Q \in [0, 10,000]$$

Find the value of Q that maximizes profits.

6. The price a firm obtains for a commodity varies with demand Q according to the formula $P(Q) = 18 - 0.006Q$. Total cost is $C(Q) = 0.004Q^2 + 4Q + 4500$.

a. Find the firm's profit and the value Q which maximizes profit.

b. Find a formula for the elasticity of $P(Q)$ w.r.t. Q , and find the particular value Q^* of Q at which the elasticity is equal to -1.

c. Show that the marginal revenue is 0 at Q^* .

7. A competitive firm receives a price p for each unit of its output, and pays a price w for each unit of its only variable input. It also incurs set up costs of F . Its output from using x units of variable input is $f(x) = \sqrt{x}$. Determine the firm's revenue, cost, and profit functions.