

Chp6 Integration and its application

1. Find the following integrals;

a) $\int x^{\frac{2}{3}} dx$

b) $\int (2x - 3)^4 dx$

c) $\int \frac{3x^2+2}{\sqrt{x}} dx$

d) $\int \sqrt[3]{x^3 + 3x^2} (x^2 + 2x) dx$

e) $\int \frac{x^2-1}{x\sqrt{x}+\sqrt{x}} dx$

2. Evaluate the following definite integrals

a) $\int_0^1 (x^4 + 2x^3 + 4x + 10) dx$

b) $\int_0^8 x^{\frac{2}{3}} dx$

c) $\int_1^2 1 dx$

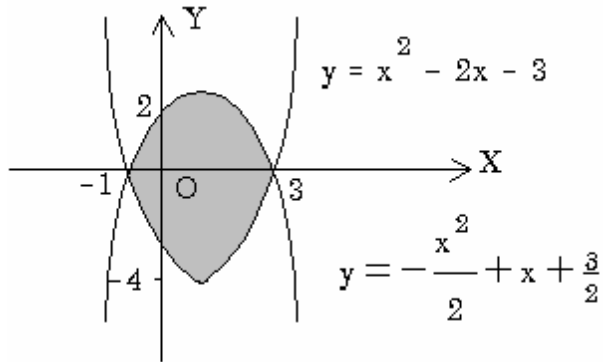
d) $\int_{-8}^8 \sqrt[3]{2 + x^{\frac{2}{3}}} dx$

e) $\int_0^{64} (x^{\frac{1}{2}} + 5x^{\frac{-2}{3}}) dx$

3. Find the area under the graph of the function $y=x^2+4x$ between $x=0$ and $x=3$

4. Find the area between the function $y=6x - x^2$ and x axis from $x=1$ to $x=5$

5. Find the shaded area between these two curves



6. Given market demand and supply functions as $Q=10 - P$ and $Q= -2 + P$, find

- a) Consumer Surplus
- b) Producer Surplus
- c) Total surplus

7. Given a marginal cost function of a firm as $MC= Q^3+2Q^2+2Q+5$ and the firm has fixed costs= 150 baht. Find Average Cost function, Average fixed cost function and Average Variable cost function

8. A marginal propensity to consume is given as 0.25. If a disposable income is zero, the consumption level is equal to 100. Find a consumption function.

9. Given demand function as $P=45 - 0.5Q$, find consumer surplus when $p=32.5$

10. Given supply function as $P=(Q+3)^2$, find producer surplus when $P=81$

11. For a consumer with demand function as $Q=5-P^{1/3}$, find

- a) Consumer Surplus at price $p_0=1$
- b) Consumer Surplus at price $p_1=27$
- c) Change in consumer surplus from the price change $p_0=1$ to $p_1=27$

12. Given the following demand and supply functions for a particular product

$Q_d = 5 - P/3$ and $P = (Q_s + 1)^2$, find consumer and producer surpluses at the equilibrium of this market.