

Instruction:

Exam time: 30 minutes.

You may use a calculator, turn off cell phones. Phone communication are strictly prohibited during the exam.

For each question, write your answer in the blank space provided.

Manage your time carefully and answer as many questions as you can.

Question1 (40 points)

Your score.....

Suppose the daily log return r_t of Stock A follows the model:

$$r_t = 0.002 + a_t$$

$$a_t = \sigma_t \epsilon_t$$

where ϵ_t is an independent and identically distributed (iid) sequence of standardized Student-t distribution with 5 degrees of freedom. In addition,

$$\sigma_t^2 = 0.01 + 0.1a_{t-1}^2$$

Question1.1 (10 points)

Your score.....

From the above model, Find out the unconditional Expectation of $a_t : E(a_t)$ and the unconditional expectation of $r_t : E(r_t)$

Question1.2 (10 points)

Your score.....

Find out the unconditional variance of a_t : $Var(a_t)$ and the conditional variance of a_t : $Var(a_t|F_{t-1})$

Question1.3 (10 points)

Your score.....

Let $h = 100$ be the forecast origin with $a_h = 0.015$ and $\sigma_h = 0.2$. Calculate the 1-step ahead prediction $r_h(1)$ and 1-step ahead volatility forecast.

Question1.4 (10 points)

Your score.....

Calculate the ∞ -step ahead prediction $r_h(\infty)$ and the ∞ -step ahead volatility forecast at the forecast origin h .