

Assignment 1

From the given data set, estimate the following models:

Capital Asset Pricing Model (CAPM)

$$\text{CAPM: } r_{jt} = \alpha_j + \beta_{j1} r_{mt} + \varepsilon_{jt} \quad (1)$$

Fama & French three-factor Model (FF)

$$\text{Fama \& French: } r_{jt} = \alpha_j + \beta_{j1} r_{mt} + \beta_{j2} r_{smbt} + \beta_{j3} r_{hmlt} + \varepsilon_{jt} \quad (2)$$

Where: r_{jt} = excess return on portfolio j at time t and
 r_{mt} = excess return on market portfolio at time t – representing market risk premium.
 r_{smbt} = return on a small-stock portfolio minus the return on a large-stock portfolio (Small Minus Big) at time t – representing size premium.
 r_{hmlt} = return on a value-stock portfolio minus the return on a growth-stock portfolio (High Minus Low) at time t – representing value premium.

Figure 1

```
. reg rj rm
```

Source	SS	df	MS	Number of obs	=	11,959
Model	11449.5344	1	11449.5344	F(1, 11957)	=	5988.94
Residual	22859.1346	11,957	1.91177842	Prob > F	=	0.0000
				R-squared	=	0.3337
				Adj R-squared	=	0.3337
Total	34308.669	11,958	2.86909759	Root MSE	=	1.3827

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
rm	.9947206	.0128536	77.39	0.000	.9695254	1.019916
_cons	.0084273	.0126552	0.67	0.505	-.0163789	.0332335

```
. test rm=1
```

```
( 1)  rm = 1
```

```
F( 1, 11957) = 0.17
Prob > F = 0.6813
```

Figure 2

```
. reg rj rm smb hml
```

Source	SS	df	MS	Number of obs	=	11,959
Model	11681.1999	3	3893.73328	F(3, 11955)	=	2057.22
Residual	22627.4691	11,955	1.89272013	Prob > F	=	0.0000
				R-squared	=	0.3405
				Adj R-squared	=	0.3403
Total	34308.669	11,958	2.86909759	Root MSE	=	1.3758

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
rm	1.005554	.0128271	78.39	0.000	.9804104	1.030697
smb	.0371377	.0061189	6.07	0.000	.0251437	.0491318
hml	.0562866	.00609	9.24	0.000	.0443492	.068224
_cons	.0073088	.0125928	0.58	0.562	-.0173752	.0319928

```
. test rm=1
```

```
( 1)  rm = 1
```

```
      F( 1, 11955) =    0.19
      Prob > F =    0.6651
```

(1) Determine whether there exists significant Jensen Alpha.

Jensen Alpha is not significant in CAPM model and FF model since the p-value in CAPM model is greater than 0.05 ($0.505 > 0.05$) showing in [Figure 1](#) and p-value in FF model is also greater than 0.05 as well ($0.562 > 0.05$) showing in [Figure 2](#).

(2) Determine whether portfolio j has the same risk as the market.

In order to find that portfolio j has the same risk as the market, the beta of portfolio j has to be "1" ($\beta_j = 1$)

CAPM model :

Testing the hypothesis : $H_0 : \beta_j = 1$

The p-value is greater than 0.05 ($0.6812 > 0.05$) showing in [Figure 1](#) which means that we fail to reject H_0 , portfolio j has the same risk as the market.

FF model :

Testing the hypothesis : $H_0 : \beta_{j1} = 1$

The p-value is also greater than 0.05 ($0.6651 > 0.05$) showing in Figure 2 which means that we fail to reject H_0 , portfolio j also has the same risk as the market.

(3) Determine whether there exists significant size premium.

From Figure 2, the p-value of r_{smbt} is less than 0.05 ($0.000 < 0.05$), there exists a significant size premium.

(4) Determine whether there exists significant growth (value) premium.

From Figure 2, The p-value of r_{hmlt} is less than 0.05 ($0.000 < 0.05$), there exists significant growth (value) premium.

(5) Compare CAPM and FF models and determine which model is the most appropriated model. Why?

```
. test smb hml
```

```
( 1)  smb = 0
```

```
( 2)  hml = 0
```

```

F( 2, 11955) = 61.20
Prob > F = 0.0000

```

Testing the hypothesis : $H_0 : \beta_2 = \beta_3 = 0$

The p-value is less than 0.05 ($0.0000 < 0.05$), we reject H_0 .

FF model is more appropriate and we should not eliminate r_{smbt} and r_{hmlt} out of the model.

To study calendar effect (January effects) from the data set, estimate the following models:

$$r_{jt} = \alpha_j + \gamma_j D_{1t} + \beta_{j1} r_{mt} + \beta_{j2} r_{smbt} + \beta_{j3} r_{hmlt} + \varepsilon_{jt} \quad (3)$$

where: $D_{1t} = 1$ on January and $= 0$ otherwise.

Figure 3

```
. reg rj rm smb hml d1
```

Source	SS	df	MS	Number of obs	=	11,959
Model	11683.8263	4	2920.95657	F(4, 11954)	=	1543.31
Residual	22624.8427	11,954	1.89265875	Prob > F	=	0.0000
				R-squared	=	0.3406
				Adj R-squared	=	0.3403
Total	34308.669	11,958	2.86909759	Root MSE	=	1.3757

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
rm	1.005405	.0128275	78.38	0.000	.9802607	1.030549
smb	.0369291	.0061214	6.03	0.000	.0249302	.048928
hml	.0562495	.00609	9.24	0.000	.0443121	.0681868
d1	.05393	.045781	1.18	0.239	-.0358082	.1436682
_cons	.0028773	.0131425	0.22	0.827	-.0228842	.0286388

(6) Determine whether there exist significant January effects.

From the ANCOVA model shown in *Figure3*, D1 which is January effects is not significant since the p-value of D1 is greater than 0.05 (0.239>0.05), we failed to reject Ho.

(7) Make interpretation of estimated result of model (3) (including (1) sign, (2) overall test, (3) R-square, and (4) individual test).

From the estimated result of model 3, we can interpret that rm, smb, hml, d1 and the interception are all positive signs. From the overall F-test, its p-value is less than 0.05 (0.0000<0.05), we reject Ho, meaning that rm, smb, hml, d1 have significance to explain the portfolio j. The R-square is equal to 0.3406 implied that this model can explain the variation in rjt by 34.06%. In terms of individual test, we fail to reject for d1 since its p-value is greater than 0.05 (0.239>0.05) while we reject for rm, smb and hml since they have their p-value less than 0.05 (0.000<0.05). We can conclude that d1 or the January effects is not significant, in other words, January effects do not have an impact on the portfolio j.

$$\begin{aligned}
 r_{jt} = & \alpha_j + \beta_{j1}r_{mt} + \beta_{j2}r_{smbt} + \beta_{j3}r_{hmlt} \\
 & + \gamma_j D_{1t} + \beta_{j1}D_{1t}r_{mt} + \beta_{j2}D_{1t}r_{smbt} + \beta_{j3}D_{1t}r_{hmlt} + \varepsilon_{jt} \quad (4)
 \end{aligned}$$

(8) Perform Chow-test (using Intercept and Slope Dummy) whether January and other month share the same structure of the Fama-French model (Model (2) vs Model (4)).

```
. reg rj rm smb hml
```

Source	SS	df	MS	Number of obs	=	11,959
Model	11681.1999	3	3893.73328	F(3, 11955)	=	2057.22
Residual	22627.4691	11,955	1.89272013	Prob > F	=	0.0000
				R-squared	=	0.3405
				Adj R-squared	=	0.3403
Total	34308.669	11,958	2.86909759	Root MSE	=	1.3758

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
rm	1.005554	.0128271	78.39	0.000	.9804104	1.030697
smb	.0371377	.0061189	6.07	0.000	.0251437	.0491318
hml	.0562866	.00609	9.24	0.000	.0443492	.068224
_cons	.0073088	.0125928	0.58	0.562	-.0173752	.0319928

```
. sca rss1=e(rss)
```

```
. sca n1=e(N)
```

```
. reg rj rm smb hml if d1==0
```

Source	SS	df	MS	Number of obs	=	10,974
Model	10805.6192	3	3601.87308	F(3, 10970)	=	1887.21
Residual	20936.975	10,970	1.90856654	Prob > F	=	0.0000
				R-squared	=	0.3404
				Adj R-squared	=	0.3402
Total	31742.5942	10,973	2.89279087	Root MSE	=	1.3815

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
rm	1.008159	.0134224	75.11	0.000	.9818484	1.034469
smb	.0364768	.0064347	5.67	0.000	.0238636	.04909
hml	.0553364	.0063956	8.65	0.000	.0427998	.0678729
_cons	.0027652	.0131985	0.21	0.834	-.0231062	.0286367

```
. sca rss2=e(rss)
```

```
. sca n2=e(N)
```

```
. reg rj rm smb hml if d1==1
```

Source	SS	df	MS	Number of obs	=	985
Model	872.032797	3	290.677599	F(3, 981)	=	169.11
Residual	1686.17832	981	1.71883621	Prob > F	=	0.0000
				R-squared	=	0.3409
				Adj R-squared	=	0.3389
Total	2558.21111	984	2.59980804	Root MSE	=	1.311

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
rm	.9725647	.0435176	22.35	0.000	.8871664	1.057963
smb	.0402395	.0198549	2.03	0.043	.0012766	.0792024
hml	.0659675	.0199538	3.31	0.001	.0268104	.1051246
_cons	.0580564	.0421181	1.38	0.168	-.0245956	.1407084

```
. sca rss3=e(rss)
```

```
. sca n3=e(N)
```

```
. sca ChowTest=((rss1-rss2-rss3)/4)/((rss2+rss3)/(n2+n3-2*4))
```

```
. sca list ChowTest
```

```
ChowTest = .56997206
```

```
. g rmd1 = rm*d1
```

```
. g smbd1 = smb*d1
```

```
. g hml1 = hml*d1
```

```
. reg rj rm smb hml d1 rmd1 smbd1 hml1
```

Source	SS	df	MS	Number of obs	=	11,959
Model	11685.5157	7	1669.35938	F(7, 11951)	=	881.86
Residual	22623.1533	11,951	1.89299249	Prob > F	=	0.0000
				R-squared	=	0.3406
				Adj R-squared	=	0.3402
Total	34308.669	11,958	2.86909759	Root MSE	=	1.3759

rj	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
rm	1.008159	.0133675	75.42	0.000	.9819563	1.034361
smb	.0364768	.0064084	5.69	0.000	.0239153	.0490383
hml	.0553364	.0063695	8.69	0.000	.0428511	.0678216
d1	.0552912	.0461135	1.20	0.231	-.0350988	.1456811
rmd1	-.035594	.0475853	-0.75	0.454	-.1288689	.0576808
smbd1	.0037628	.0217997	0.17	0.863	-.0389682	.0464937
hml1	.0106311	.0218876	0.49	0.627	-.0322721	.0535344
_cons	.0027652	.0131445	0.21	0.833	-.0230002	.0285307

```
. test d1 rmd1 smbd1 hmdl1

( 1)  d1 = 0
( 2)  rmd1 = 0
( 3)  smbd1 = 0
( 4)  hmdl1 = 0

F( 4, 11951) =    0.57
Prob > F =    0.6844
```

From testing $H_0 : d1 = rmd1 = smbd1 = hmdl1 = 0$, the p-value is greater than 0.05 (0.6844 > 0.05), we failed to reject H_0 . Hence, there is no structure change in this case.