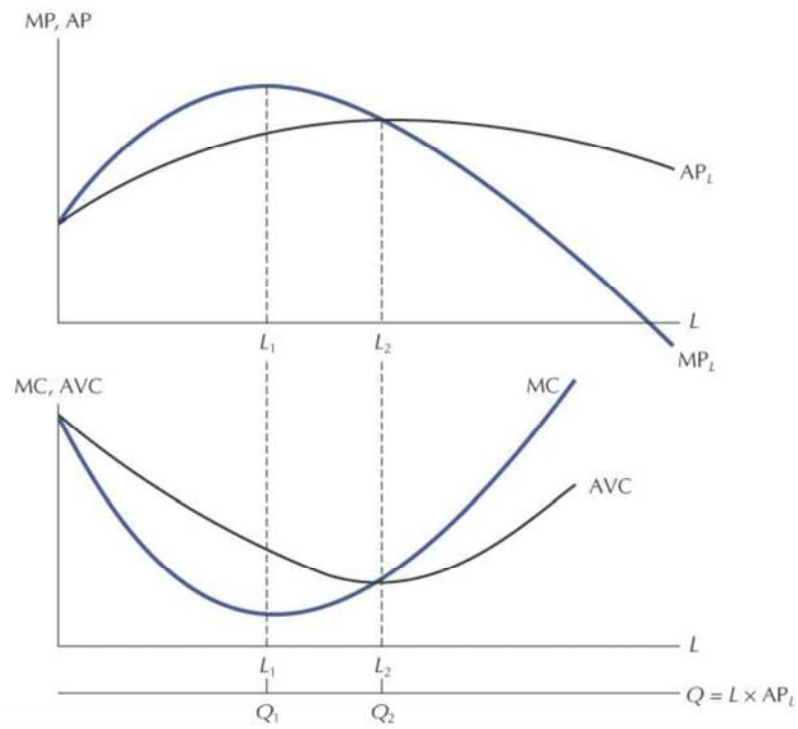
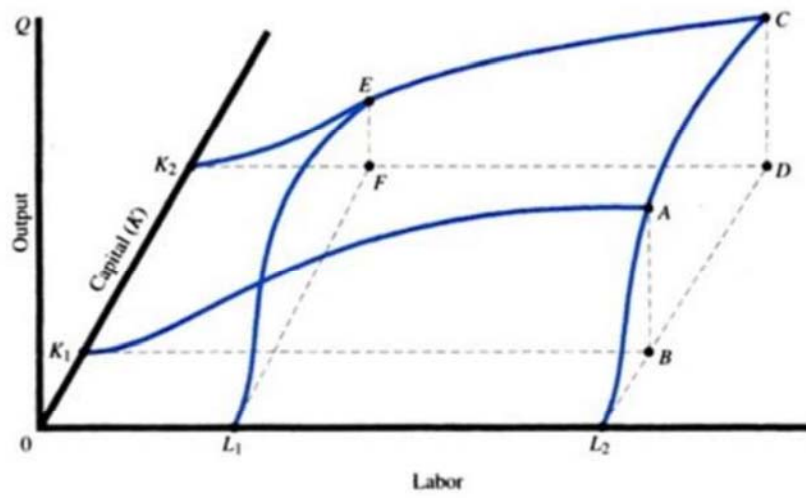


Figure 10.9: The Relationship Between MP, AP, MC, and AVC



# Continuous Production Surface



## Production Function With Two Inputs

$$Q = f(L, K)$$

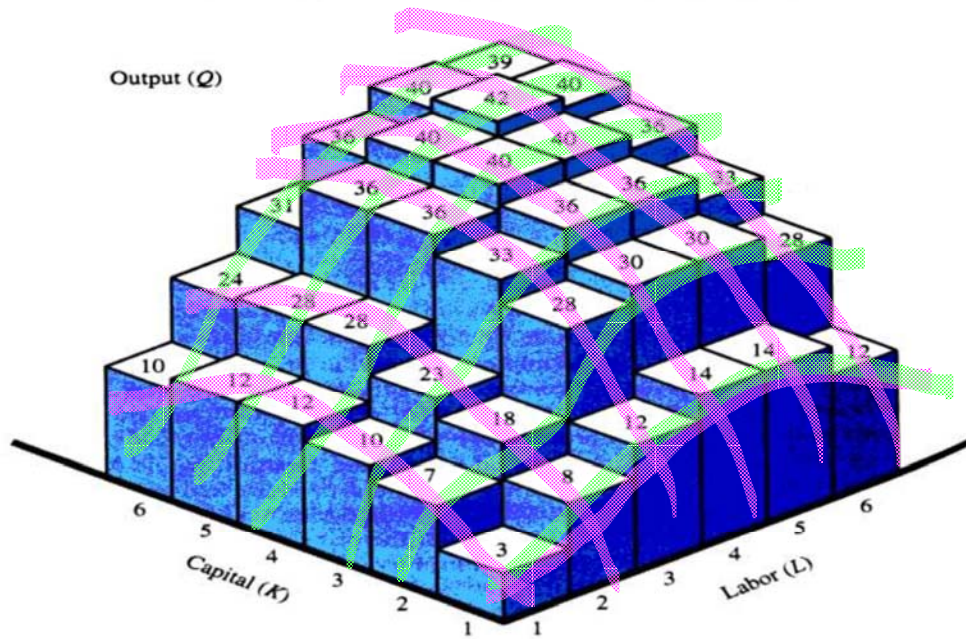
K							Q
6	10	24	31	36	40	39	
5	12	28	36	40	42	40	
4	12	28	36	40	40	36	
3	10	23	33	36	36	33	
2	7	18	28	30	30	28	
1	3	8	12	14	14	12	
	1	2	3	4	5	6	L

# PRODUCTION IN THE LONG RUN

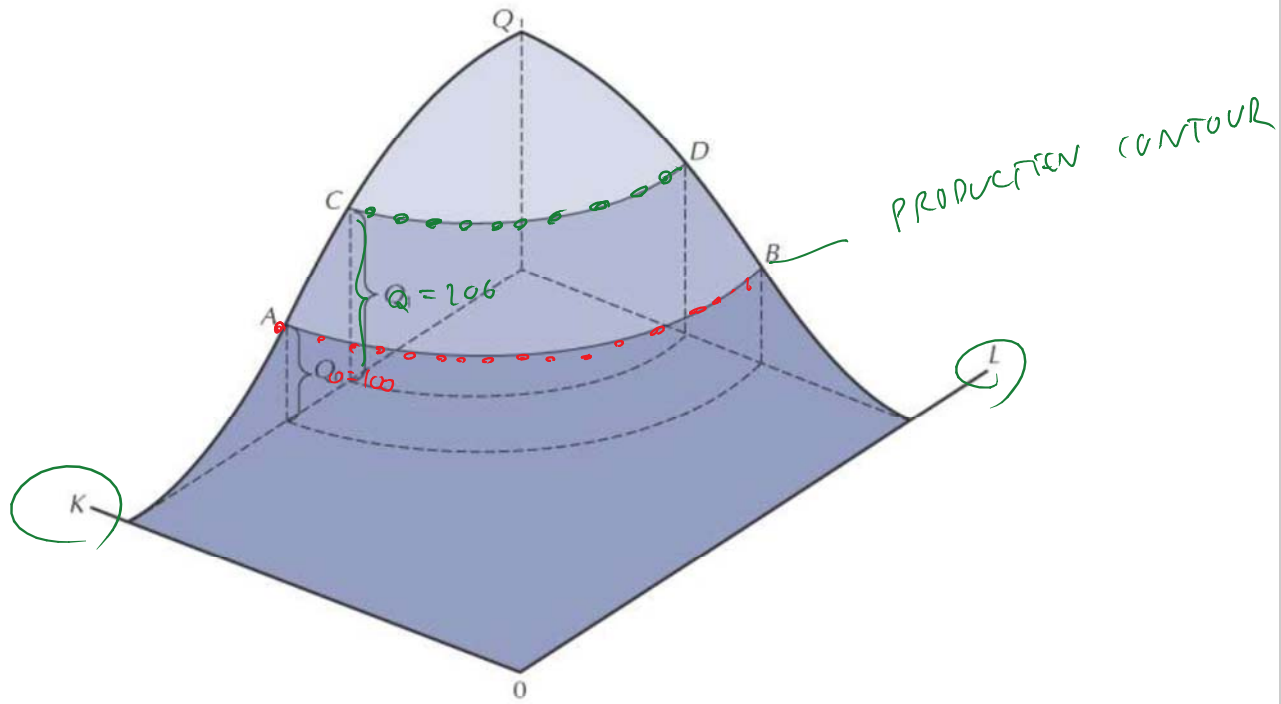
- NO FIXED INPUTS
- ALL INPUTS BECOME VARIABLE.

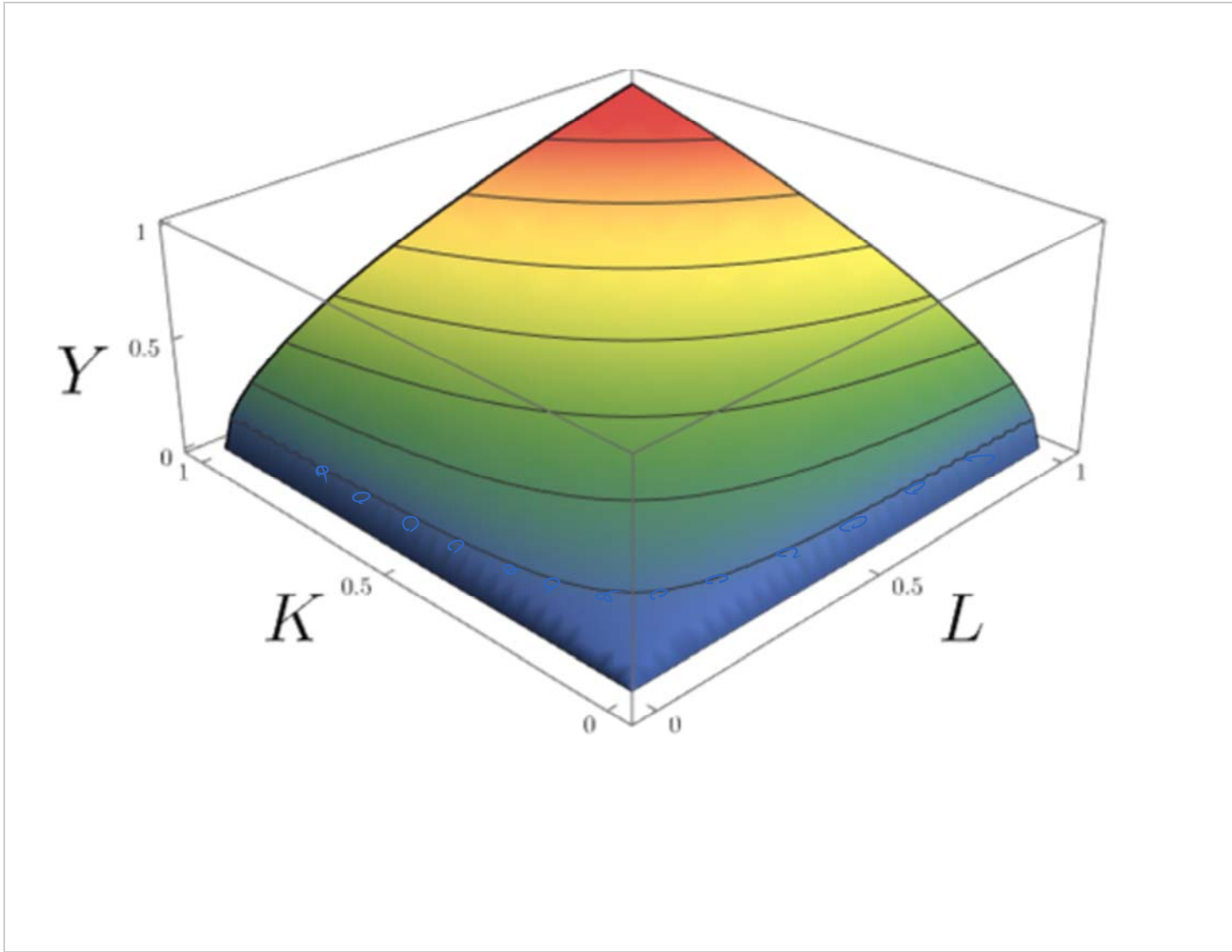
# Production Function With Two Inputs

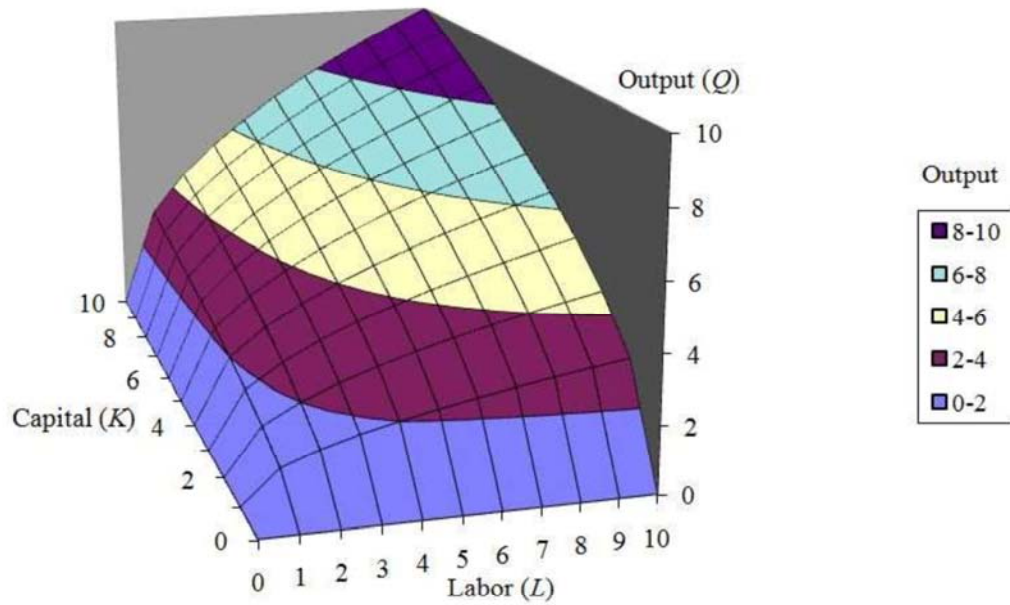
## Discrete Production Surface

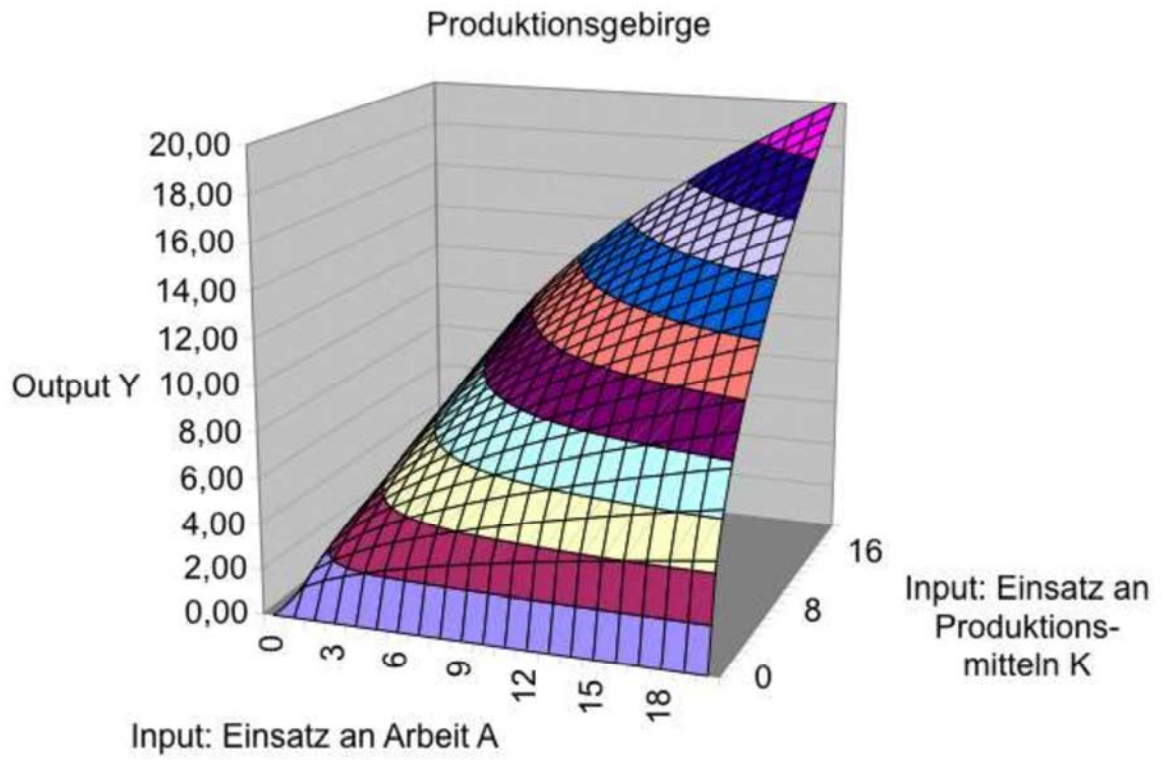


# Figure A9-4: The Production Mountain

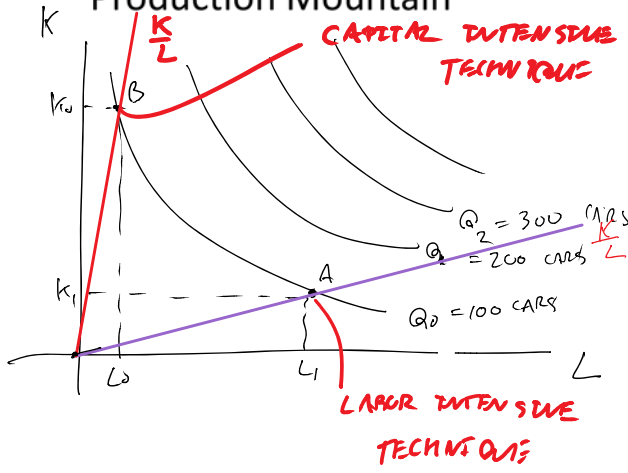








# The Isoquant Map Derived from the Production Mountain



AN ISOQUANT IS  
A CURVE THAT CONTAINS  
ALL INPUT COMBINATIONS THAT  
DELIVER THE SAME AMOUNT OF  
OUTPUT.

EX:  $A(L_1, K_1)$   
 $B(L_0, K_0)$  }  $\rightarrow Q = 100$

$$\left(\frac{K}{L}\right)_{AT A} < \left(\frac{K}{L}\right)_{AT B}$$

$$Q = F(L, K)$$

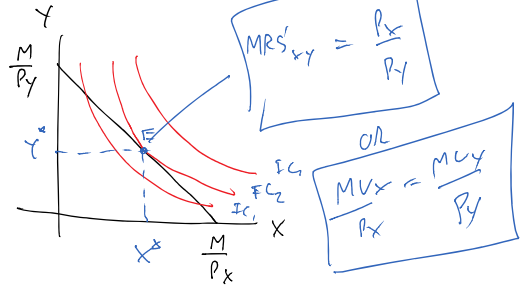
$\downarrow$        $\downarrow$   
 WAGE      RENTAL RATE

A CONSUMER

$$\begin{aligned} \text{MAX } U(X, Y) \\ \text{s.t. } P_x X + P_y Y = M \end{aligned}$$

UMP  
 $(X^*, Y^*) \rightarrow \text{MAX } U$

$$P_x, P_y, M$$



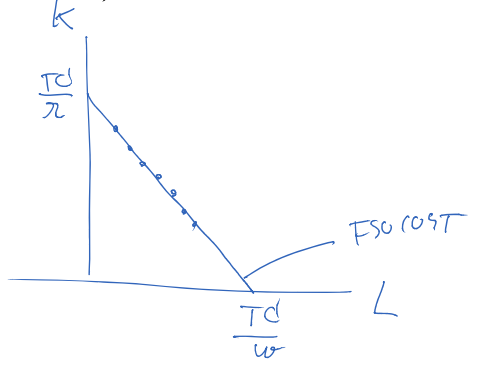
A PRODUCER

$$\begin{aligned} \text{MIN } TC = w \cdot L + r \cdot K \\ \text{s.t. } Q = \bar{Q} \end{aligned}$$

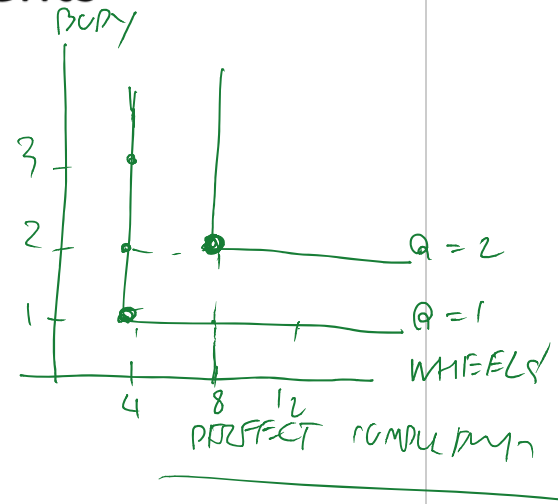
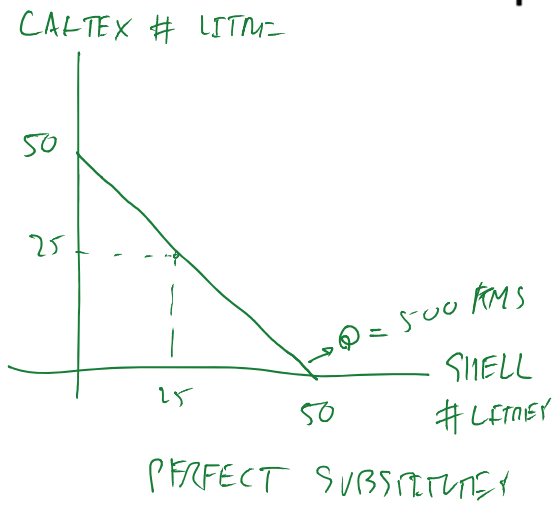
COST-MINIMIZATION  
PROBLEM

$(L^*, K^*) \rightarrow \text{MIN } TC$

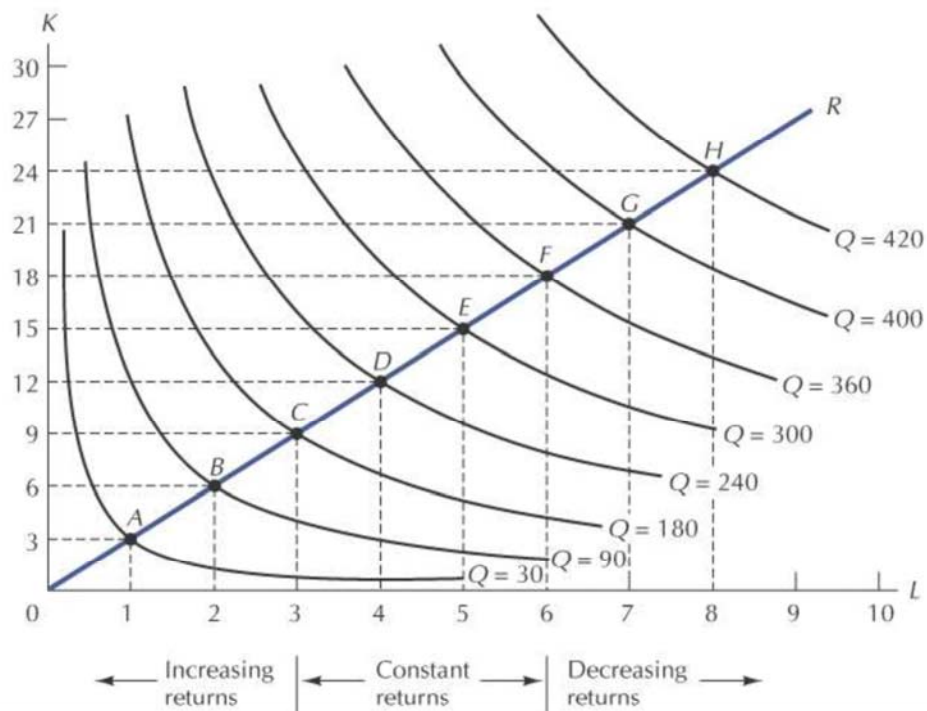
$$w = P_L, r = P_K, \bar{Q}$$



# Isoquant Maps for Perfect Substitutes and Perfect Complements



# Figure 9-11: Returns to Scale Shown on the Isoquant Map



Point	L	% change	K	% change	Q	% change	RTS
A	1	-	3	-	30	-	
B	2	100.0%	6	100.0%	90	200%	IRS
C	3	50.0%	9	50.0%	180	100%	IRS
D	4	33.3%	12	33.3%	240	33%	CRS
E	5	25.0%	15	25.0%	300	25%	CRS
F	6	20.0%	18	20.0%	360	20%	CRS
G	7	16.7%	21	16.7%	400	11%	DRS
H	8	14.3%	24	14.3%	420	5%	DRS

Note: Calculated from Figure 9-11: Returns to Scale Shown on the Isoquant Map, Frank (2006).

7.4



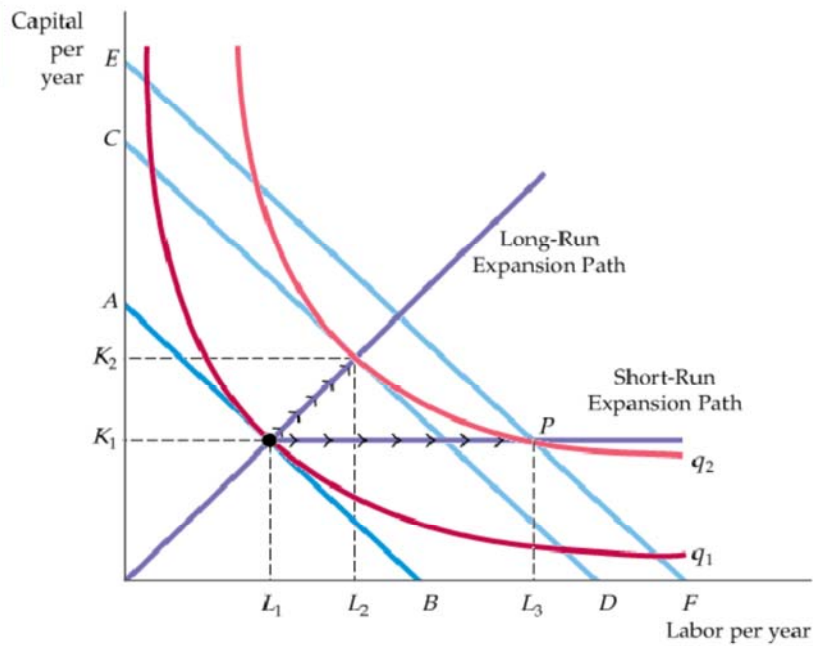
## The Inflexibility of Short-Run Production

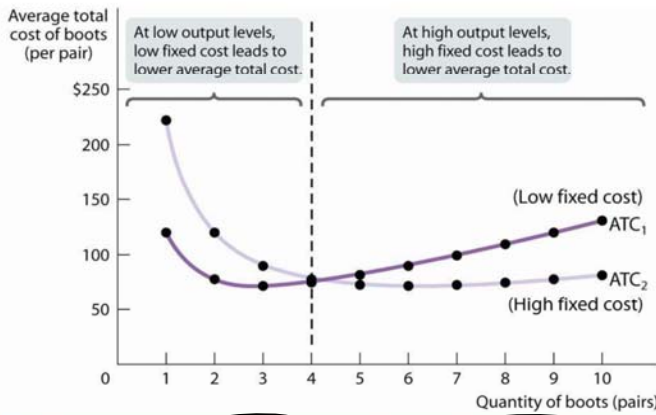
Figure 7.7

### The Inflexibility of Short-Run Production

When a firm operates in the short run, its cost of production may not be minimized because of inflexibility in the use of capital inputs.

Output is initially at level  $q_1$ . In the short run, output  $q_2$  can be produced only by increasing labor from  $L_1$  to  $L_3$  because capital is fixed at  $K_1$ . In the long run, the same output can be produced more cheaply by increasing labor from  $L_1$  to  $L_2$  and capital from  $K_1$  to  $K_2$ .





## Choosing the Level of Fixed Cost for Ben's Boots

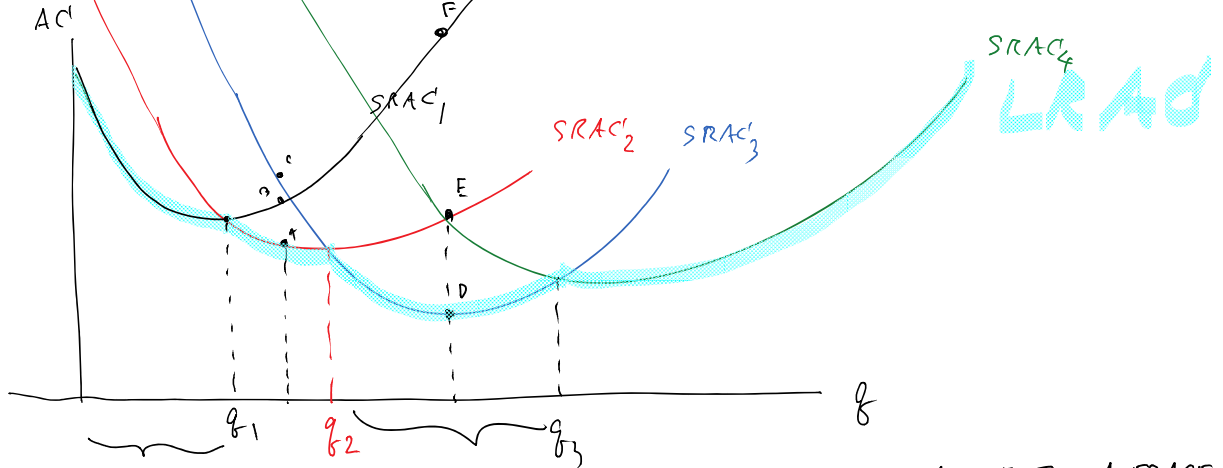
There is a trade-off between higher fixed cost and lower variable cost for any given output level, and vice versa.

But as output goes up, average total cost is lower with the higher amount of fixed cost.

Quantity of boots (pairs)	Low fixed cost (FC = \$108)			High fixed cost (FC = \$216)		
	Variable cost	Total cost	Average total cost of boots ATC <sub>1</sub> (per pair)	Variable cost	Total cost	Average total cost of boots ATC <sub>2</sub> (per pair)
1	\$12	\$120	\$120	\$6	\$222	\$222
2	48	156	78	24	240	120
3	108	216	72	54	270	90
4	192	300	75	96	312	78
5	300	408	81.6	150	366	73.2
6	432	540	90	216	432	72
7	588	696	99.4	294	510	72.9
8	768	876	109.5	384	600	75
9	972	1,080	120	486	702	78
10	1,200	1,308	130.8	600	816	81.6


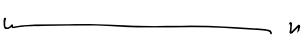




14

NOW, WE ARE IN LONG-RUN PRODUCTION. ALL INPUTS CAN BE VARIED, AMOUNT OF CAPITAL (K) CAN BE CHOSEN TO MATCH W/ YOUR DESIRABLE LEVEL OF YOUR OUTPUT.



LRAC (LONG-RUN AVERAGE COST) REPRESENT THE LOWEST AVERAGE COST OF PRODUCTION IN THE LONG RUN WHEN A MANAGER IS FREE TO CHOOSE AN APPROPRIATE LEVEL OF K TO MINIMIZE HIS AVERAGE COST OR UNIT COST.

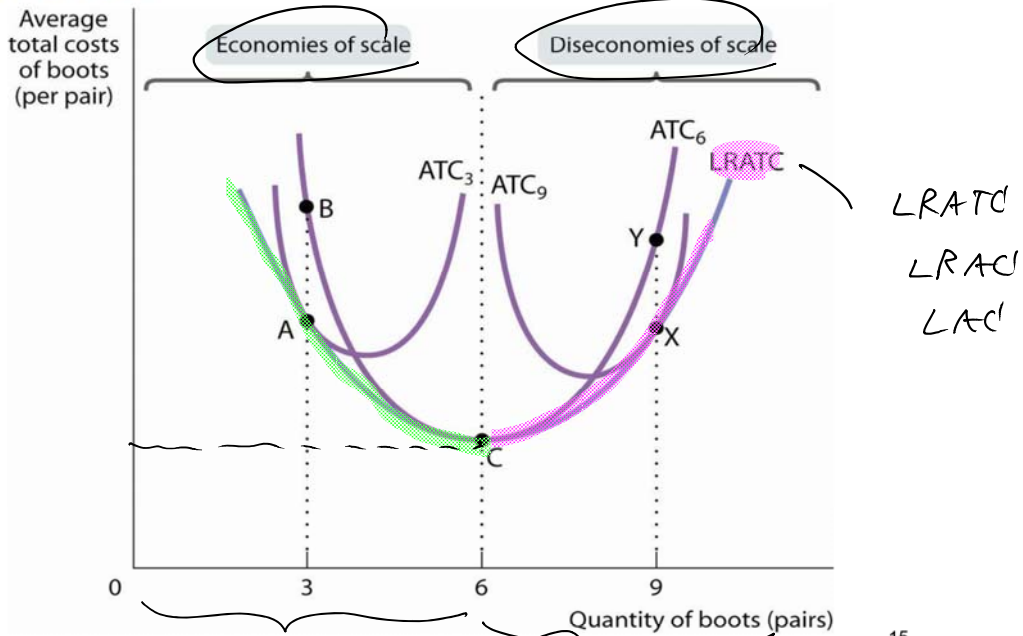
i.e., IF  $Q \leq 1$ , FACTORY W/ 1 MACHINE MINIMIZES YOUR AC,  
IF  $Q > 1$ , 2 MACHINES ...

i.e., IF  $q \leq 1$  , FACTORY W/ 1 MACHINE MINIMIZES YOUR AC,  
 IF  $q_1 < q \leq 2$  ,  2 MACHINES   
 IF  $q_2 < q \leq q_3$  ,  3 MACHINES   
 IF  $q > q_3$  ,  4 MACHINES 

LRAC IS AN ENVELOPE CURVE OF MANY SRACs.

(  
 $q_1, q_2, q_3$ )

## Short-Run and Long-Run Average Total Cost Curves



EoS!

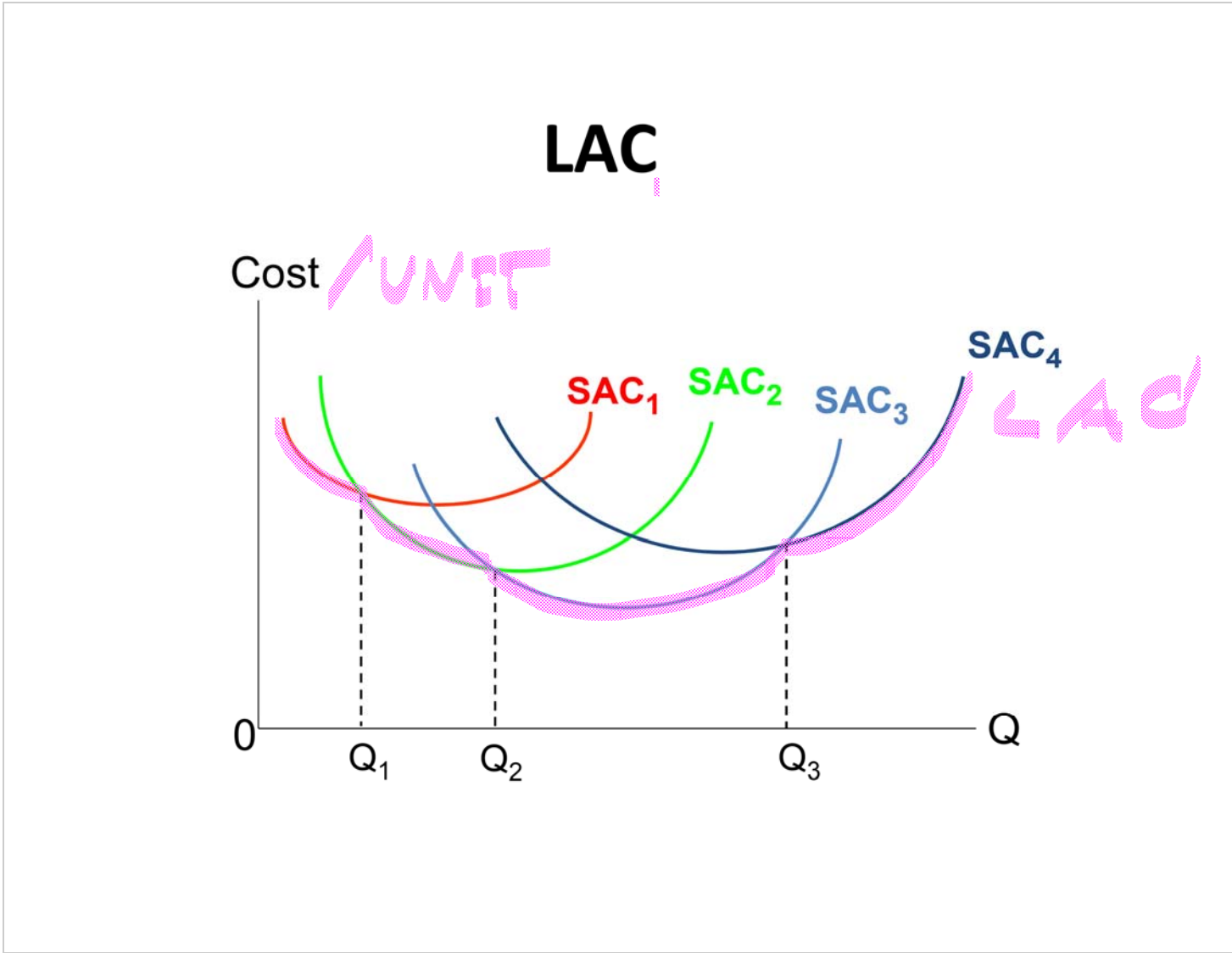
WHEN YOU INCREASE  
YOUR OUTPUT,  
COST PER UNIT  
FALLS

- SPECIALIZATION
- BETTER PRICE FOR BUYING RAW MATERIALS FROM SUPPLIERS

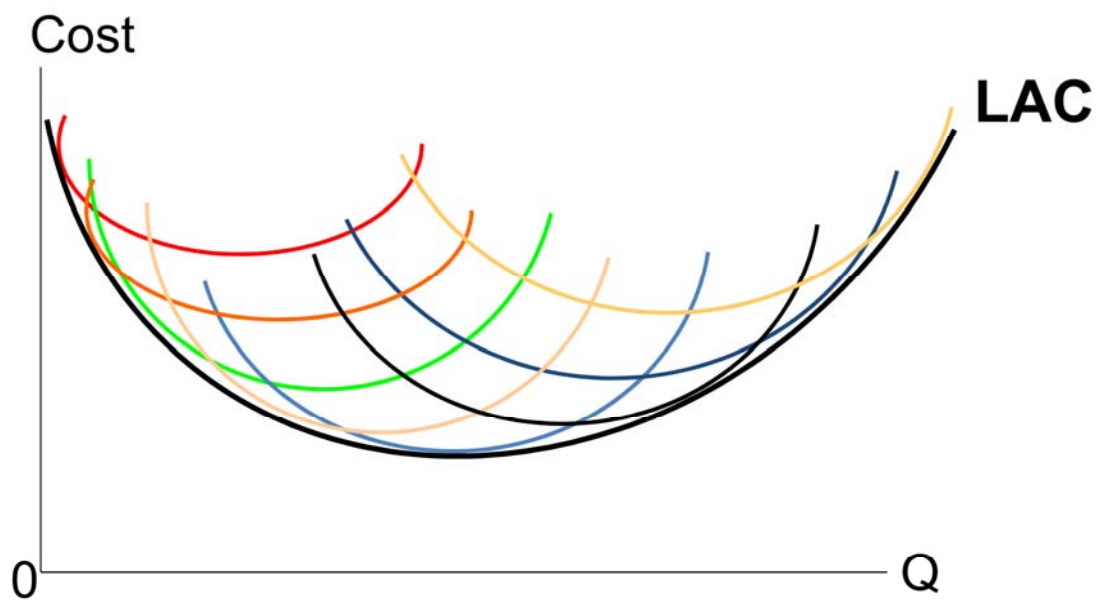
DISECONOMIES OF SCALE:

AS Q ↑, LRAVC ↑ (WHY?)

- ORGANIZATION BECOMES TOO BIG TO MANAGE
- MISCOMMUNICATION AMONG SEVERAL DEPARTMENTS IN THE FIRM.



# Long Run Average Cost Curve (LAC)



**Why would a bathroom equipment manufacturer bake the image of a housefly onto the center of its ceramic urinals?**



*This example is base on Stefan Verhagen, "Fly in the Pot," Cornell Business, April 21, 1992.*