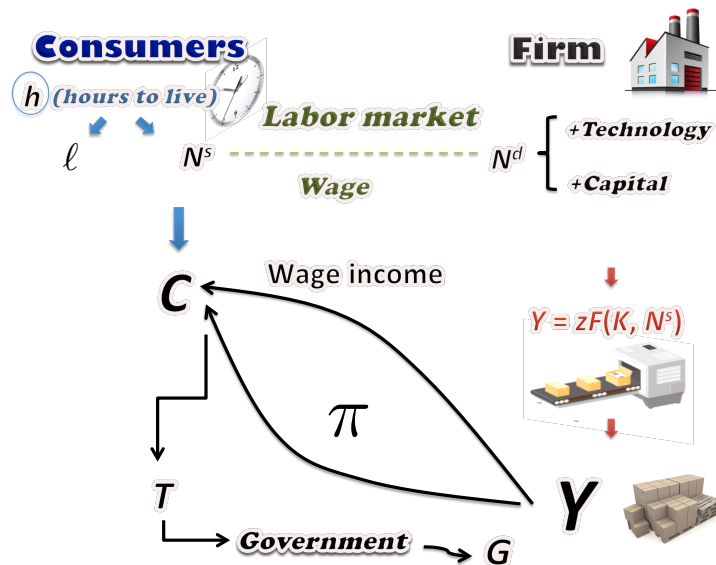


A Short Note: Ch.3 A Closed Economy One-Period Macroeconomic Model (Part 1)

1. One period decisions; static analysis
2. Consumers
3. Firm
4. Government
5. Equilibrium and Pareto Optimality
6. Application

1 One-period decisions:



2 Consumers : A representative consumer

- Utility Function : $U = U(C, \ell)$,
 $\frac{\partial U}{\partial C} = MU_C \dots 0, \frac{\partial^2 U}{\partial^2 C} \dots \dots 0, MU_C \downarrow$ as $C \uparrow$
 $\frac{\partial U}{\partial \ell} = MU_\ell \dots 0, \frac{\partial^2 U}{\partial^2 \ell} \dots \dots 0, MU_\ell \downarrow$ as $\ell \uparrow$
- Budget constraint :
 $C = \dots \dots \dots$
 $C + w\ell = \dots \dots \dots$

The household (consumer) budget constraint may have a kink because

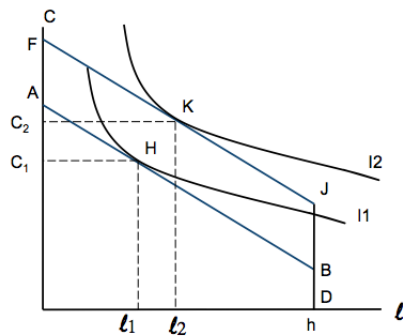
From the budget constraint the maximum ℓ will be equal to Putting together, since $\ell \leq h$, the budget constraint has a kink at ($\ell = \dots$, $C = \dots$)

w is “the market price” of leisure.



- Optimization : tangency point between indifference curve and the budget line, corner solution is impossible

- Change in non-wage income ($\pi - T$).



An increase in $\pi - T$

- An increase in $\pi - T$ (by JB) causes the consumer to increase both C and ℓ .
- For a given real wage, $(\pi - T) \uparrow \Rightarrow C \uparrow$ and $\ell \uparrow$
- This is called effect.

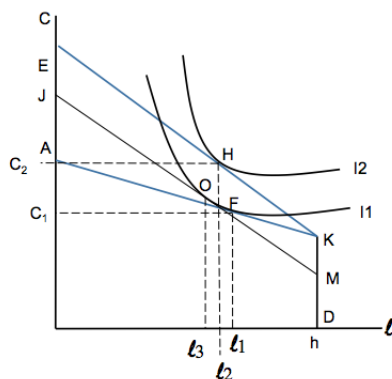
- Change in real wage (w)

* $w \uparrow \Rightarrow$ Income Effect $\Rightarrow$ wage income..... $\Rightarrow$ income $\uparrow \Rightarrow C \dots, \ell \dots$
 $\Rightarrow$ Substitution Effect $\Rightarrow \ell$ becomes relatively more expensive $\Rightarrow C \dots, \ell \dots$

(Note: A good is normal to consumer if its consumption when income rises.

A good is inferior to consumer if its consumption..... when income rises.)

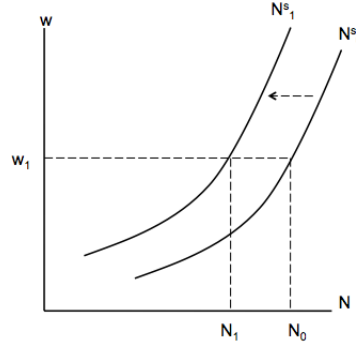
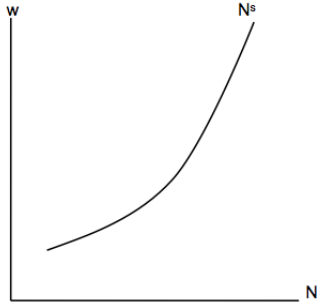
Stronger substitution effect



- * The budget line rotates clockwise (the slope and the vertical intercept) from
- * The optimal point changes from to
- * Draw AM, AM is parallel to the budget line (relative price change).
- * AM is tangent to (the IC). (keeping income constant)
- * Point O is where AM is tangent to the IC.
- * FO is effect
- * OH is effect
- * $FO > OH$, C increases and ℓ decreases.
- * So N^s increases.

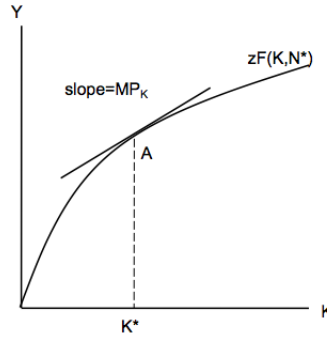
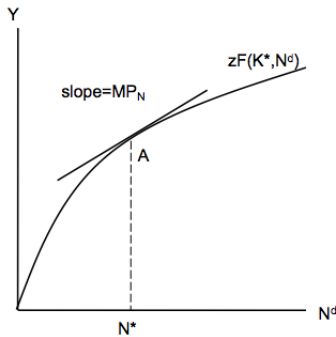
- Derive Labor supply function $N^s(w) = h - \ell(w)$.

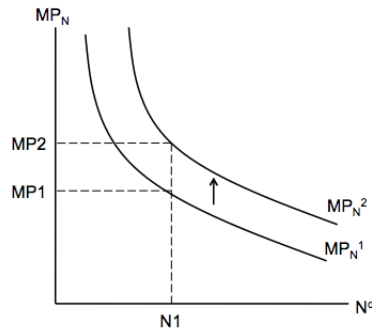
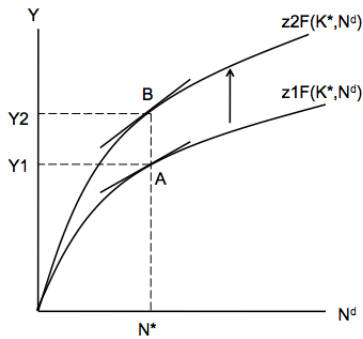
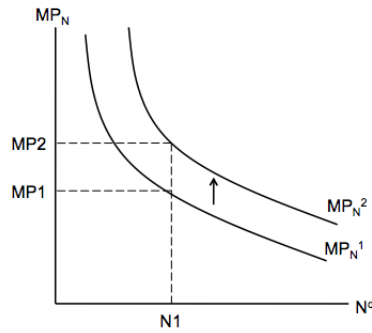
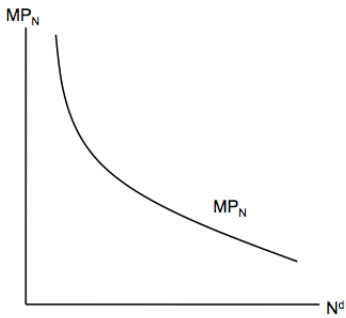
- * $w \uparrow$ (keeping non-wage income $(\pi - T)$ constant $\Rightarrow \ell \downarrow$ (stronger substitution effect) $\Rightarrow N^s \uparrow$
- * As non-wage income $(\pi - T)$ increases, ℓ for all levels of real wage (a pure income effect). As a result, N^s for all levels of wage.



3 Firm : A representative firm

- $Y = zF(K, N^d)$;
 - Y = output of consumption goods;
 - K = capital input;
 - N^d = labor input (hours);
 - z = total factor productivity (TFP).
 - $\frac{\partial Y}{\partial K} = \frac{\Delta Y}{\Delta K} = MP_K \dots 0$, $\frac{\partial Y}{\partial N} = \frac{\Delta Y}{\Delta N} = MP_N \dots 0$; upward slope production function
 - $\frac{\partial^2 Y}{\partial^2 K} \dots 0$, MP_K as $K \uparrow$; concave production function
 - $\frac{\partial^2 Y}{\partial^2 N} \dots 0$, MP_N as $N \uparrow$; concave production function
 - $\frac{\partial Y}{\partial K} = z \frac{\partial F}{\partial K}$, $\frac{\partial Y}{\partial N} = z \frac{\partial F}{\partial N}$
- Constant returns to scale:
 - $zF(xK, xN^d) = xzF(K, N^d)$
 - Increase each input by x times will raise the total output by x times.





- Profit maximization condition

$$\pi = zF(K, N^d) - wN^d$$

VMPL = Value of the Marginal Product the marginal product of an input

Profit maximization condition :

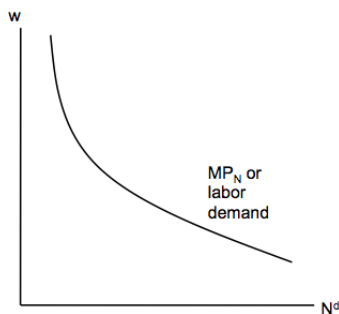
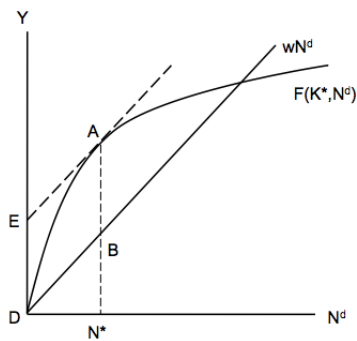
Slope of Y = slope of wN^d ;

$VMPL$ = real wage ,

$$MP_L = w.$$

The MP_N is the firm's labor demand curve.

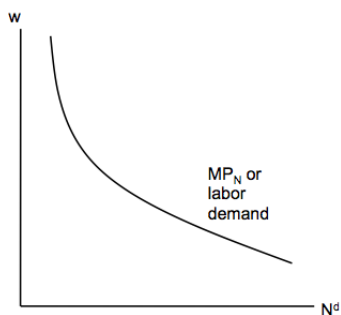
Slope of Y = slope of wN^d ;



Profit Maximization

- Y = revenue;
- MP_N = marginal revenue;
- wN^d = variable cost;
- w = marginal cost;
- Profit = $Y - wN^d$;
- Max profit = AB where $MP_N = w$.
- $N^* = N^d$ for the given w
- As $w \uparrow$, Max profit : $MP_{N^*} = w$, $MP_{N^*} \uparrow$, $N^* \dots\dots\dots$
- As $w \uparrow$, $N^d \dots\dots\dots$
- Profit-max: the firm hires labor up to the point where $MP_N = w$.

- What will happen to N^d if $z \uparrow$? What will happen to N^d if $K \uparrow$?



- An increase in K causes MP_N to rise for all levels of N .
- Profit-max: the firm hires labor up to the point where $MP_N = w$.
- For all levels of N^d , MP_N and w
- labour demand increases for all w
- (or in other words, for all levels of labor employed, the real wage the firm is willing to pay increases.)