

Perfect Competition

- 1) Many buyers and many sellers. - no single buyer or seller can have any effect on price by buying or selling more or less.
 - 2) Homogeneous product.
- each seller produces essentially the same product that is perfect substitute for others' output.
 - 3) Every firm has the same technology (i.e. production function) $Q = f(L, K)$
 - 4) every buyer + seller is price taker. the same access to $L + K$ at the same prices of $w + r$. (same input quality)
 - 5) Full Efficiency.
 - 6) Free Entry and Exit to the market.
- Every firm has the same cost curves.

Every firm wants to maximize profit.

$$\text{Total Profit} = \text{Total Revenue} - \text{Total Cost.}$$

$$\Pi(Q) = TR(Q) - TC(Q)$$

Note If we are producing in Short Run

$$TC(Q) = TFC(Q) + TVC(Q)$$

In perfect competition, every firm wants to

$$\max_Q \Pi(Q) = TR(Q) - TC(Q)$$

Calculus: $\max_x f(x) = 5 + 16x - x^2$

$$f'(x^*) = \frac{d f(x^*)}{dx} = 16 - 2x^* = 0, x^* = 8 - \text{critical point.}$$

$$\frac{d f(x)}{dx} = 16 - 2x$$

$$\frac{d^2 f(x)}{dx^2} = \frac{d}{dx} \left(\frac{d f(x)}{dx} \right) = -2$$

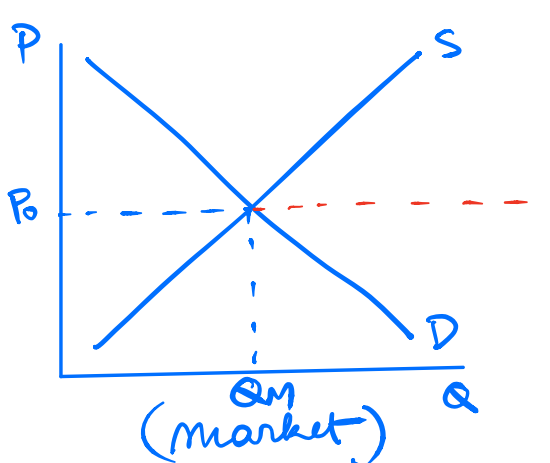
$$\text{so at } x^* \quad \frac{d^2 f(x^*)}{dx^2} = -2 < 0$$

By sufficient conditions.

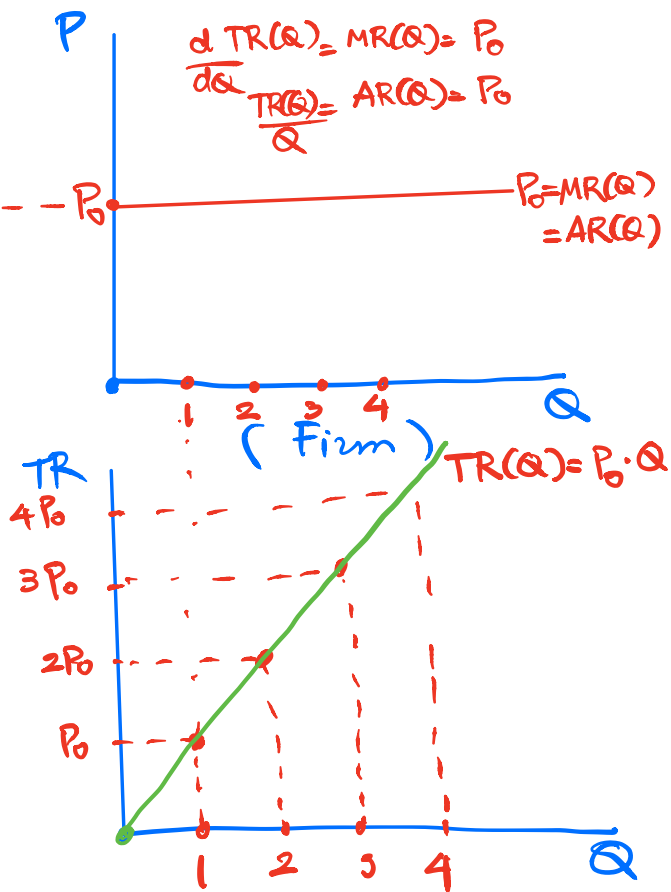
$$\left. \begin{array}{l} \text{1st order suff.} \\ \text{2nd order suff. 1)} \end{array} \right\} \begin{array}{l} f'(x^*) = 0 \\ f''(x^*) < 0 \end{array} \Rightarrow x^* \text{ is max.}$$

Necessary Conditions

$$x^* \text{ is max} \Rightarrow \begin{array}{l} 1) f'(x^*) = 0 \\ 2) f''(x^*) \leq 0. \end{array}$$



Market Equilibrium is at price = P_0 and total market output (consumption) = Q_M .



$$\max_Q \pi(Q) = TR(Q) - TC(Q)$$

1st-order suff. condition.

$$\frac{d\pi(Q)}{dQ} = \frac{dTR(Q)}{dQ} - \frac{dTC(Q)}{dQ}$$

$$\begin{aligned} \pi'(Q^*) &= TR'(Q^*) - TC'(Q^*) \\ &= MR(Q^*) - MC(Q^*) = 0 \end{aligned}$$

at critical point Q^* we have \Rightarrow $MR(Q^*) = MC(Q^*)$

Check 2nd-order suff. condition at Q^*

$$\pi''(Q^*) = \frac{d}{dQ} MR'(Q^*) - \frac{d}{dQ} MC(Q^*) < 0$$

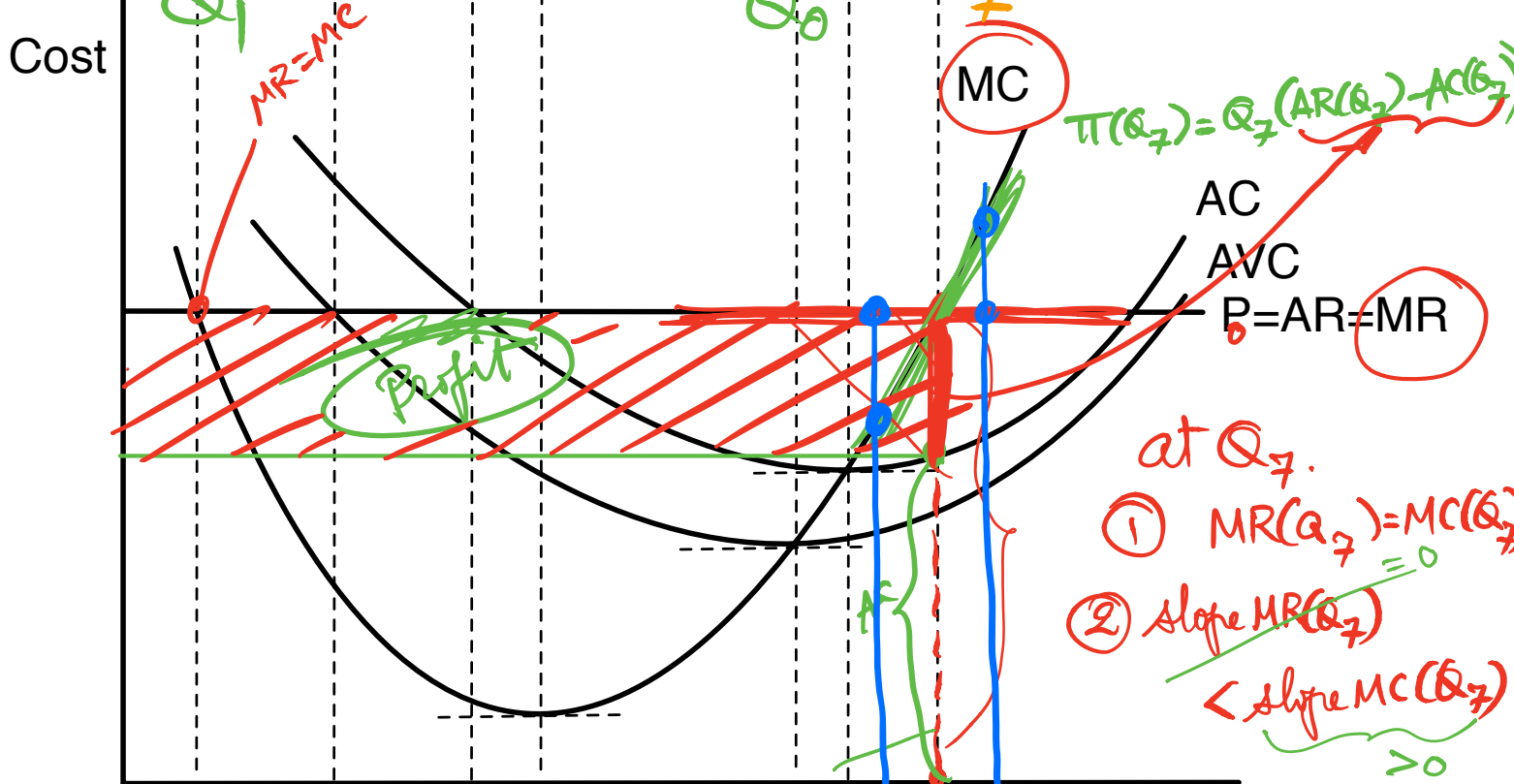
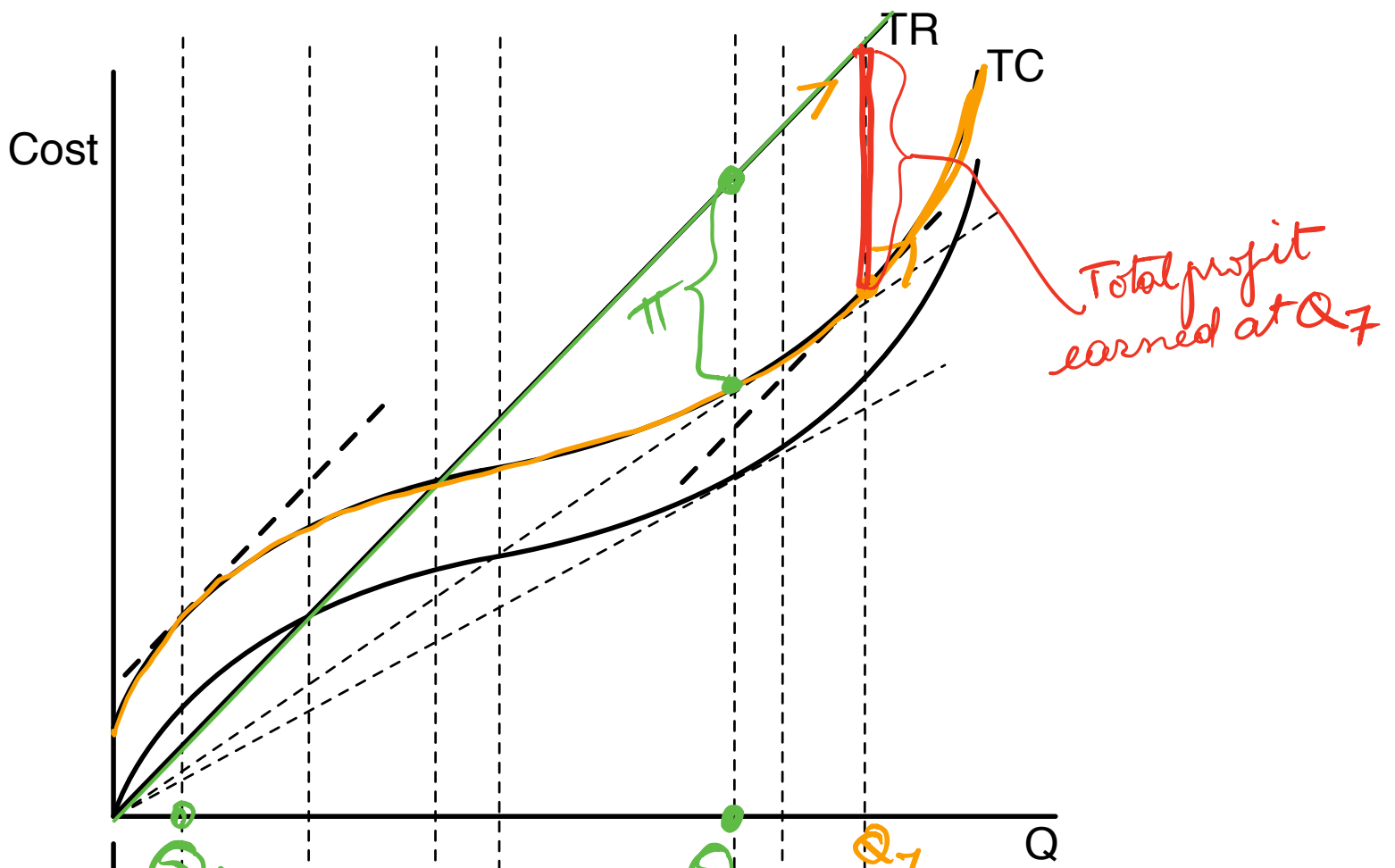
\Rightarrow slope of MR < slope of MC at Q^*

\therefore We can conclude that Q^* maximizes profit if

$$\left. \begin{array}{l} 1) \quad MR(Q^*) = MC(Q^*) \\ 2) \quad \frac{d}{dQ} MR(Q^*) < \frac{d}{dQ} MC(Q^*) \\ \quad \quad (\text{slope } MR < \text{slope } MC) \text{ at } Q^* \end{array} \right\} \text{Equilibrium Conditions.}$$

Perfect Competition Equilibrium of a Firm in Short Run

$\pi = TR - TC$



- at Q_7 .
- ① $MR(Q_7) = MC(Q_7)$
 - ② $\text{slope } MR(Q_7) = 0$
 $< \text{slope } MC(Q_7) > 0$

q_1 q_2 q_3 q_4 q_5 q_6 q_7 q

at Q_1 $MR(Q_1) = MC(Q_1)$
 but $\text{slope } MR(Q_1) = 0 > \text{slope } MC(Q_1) < 0$ } Q_1 actually minimizes π

$$\begin{aligned}
 \pi(Q_7) &= TR(Q_7) - TC(Q_7) \\
 &= Q_7 \cdot AR(Q_7) - Q_7 AC(Q_7) \\
 &= Q_7 (AR(Q_7) - AC(Q_7)) \\
 &= Q_7 (\text{Average Profit}(Q_7))
 \end{aligned}$$

H.W. Why does the firm not produce at the quantity that maximizes average profit?

$$\text{Average profit} = AR(Q) - AC(Q)$$

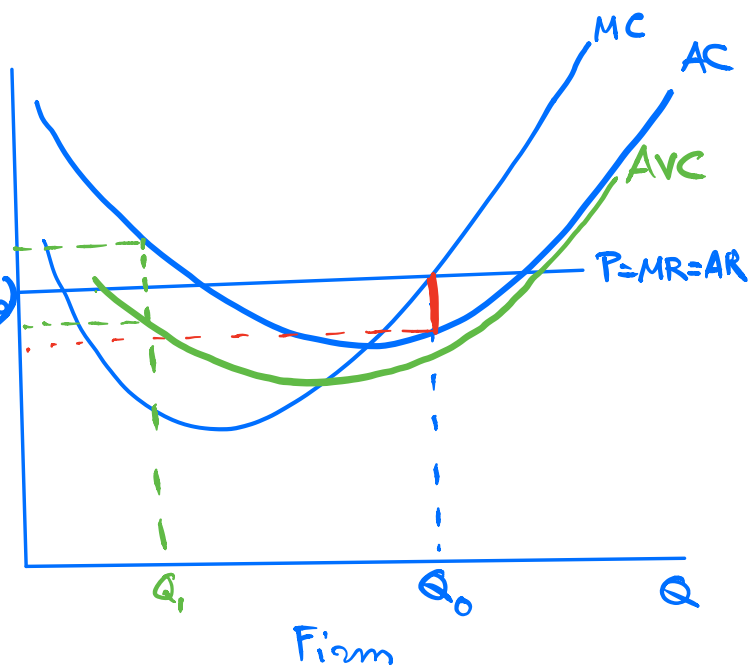
SR Equilibrium

at Q_0 because

- 1) $MR(Q_0) = MC(Q_0)$
- 2) $\text{slope } MR(Q_0) < \text{slope } MC(Q_0)$

Average profit at Q_0
 $= AR(Q_0) - AC(Q_0)$

At Q_0 , total profit.
 $= (AR(Q_0) - AC(Q_0)) \cdot Q_0$

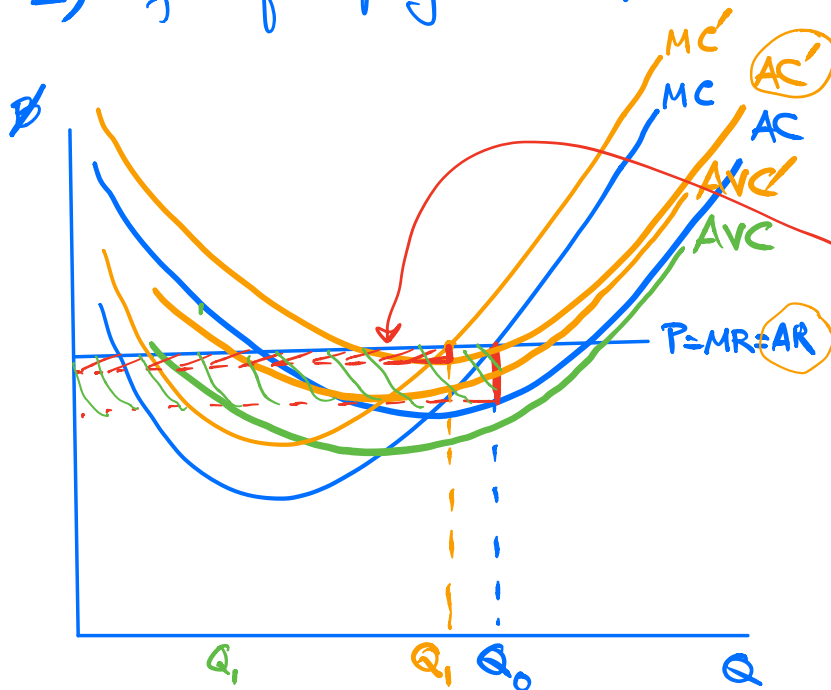


Note. The firm does not necessarily max profit at quantity where AC is minimum

- at any Q , $AFC(Q) = AC(Q) - AVC(Q)$

Application

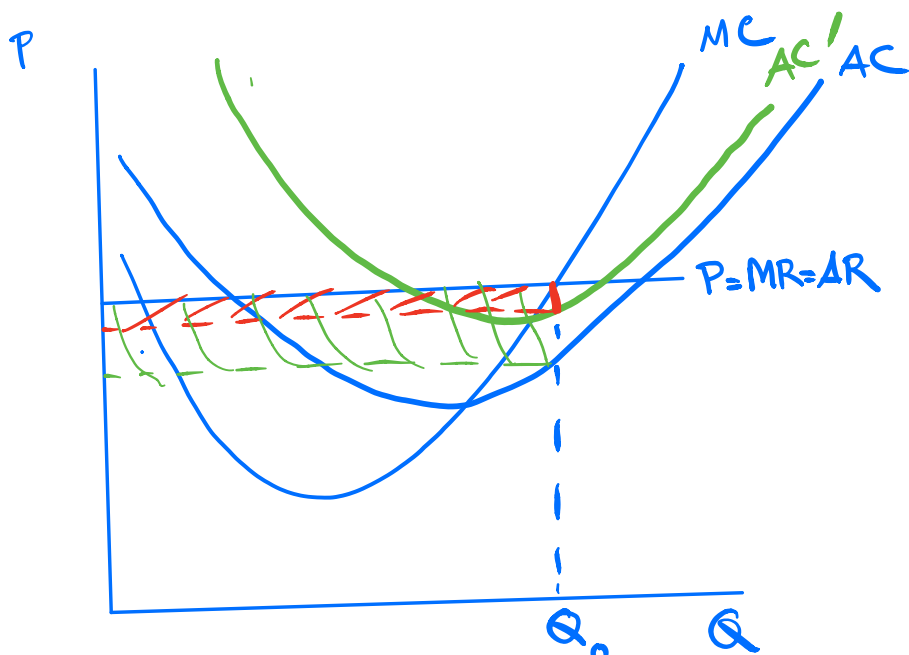
1) If the firm pays tax 10\$ / unit.



- Firm produces less at Q_1 , where
 1) $MR(Q_1) = MC'(Q_1)$
 2) $\text{slope } MR(Q_1) < \text{slope } MC'(Q_1)$
 Less profit.

HW. The tax can be so high that the firm is making a loss in SR. Show this and explain why the firm does not shut down in SR.

2.) Increase in Fixed Cost. - Rent, License Fees.



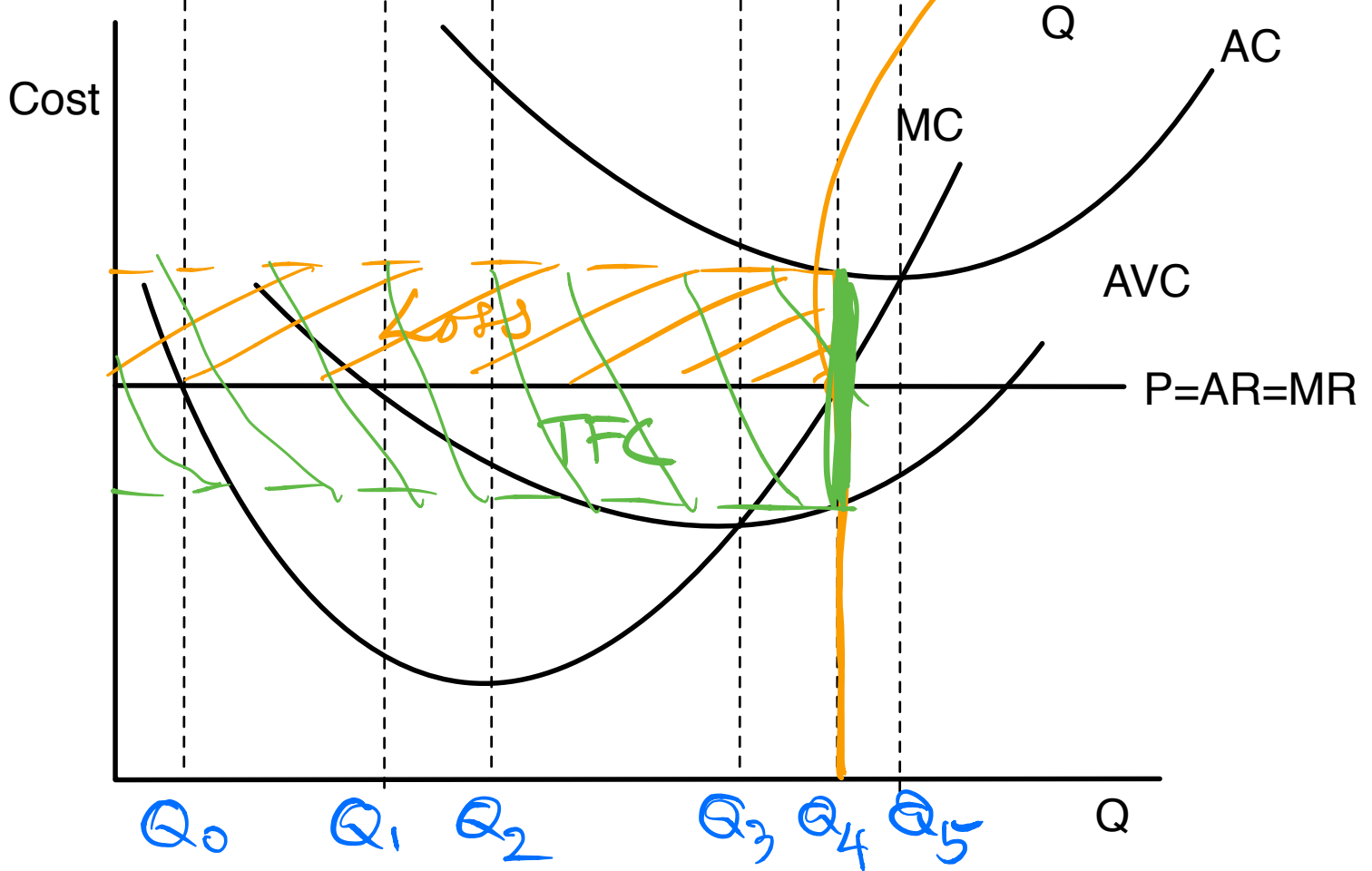
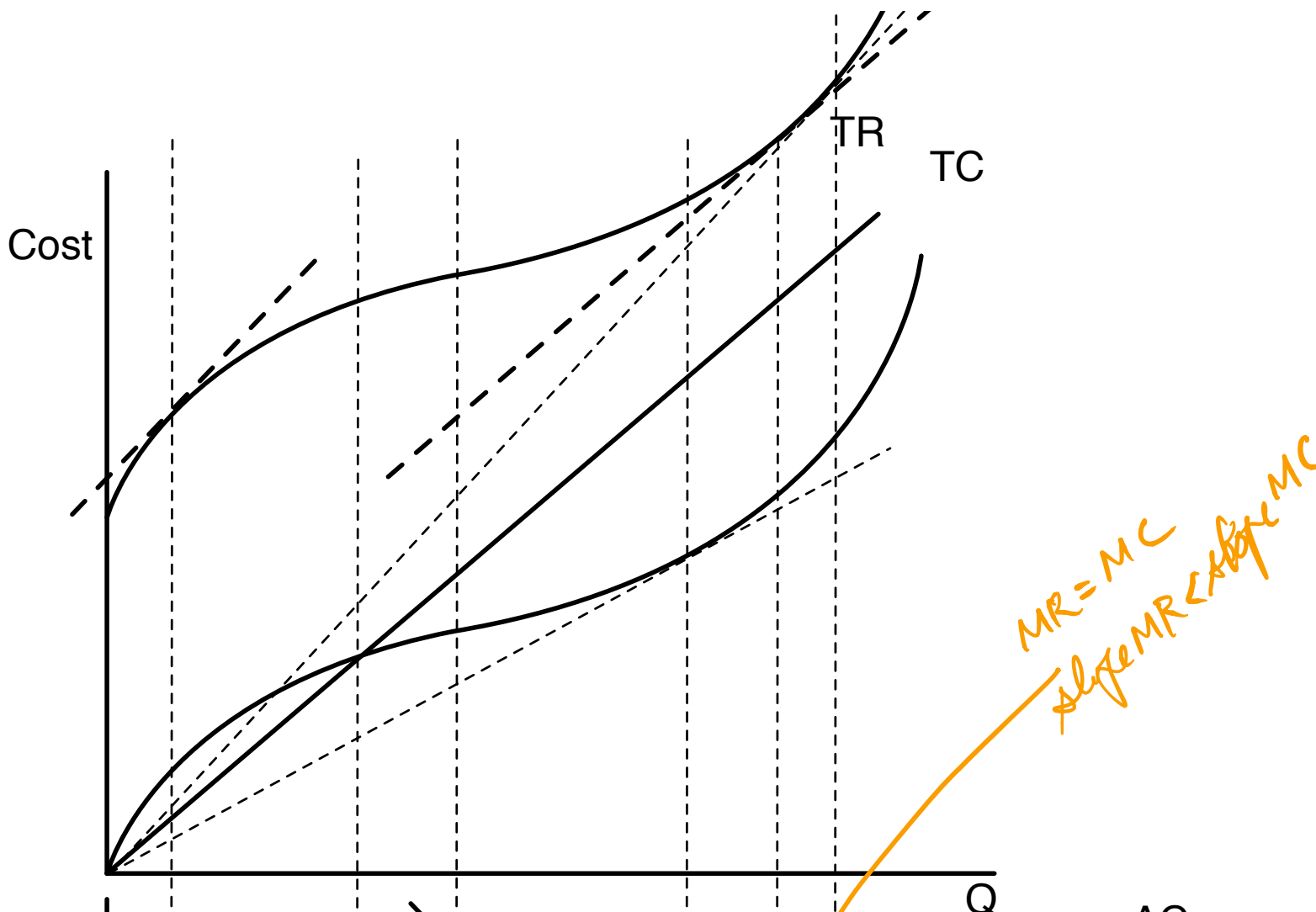
Before increase in Rent, Q_0 is the eq.
 Higher rent does not change MC. so Q_0 remains the
 equilibrium. - but less profit.

Shut-Down Point in S.R.

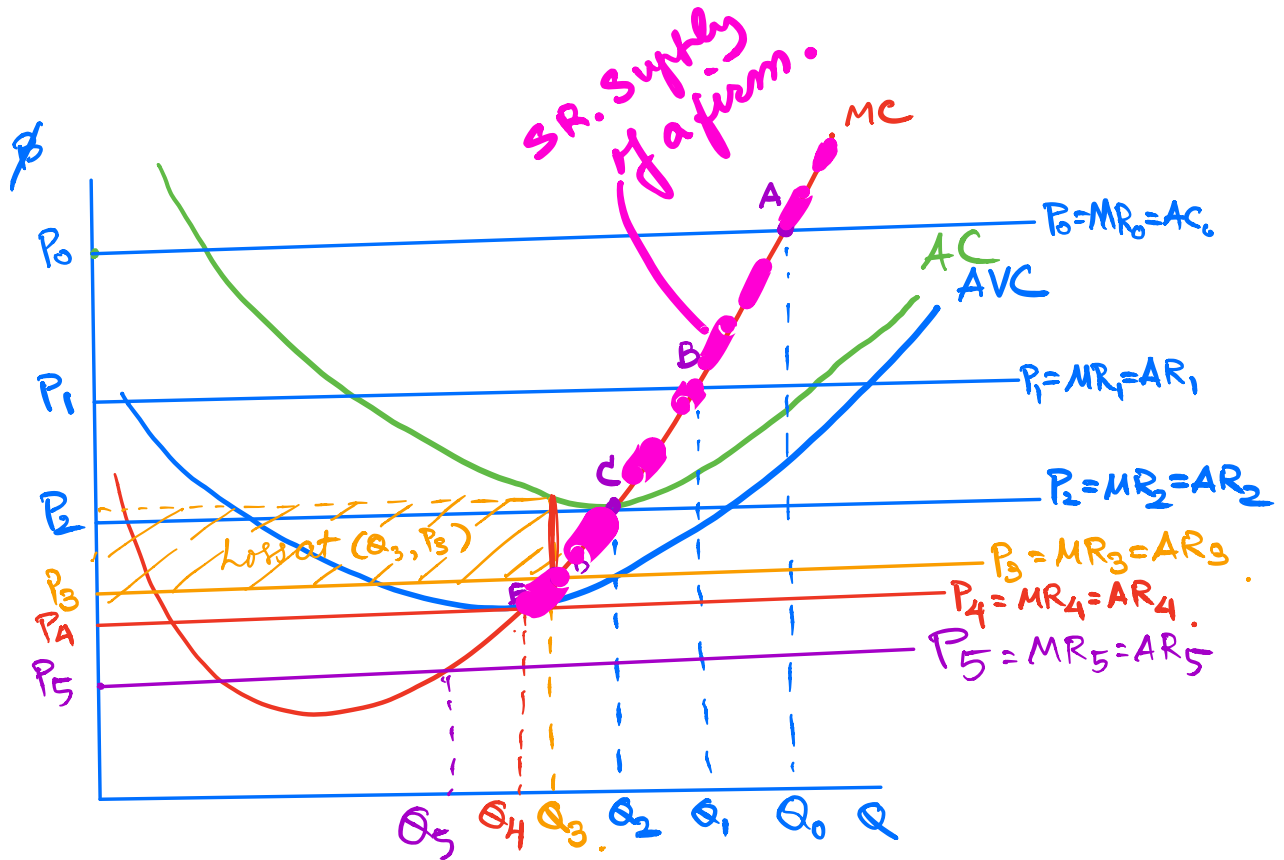
- In SR, even the firm is making a loss, the firm might still want to continue operating.

If shut-down - pays TFC.

∴ Continue if $LOSS < TFC$



Loss - but continue to produce at Q_4 .
because $LOSS < TFC$



Lower price \Rightarrow 1) Lower Q
 2) Lower Π .

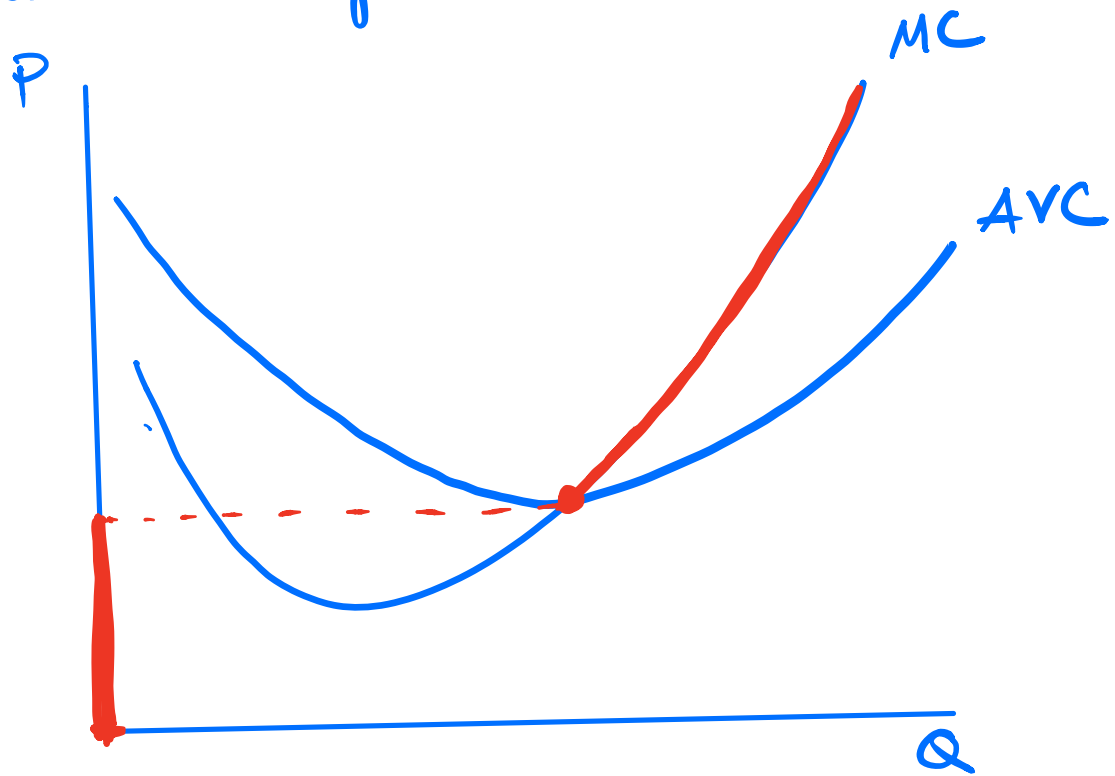
At Q_1 and price $P_2 \Rightarrow$ Break-even - Profit = 0.

At Q_3 , $P_3 \Rightarrow$ Loss < TFC \Rightarrow continue.

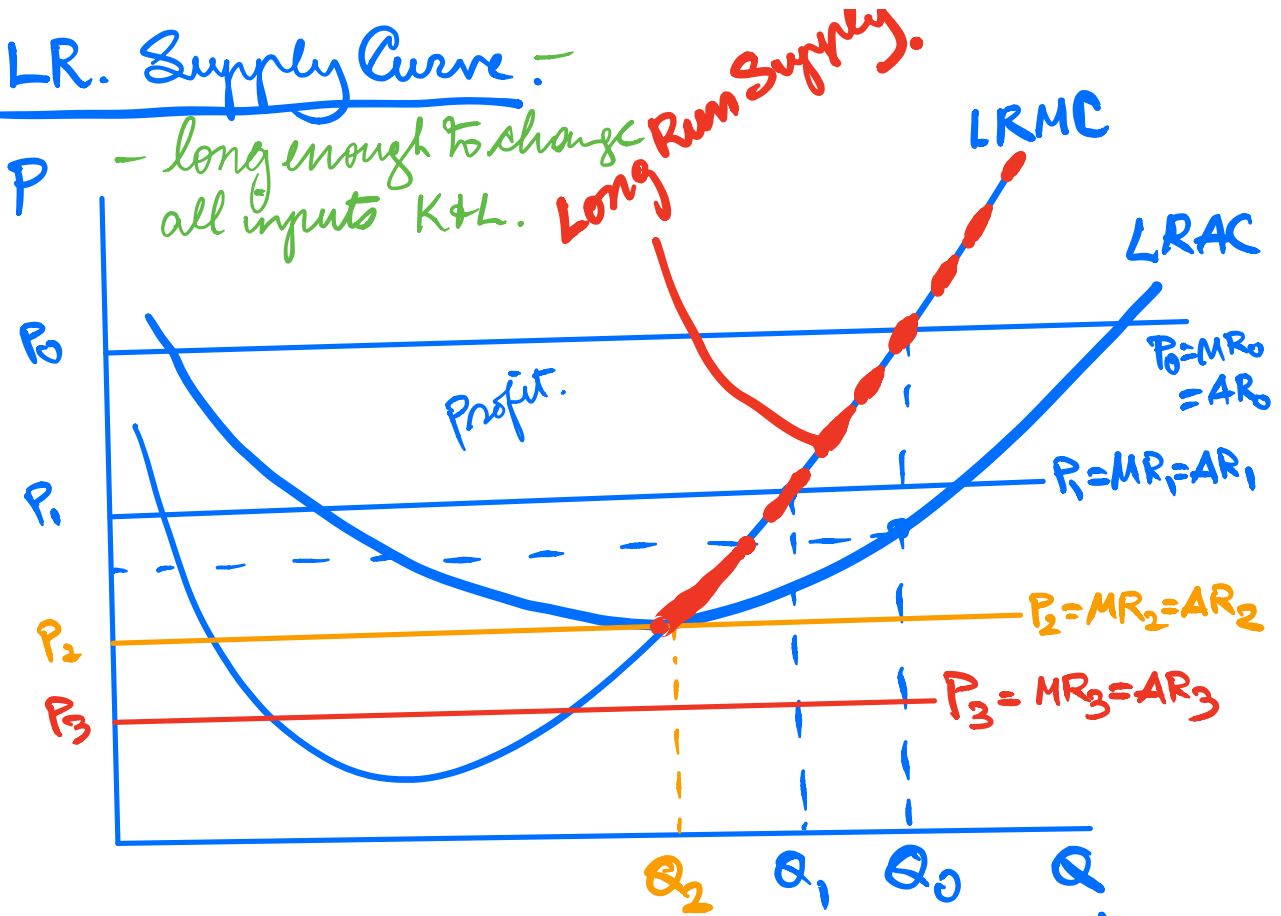
At Q_4 , $P_4 \Rightarrow$ Loss = TFC \Rightarrow Shut down point

At Q_5 , P_5 - Loss > TFC - Shut down.

S.R. Supply curve is MC from the minimum of AVC, and quantity supplied will be 0 for any price lower than min of AVC



LR. Supply Curve:-



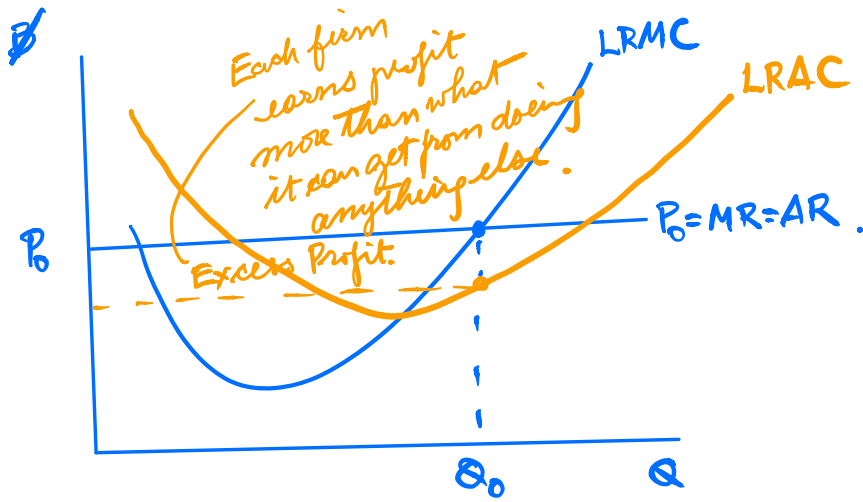
Lower price \Rightarrow Lower Q and have lower profit
 at P_2 and Q_2 - profit = 0
 at P_3 and Q_3 - Loss - Shut down.

In L.R if the cost also includes the oppcost of each firm

oppcost = profit or earning each firm can get from the next best thing it can do.

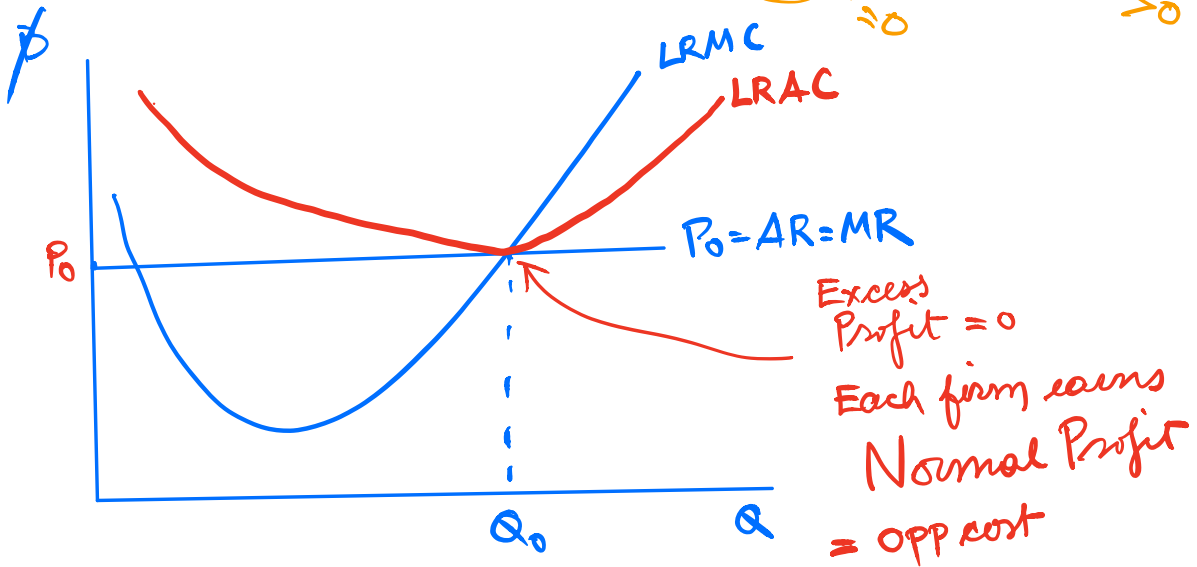
\therefore Given a price P_0 , if the firm receives

positive profit \Rightarrow Excess Profit.



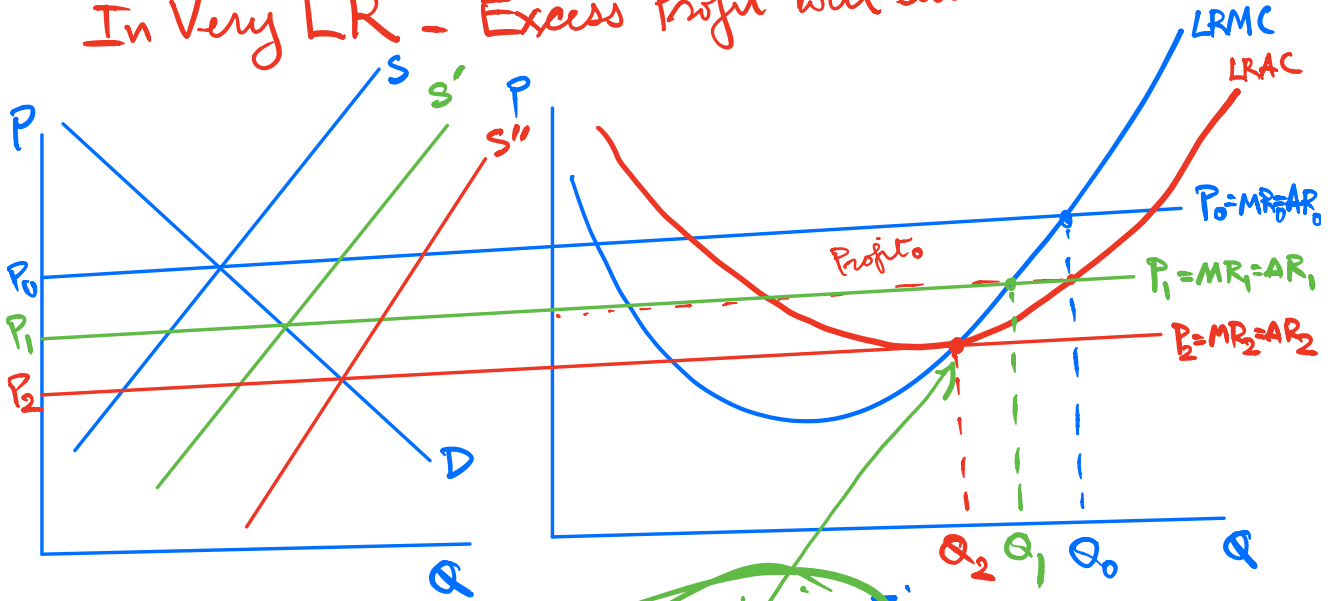
Eq at (Q_0, P_0) because

- 1) $MR(Q_0) = LRMC(Q_0)$
- 2) $\underbrace{\text{slope } MR(Q_0)}_{=0} < \underbrace{\text{slope } LRMC(Q_0)}_{>0}$



Equilibrium in LR - Long enough to change all inputs
and in Very LR - long enough that new firms can enter the market.

In Very LR - Excess Profit will attract new comers.



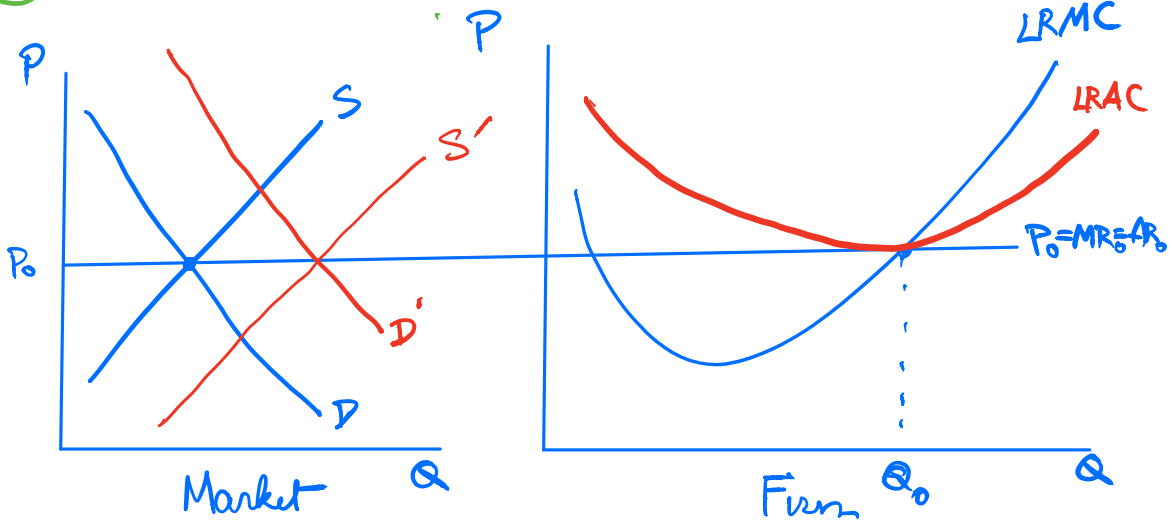
Market
 at P_0 , Excess Profit

- Supply increases from S to S' - but profit is still > 0
- Supply will increase until S'' so that P is P_2 and each firm produces Q_2 where LRAC is min. and Excess profit = 0 \Rightarrow Normal Profit.

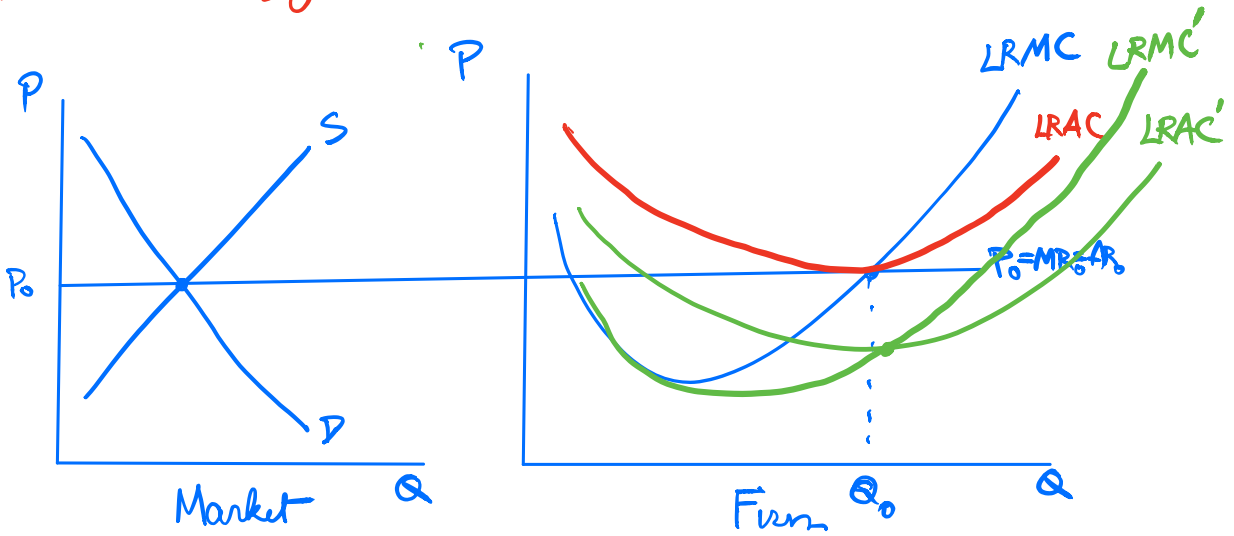
Equilibrium in Very LR Firm

Applications.

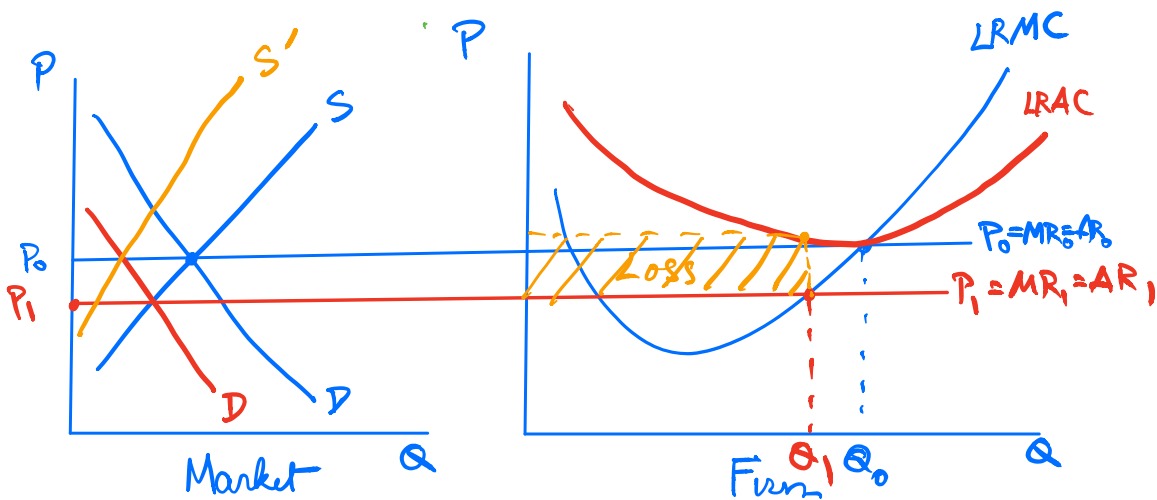
① D increases



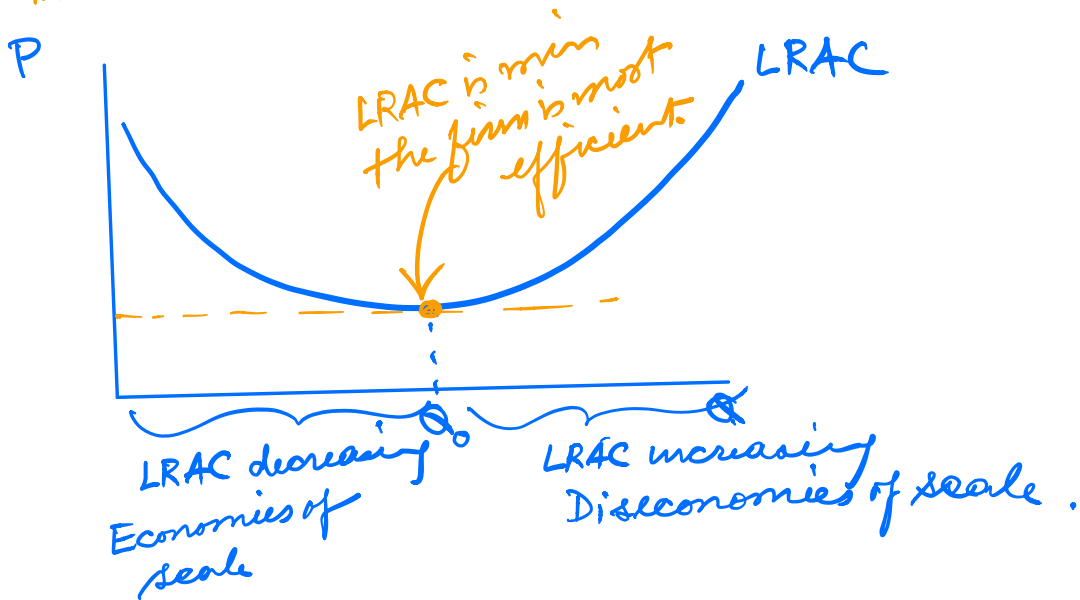
2) Technology Improves.



8) Demand Decreases.



Price returns to P₀ where LRAC is min.



Perfect Competition in Very LR

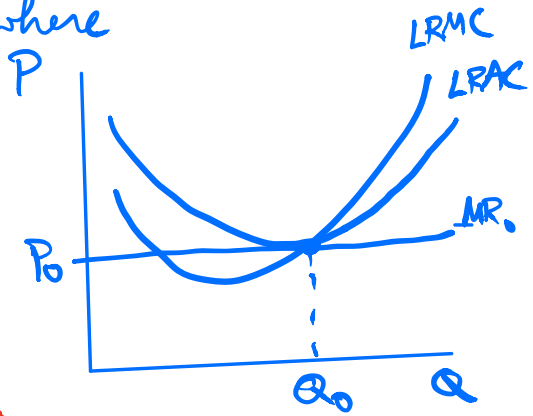
The equilibrium will be where

1) $P_0 = LRMC = MR$

and slope $MR < \text{slope } MC$.

where $LRAC$ is min.

i.e. every firm produces at Q_0 where it is most efficient

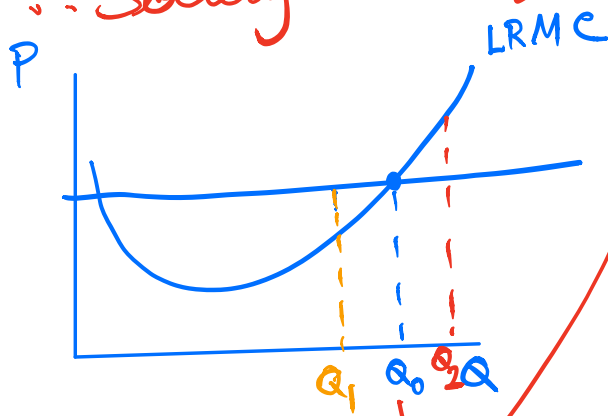


2) $P_0 = LRMC(Q_0)$

Value of last unit sold.

Cost of producing the last unit.

∴ Society maximizes the Social Welfare.



Efficiency in the distribution of resources of society to maximize social welfare.