

3. Suppose the price elasticity of demand for heating oil is 0.2 in the short run and 0.7 in the long run.

- a. If the price of heating oil rises from \$1.80 to \$2.20 per gallon, what happens to the quantity of heating oil demanded in the short run? In the long run? (Use the midpoint method in your calculations.)
- b. Why might this elasticity depend on the time horizon?

a. short run

$$\eta_D = 0.2$$

$$\begin{aligned}\% \Delta P &= \frac{P_1 - P_0}{(P_1 + P_0)/2} \times 100 \\ &= \frac{2.2 - 1.8}{2} \times 100 \\ &= 20\%\end{aligned}$$

$$\text{from midpoint method; } \eta_D = \frac{\% \Delta Q_D}{\% \Delta P}$$

$$\begin{aligned}0.2 &= \frac{\% \Delta Q_D}{20\%} \\ \% \Delta Q_D &= 0.2 \times \frac{20}{100}\end{aligned}$$

$$\% \Delta Q_D = 0.04$$

long run

$$\eta_D = 0.7$$

$$\begin{aligned}\% \Delta P &= \frac{P_1 - P_0}{(P_1 + P_0)/2} \times 100 \\ &= \frac{2.2 - 1.8}{2} \times 100 \\ &= 20\%\end{aligned}$$

$$\text{from midpoint method; } \eta_D = \frac{\% \Delta Q_D}{\% \Delta P}$$

$$\begin{aligned}0.7 &= \frac{\% \Delta Q_D}{20\%} \\ \% \Delta Q_D &= 0.7 \times \frac{20}{100}\end{aligned}$$

$$\% \Delta Q_D = 0.14$$

b. More time create more elasticity because people can find things to use instead of the old one.

7. Suppose that your demand schedule for pizza is as follows:

Price	Quantity Demanded (income = \$20,000)	Quantity Demanded (income = \$24,000)
\$8	40 pizzas	50 pizzas
10	32	45
12	24	30
14	16	20
16	8	12

- a. Use the midpoint method to calculate your price elasticity of demand as the price of pizza increases from \$8 to \$10 if (i) your income is \$20,000 and (ii) your income is \$24,000.
- b. Calculate your income elasticity of demand as your income increases from \$20,000 to \$24,000 if (i) the price is \$12 and (ii) the price is \$16.

a. $P_0 = 8, P_1 = 10$

(i) $Q_0 = 40, Q_1 = 32$

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{\Delta P}{\Delta Q} = \frac{10 - 8}{32 - 40} = \frac{-2}{-8} = \frac{1}{4}$$

from midpoint method; $\eta_D = \frac{1}{\text{slope}} \times \frac{P_1 + P_0}{Q_1 + Q_0}$

$$= \frac{1}{-1/4} \times \frac{10 + 8}{32 + 40}$$

$$= -4 \times \frac{18}{72} = -1$$

(ii) $Q_0 = 50, Q_1 = 45$

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{\Delta P}{\Delta Q} = \frac{10 - 8}{45 - 50} = \frac{-2}{-5} = \frac{2}{5}$$

from midpoint method; $\eta_D = \frac{1}{\text{slope}} \times \frac{P_1 + P_0}{Q_1 + Q_0}$

$$= \frac{1}{-2/5} \times \frac{10 + 8}{45 + 50}$$

$$= -\frac{5}{2} \times \frac{18}{95} = -\frac{9}{19}$$

b. (i) at $P = 12$

from $\eta_D = \frac{\% \Delta Q_D}{\% \Delta I} \rightarrow$ income elasticity of demand

$$= \frac{(Q_1 - Q_0)/Q_0 \times 100}{(I_1 - I_0)/I_0 \times 100}$$

$$= \frac{Q_1 - Q_0}{I_1 - I_0} \times \frac{I_0}{Q_0}$$

$$= \frac{30 - 24}{24000 - 20000} \times \frac{20000}{24}$$

$$= \frac{6}{4000} \times \frac{20000}{24} = 1.25$$

(ii) at $P = 16$

from $\eta_D = \frac{\% \Delta Q_D}{\% \Delta I}$

$$= \frac{(Q_1 - Q_0)/Q_0 \times 100}{(I_1 - I_0)/I_0 \times 100}$$

$$= \frac{Q_1 - Q_0}{I_1 - I_0} \times \frac{I_0}{Q_0}$$

$$= \frac{12 - 8}{24000 - 20000} \times \frac{20000}{8}$$

$$= \frac{4}{4000} \times \frac{20000}{8} = 2.5$$