

Thursday, November 10, 2016 11:55 AM

Product differentiation

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Topic 7. Product differentiation: patterns of price setting

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2. Horizontal *versus* vertical product differentiation
3. The linear city model
4. Applications: Coca-Cola *versus* Pepsi-Cola
5. Conclusions

1. Introduction

- **Aim:** To study an oligopoly model relaxing the homogeneous product assumption, to analyse the effect of product differentiation on price competition intensity and product choice.

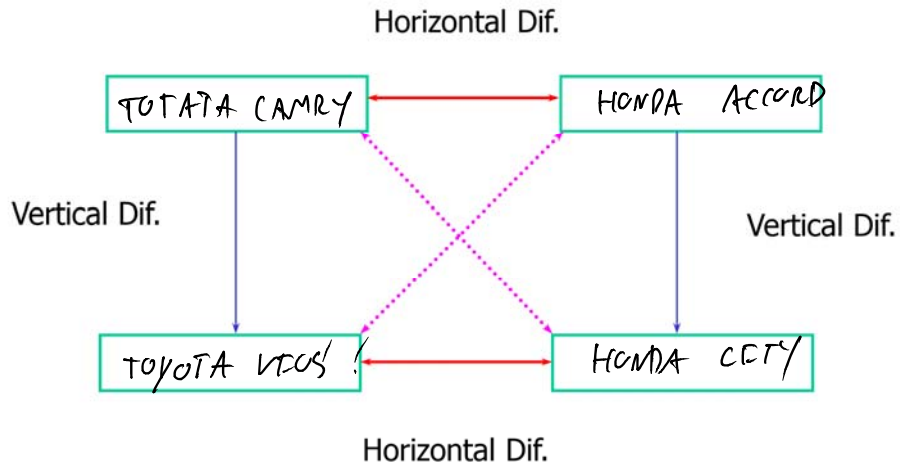
- Main implication of the homogeneous product assumption in an oligopoly model of price competition (*à la Bertrand*)
 - Bertrand paradox → Price competition between two firms is a sufficient condition to restores the competitive situation

$$p = c$$

2. Horizontal and vertical product differentiation

- **Horizontal product differentiation:** two products are differentiated horizontally if, when they are offered at the same price consumers **do not agree** on which is the preferred product.
Example:
- **Vertical product differentiation:** two products are differentiated vertically if, when they are offered at the same price consumers **agree** on which is the preferred product.
 - Example:

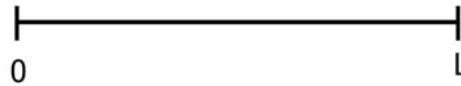
Example



HOTELLING (1929)

3. Linear city model with linear transport costs : assumptions

- Consumers are uniformly distributed with unit density along a segment of L length



- Two firms (firms 1 and 2) are located along the segment
 - The two firms sell a product that is identical except for the location of the firm.
 - The two firms have constant and identical marginal cost $c \rightarrow c_1 = c_2 = c$
 - Each consumer buys a single unit of the product.
- Alternative interpretation of the segment as a product characteristic

3 Linear city model with linear transport costs : two-stage game

Stage 1: the two firms choose simultaneously their location (long-run decision)

Stage 2: the two firms choose simultaneously their prices (short-run decision)

We impose maximum product differentiation and so we focus on the determination of the *Nash equilibrium in prices* (Stage 2).



3. Linear city model with linear transport costs : consumers' utility function

- The utility that a consumer i located in X obtains from the purchase of the good of firm j is given by:

$$U_{ij} = r - p_j - t x_{ij}$$

r : reservation price

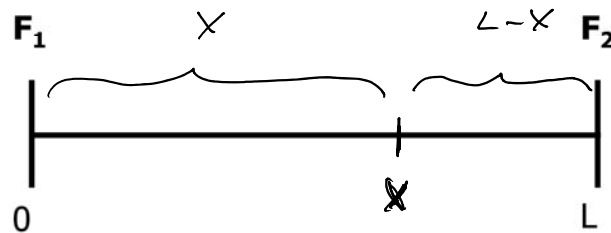
p_j : price of the product of firm j

x_{ij} : distance (along the segment) between the location of consumer i and the location of firm j

t : transport cost per unit of distance (or alternatively intensity of the preference for a given product)

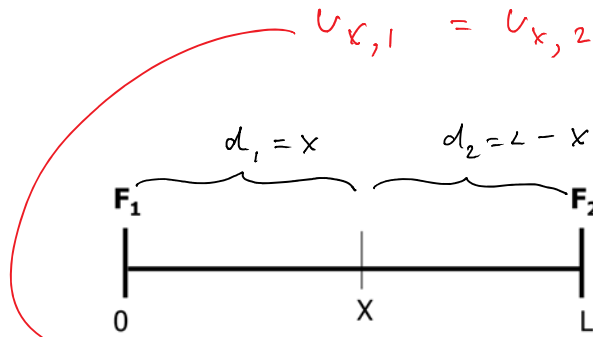
3 Linear city model with linear transport costs : transport costs

- With linear transport costs per unit of distance :



- Transport cost if the product is bought at firm 1 = $t \cdot X$
- Transport cost if the product is bought at firm 2 = $t \cdot (L - X)$
- Total cost of the product = price + transport costs
 - Total cost if the product is bought at firm 1 = $p_1 + t \cdot X$
 - Total cost if the product is bought at firm 2 = $p_2 + t \cdot (L - X)$

3 Linear city model with linear transport costs : demands determination



$$\cancel{x - p_1 - t \cdot x} = \cancel{x - p_2 - t(L - x)}$$

$$p_1 + tx = p_2 + t(L - x)$$

$$\text{so } d_1 = x = \frac{p_2 - p_1}{2t} + \frac{L}{2} \quad \rightarrow \text{DEMAND FUNCTION FOR FIRM 1}$$

$$d_2 = L - x = \frac{p_1 - p_2}{2t} + \frac{L}{2} \quad \rightarrow \text{DEMAND FUNCTION FOR FIRM 2}$$

3 Linear city model with linear transport costs : demand properties

- Price elasticity of demand

$$\eta = \frac{\partial d_1}{\partial p_1} \frac{p_1}{d_1} = -\frac{p_1}{p_2 - p_1 + Lt} < 0$$

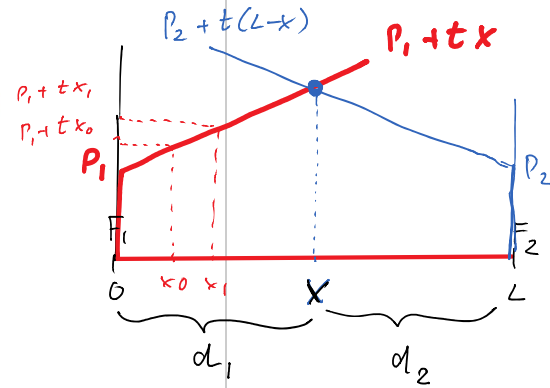
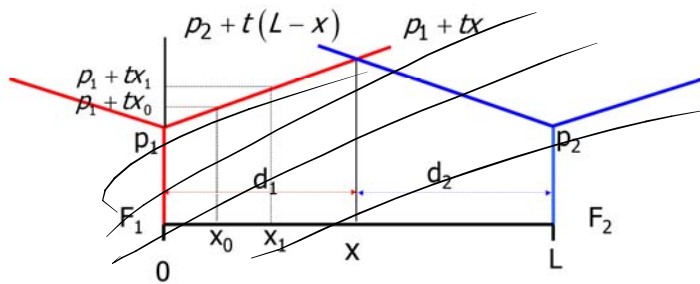
- Price elasticity of demand and transport costs

$$\frac{\partial |\eta|}{\partial t} = -\frac{Lp_1}{(p_2 - p_1 + Lt)^2} < 0$$

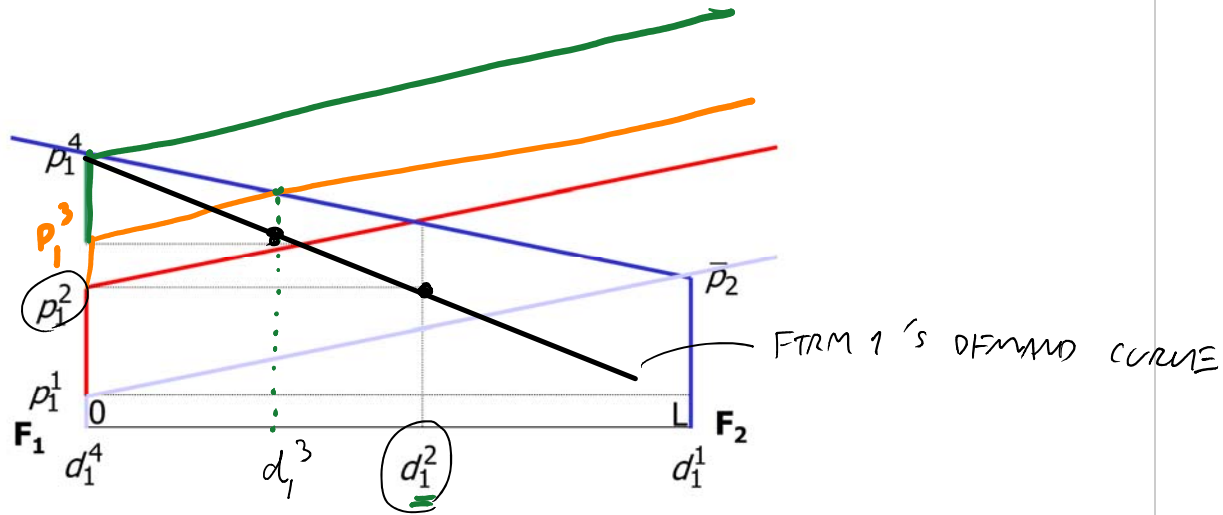
3 Linear city model with linear transport costs : demands determination

- Total cost of buying at 1 = Total cost of buying at 2

$$p_1 + tx = p_2 + t(L - x)$$



3 Linear city model with linear transport costs : **firm 1 demand**



3 Linear city model with linear transport costs : Obtaining the Nash equilibrium in prices (I)

- Maximization problem of firm 1

$$\max_{p_1} \pi_1 = d_1(p_1 - c) = \left[\frac{p_2 - p_1}{2t} + \frac{L}{2} \right] \cdot (p_1 - c)$$

$$\text{F.O.C : } \frac{\partial \pi_1}{\partial p_1} = \frac{p_2 - 2p_1 + c}{2t} + \frac{L}{2} = 0$$

- Maximization problem of firm 2

$$\max_{p_2} \pi_2 = d_2(p_2 - c) = \left[\frac{p_1 - p_2}{2t} + \frac{L}{2} \right] \cdot (p_2 - c)$$

$$\text{F.O.C : } \frac{\partial \pi_2}{\partial p_2} = \frac{p_1 - 2p_2 + c}{2t} + \frac{L}{2} = 0$$

$$p_1^*(p_2) = \frac{p_2 + Lt + c}{2} \quad : \text{ BR FUNCTION OF FIRM 1}$$

$$p_2^*(p_1) = \frac{p_1 + Lt + c}{2} \quad : \text{ BR FUNCTION OF FIRM 2}$$



3 Linear city model with linear transport costs : Obtaining the Nash equilibrium in prices (II)

- Solving the system of equations given by the two reaction functions we obtain the price equilibrium: (given locations)

$$P_1^c = P_2^c = Lt + c$$

- Profits for both firms are:

$$\pi_1 = \pi_2 = \frac{1}{2} L^2 \cdot t$$

