

GAINS FROM VERTICAL INTEGRATION

- ① LOWER TRANSACTION COSTS
- ② ASSURE THE SUPPLY OF IMPORTANT INPUTS (BACKWARD VI)
- ③ ELIMINATE NEGATIVE EXTERNALITIES

EX: MCDONALD / BURGER KING OWNS UPSTREAM FIRMS TO ENSURE THAT ITS REPUTATION WILL NOT BE AFFECTED BY ANY MISTAKES THAT MIGHT OCCUR IN THE SUPPLY CHAIN IF IT IS NOT VERTICALLY INTEGRATED.

- ④ AVOID GOVERNMENT REGULATION / RULE

EX: PRICE CONTROLS
STEEL FIRM ← CAR MANUFACTURERS

SUPPOSE GOVT IMPOSE PRICE FLOOR ON STEEL; A LEGALLY MINIMUM PRICE STEEL FIRM MUST GET WHEN IT SELLS

TO AVOID THIS REGULATION, CAR MANUFACTURERS MAY TAKE OVER STEEL FIRM. (SELLING STEEL TO ITSELF)

- ⑤ INCREASE MONOPOLY PROFITS FOR A VERTICALLY INTEGRATED FIRM,
- ⑥ REDUCE OR ELIMINATE MARKET POWER (OF BIG FIRMS).

A GROUP OF SMALL FIRMS MAY DO VI TO REDUCE THE BIG FIRMS' MARKET POWER.

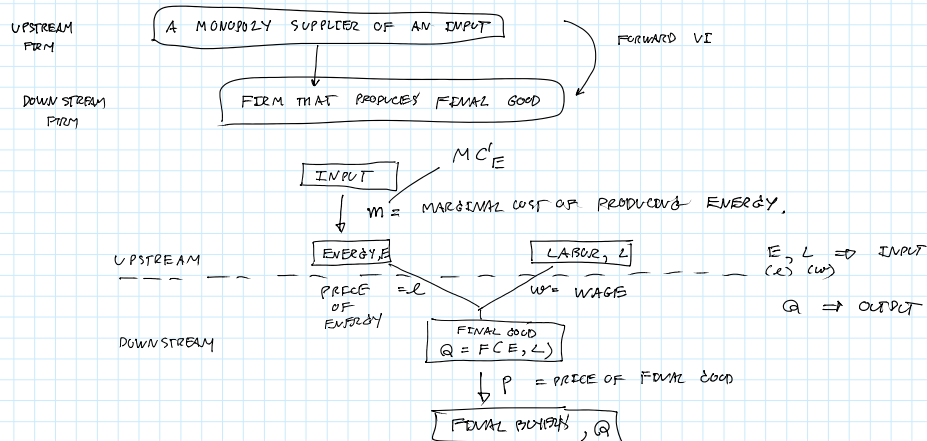
COSTS OF VERTICAL INTEGRATION

- LEGAL COSTS OF MERGERS MAY BE HIGH.
- LARGE FIRMS ARE HARDER TO MANAGE.
- COSTS MAY BE HIGHER THAN THE CASE YOU JUST BUY INPUTS FROM COMPETITIVE SUPPLIERS.

BOTTOM LINE

IF BENEFIT FROM VI > COSTS OF VI, FIRMS ARE VERTICALLY INTEGRATED.

OTHERWISE, THEY WILL NOT DO SO.

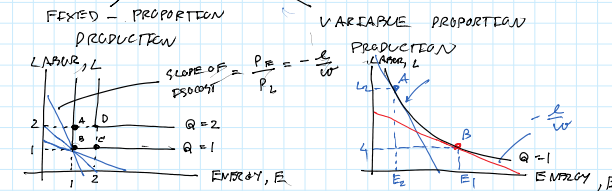
VERTICAL INTEGRATION TO MONOPOLIZE ANOTHER INDUSTRYASSUMPTIONS

- ① CONSTANT RETURNS TO SCALE: DOUBLING ALL INPUTS DOUBLES OUTPUT.
- ② CONSTANT MARGINAL COST OF INPUTS: $\bar{m}, \bar{w}$
- ③ UPSTREAM FIRM $\Rightarrow$ MONOPOLY
DOWNSTREAM FIRM $\Rightarrow$ COMPETITIVE FIRM (WE RELAX THIS ASSUMPTION LATER)
- ④ VERTICAL INTEGRATION IS COSTLY.

KEY POINT

MONOPOLY UPSTREAM WILL ENJOY HIGHER PROFITS

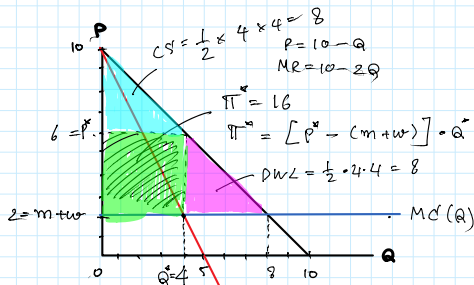
FROM VERTICALLY INTEGRATED W/ COMPETITIVE
DOWNSTREAM OR NOT DEPENDS ON
PRODUCTION TECHNOLOGY OF COMPETITIVE DOWNSTREAM



FIXED - PROPORTION PRODUCTION
LABOR, L
SLOPE OF ISOCOST = $\frac{P_E}{P_L} = -\frac{L}{E}$
ENERGY, E
A(1,2) → Q=1
B(1,1) → Q=1
C(2,1) → Q=1
D(2,2) → Q=2
TWO INPUTS MUST BE USED
IN THE SAME FIXED PROPORTION: 1:1

CASE1 FIXED PROPORTION PRODUCTION FUNCTION

(a) PROFITS OF AN INTEGRATED FIRM



DEMAND FUNCTION FACING BY COMPETITIVE FIRM:

$$P = 10 - Q$$

$$\text{SUPPOSE } m = 1, w = 1$$

$$Q = F(E, L)$$

SO MARGINAL COST OF PRODUCING A UNIT

$$\text{OF FINAL GOOD} = 1 \cdot 1 + 1 \cdot 1 = 2$$

SINCE 1E + 1L → 1Q.

$$\text{SOLVE: } P = 10 - Q \quad (P = a - bq)$$

$$TR = P \cdot Q = (10 - Q)Q = 10Q - Q^2$$

$$MR = \frac{dTR}{dQ} = 10 - 2Q, \quad (P = a - 2bq)$$

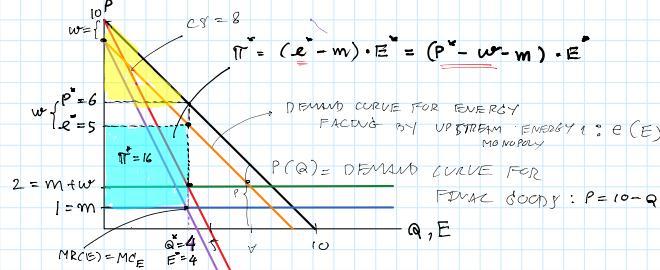
$$Q^* \Rightarrow MR = MC \Rightarrow 10 - 2Q = 2$$

$$Q^* = 4$$

$$P^* = 10 - Q^* = 10 - 4 = 6$$

$$\begin{aligned} \pi^* &= (P^* - AC) \cdot Q^* \\ &= (6 - 2) \cdot 4 \\ &= 16 \end{aligned}$$

(b) PROFITS OF UPSTREAM MONOPOLY
SUPPLYING ENERGY TO A
COMPETITIVE DOWNSTREAM



$$MR(Q) : P = 10 - 2Q$$

TO PRODUCE A UNIT OF GOOD,
A COMPETITIVE DOWNSTREAM FIRM
MUST SPEND w AMT + e AMT.
THE DOWNSTREAM GETS P AMT WHEN IT SELLS
WITH $P = MC$

$$P = e + w$$

$e = P - w \rightarrow$ THE HIGHEST PRICE OF E
AN OUTPUT FIRM IS WILLING TO PAY

NOTICE THAT IF PRICE OF ENERGY (e) RISES BY
1 AMT, THEN PRICE OF FINAL GOOD WILL
ALSO RISE BY 1 AMT.

EMULATION?

NON VERTICALLY INTEGRATED ENERGY
MONOPOLY TAKES FULL CONTROL
OVER THE MKT PRICE OF
FINAL GOOD.

$$P = 10 - Q, m = 1, w = 1$$

SUMMARY

- PRICE, P
- QUANTITY, Q
- CONSUMER SURPLUS
- PROFIT TO OWNER OF E
- DWL
- LOSS FROM INEFFICIENT PRODUCTION
- E
- L
- m

ALL MARKETS ARE COMPETITIVE

FIXED PROPORTION

NO VI

VI

6

4

8

16

8

0

0

4

4

5

1

$e = m$

OR $e > m$

VARIABLE PROPORTIONS

NO VI

VI

5.63

4.37

9.55

10.75

6.59

5.11

1.55

12.30

7.93

4

4

1

1

CASE2 VARIABLE - PROPORTIONS PRODUCTION FUNCTION

NOW, IF PRICE OF L IS RELATIVELY CHEAPER COMPARED
TO PRICE OF E , DOWNSTREAM COMPETITIVE FIRM
CAN SUBSTITUTE AWAY FROM A RELATIVELY EXPENSIVE
INPUT TO A RELATIVELY CHEAPER INPUT.

IN THIS CASE, ENERGY MONOPOLY CANNOT TAKE CONTROL

UP DOWNSTREAM FIRM FOR THE CHOICE OF USING INPUT MIX!
 THEREFORE, ENERGY MONOPOLY MAY WANT TO DO (E, L)
 FORWARD VI IN ORDER TO HAVE ABILITY TO CONTROL THE
 USE OF INPUTS CHOSEN BY DOWNSTREAM FIRM.

LET'S START OUR ANALYSIS!

COST FUNCTION FOR DOWNSTREAM FIRM:

$$C(e, w, Q) = \min_{E, L} e \cdot E + w \cdot L$$

$\swarrow$ PRICE OF ENERGY $\swarrow$ PRICE OF LABOR

PRODUCTION FUNCTION:

$$Q = E^{\frac{1}{2}} L^{\frac{1}{2}} \quad [\text{Cobb-Douglas Production Function}]$$

LET'S FIND DEMAND FUNCTION FOR E, CONDITIONAL ON
 FACTOR COSTS AND OUTPUT...

$$C(e, w, Q) = \min_{E, L} e \cdot E + w \cdot L$$

$$= \min_{E, L} e \cdot E + w \cdot \frac{Q^2}{E}$$

NOTE:

$$Q = E^{\frac{1}{2}} L^{\frac{1}{2}}$$

$$L^{\frac{1}{2}} = \frac{Q}{E^{\frac{1}{2}}} \text{ OR } \frac{Q}{\sqrt{E}}$$

$$\sqrt{L} = \frac{Q}{\sqrt{E}}$$

$$L = \frac{Q^2}{E}$$

- SOLVING FOR FOC TO OBTAIN THE DEMAND
 FUNCTION FOR E:

$$\frac{\partial C(e, w, Q)}{\partial E} = 0 \rightarrow E(e, w, Q) = Q \left(\frac{w}{e} \right)^{\frac{1}{2}}$$

- DEMAND FUNCTION FOR L:

$$\frac{\partial C(e, w, Q)}{\partial L} = 0 \rightarrow L(e, w, Q) = Q \left(\frac{e}{w} \right)^{\frac{1}{2}}$$

- SO, TOTAL COST $C(e, w, Q) = e \cdot E(e, w, Q) + w \cdot L(e, w, Q)$

$$= e \cdot Q \left(\frac{w}{e} \right)^{\frac{1}{2}} + w \cdot Q \left(\frac{e}{w} \right)^{\frac{1}{2}}$$

$$= \underline{\underline{2Q (w \cdot e)^{\frac{1}{2}}}}$$

- IF VERTICALLY INTEGRATED:

THE DOWNSTREAM FIRM WILL MAXIMIZE PROFITS BY
 PRODUCING Q WHERE $MR(Q^*) = MC'(Q^*)$

$$MR = MC'$$

$$a - 2bQ = 2w^{\frac{1}{2}} \cdot m^{\frac{1}{2}}$$

$$Q = \frac{(a - 2w^{\frac{1}{2}} m^{\frac{1}{2}})}{2b}$$

[NOTE: INVERSE
 DEMAND FUNCTION
 $P = a - bQ$]

"OUTPUT PRODUCED BY THE INTEGRATED FIRM"

USING THE SAME PARAMETERS ($a=10$, $b=1$, $m=1$, $w=1$)

WE WILL GET $Q^* = 4$ UNITS.

NOTE THAT

THE INTEGRATED FIRM W/ VARIABLE PRODUCTION
 FUNCTION PRODUCES THE SAME OUTPUT AS

WE FOUND IN THE CASE OF FIXED PROPORTION
 PRODUCTION FUNCTION.

- IF NO VERTICAL INTEGRATION:

THE DEMAND FOR E FACING UPSTREAM ENERGY MONOPOLY
 CAN BE DERIVED BY SETTING $P = MC'$:

$$P = 2w^{\frac{1}{2}} e^{\frac{1}{2}} \quad \text{AND THEN SOLVING FOR E:}$$

$$\text{SO } E = a \left(\frac{w}{e} \right)^{\frac{1}{2}} - 2w$$

UPSTREAM MONOPOLY MAXIMIZES PROFIT: $\frac{(e-m) \cdot E}{2}$

BY DOING F.O.C., WE GET

$$a w^{\frac{1}{2}} - 2 w \cdot e^{\frac{1}{2}} - \frac{1}{2} (e-m) \cdot a \cdot \left(\frac{w}{2}\right)^{\frac{1}{2}} = 0$$

USING THE SAME SET OF PARAMETERS,

- $e = 7.9265$

- MARGINAL COST = $2 w^{\frac{1}{2}} \cdot e^{\frac{1}{2}} = 2 (1)^{\frac{1}{2}} (7.9265)^{\frac{1}{2}} = 5.6308 = P$

- $Q = 10 - P = 10 - 5.6308 = 4.3692$

OUTPUT THAT DOWNSTREAM COMPETITIVE FIRM PRODUCES.

- NOTICE THAT

Q
w/o VI
w/ VARIABLE
PRODUCTION
FUNCTION

Q = 4 IN ALL CASES.

OBSERVATIONS

- ① W/ INTEGRATION, $e = m = 1 \Rightarrow E^* = L^* = Q^* = 4$
W/O INTEGRATION, IF $e \uparrow$, DOWNSTREAM WILL TRY TO DO SUBSTITUTION BY USING MORE L AND E. IF IT DOES SO, MARGINAL COST (MC) OF OUTPUT WILL NOT RISE AS MUCH AS THE INCREASE IN PRICE OF ENERGY (e)!

EX: $MC = 2 (w \cdot e)^{\frac{1}{2}} = 2 \cdot e^{\frac{1}{2}} \quad (\text{NOTE } w=1)$

e	$2 \cdot e^{\frac{1}{2}}$	
1	2	
2	$2 \cdot 2^{\frac{1}{2}} = 2.82$	41% INCREASE
4	$2 \cdot 4^{\frac{1}{2}} = 4.00$	41% INCREASE
8	$2 \cdot 8^{\frac{1}{2}} = 5.64$	41% INCREASE

MC RISES BY ONLY 41% IN RESPONSE TO 100% INCREASE TO PRICE OF ENERGY (e)

RECALL THAT E AND L ARE NO LONGER USED IN EQUAL PROPORTIONS!

- ② PRICE OF FINAL GOOD = 5.63 (W/O INTEGRATION)
WHICH IS CHEAPER THAN WHEN 2 FIRMS MERGE!
(P=6)

- ③ $C'S_{NO VI} > C'S_{VI}$
(= 9.55) > (= 8)
C'S IS HIGHER BY 19.375%

W/ VARIABLE PROPORTION PRODUCTION FUNCTION,
CONSUMERS' WELFARE IS HIGHER UNDER THE CASE OF NO VI.

- ④ INEFFICIENT PRODUCTION OCCURS WHEN NO INTEGRATION, HOWEVER. (WHY?)

ACTUALLY THE LEAST EXPENSIVE WAY TO PRODUCE QUANTITY THAT WE FOUND (Q = 4.37) IS TO USE

$$E = 4.37 + L = 4.37$$

$$\text{WHICH COST} = 4.37 \times 1 + 4.37 \times 1 = 8.74$$

BUT, LOOK... NOW, W/O VI, $E = 1.55 + L = 12.30$

$$\text{WHICH COSTS}$$

$$= 1.55 + 12.30 = 13.85$$

SO, SOCIAL LOSS FROM INEFFICIENT PRODUCTION

$$= 13.85 - 8.74 = 5.11$$

⑤ SOCIAL WELFARE IS LOWER UNDER W/O VI THAN UNDER W/ VI.

	W/O VI	W/ VI
CS	9.55	8
π	$\frac{10.75}{20.3}$	$\frac{16}{24}$

$$\Delta SW = 20.3 - 24 = -3.7$$

W/O VI W/VI

REFLECTS

LOSS FROM INEFFICIENT PRODUCTION WHEN WE DO NOT INTEGRATE

$$(= -5.11)$$

LOSS

THAT "OUTWEIGHS"

THE REDUCTION

IN DWL

DUE TO MONOPOLY PRICING

$$(+1.44)$$

COME FROM

$$= 8 - 6.59$$

DWL_{VI}

DWL_{NOVI}

GAIN

TO SUMMARISE, UNDER VARIABLE PROPORTION PRODUCTION FUNCTION,

FIRMS HAVE INCENTIVE TO "MERGE" AS $\pi_{VI} > \pi_{NOVI}$

$$(16)$$

$$(10.75)$$

FIRMS THEN WILL MERGE IF $\text{BENEFIT}_{VI} > \text{COST OF INTEGRATION}$

SOCIAL WELFARE W/ VI IS HIGHER.

VERTICAL RESTRICTIONS

"I DON'T TRUST HIM. WE'RE FRIENDS!"

- BERTOLT BRECHT

MANUFACTURER

DISTRIBUTOR
OR RETAILER

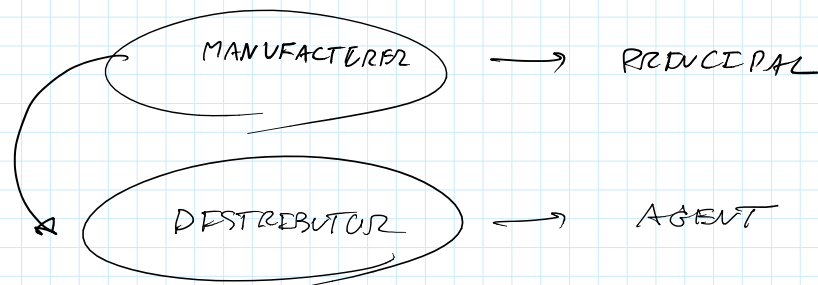
VR : CONTRACTUAL RESTRICTIONS IMPOSED ON DISTRIBUTOR(S)
BY A MANUFACTURER.

- EX:
- RESTRICTION OF MINIMUM SALES
 - RESTRICTION ON PRICE CHARGED TO BUYERS
 - RESTRICTION ABOUT LOCATIONS (EX: THEY MUST NOT LOCATE CLOSE TO EACH OTHER)
 - DO NOT SELL ANY COMPETING PRODUCTS

RATIONALE

- ① TWO FIRMS LOCATE AT DIFFERENT COUNTRIES
- ② MANUFACTURER MAY GAIN/BENEFIT FROM EXPERIENCES OF DISTRIBUTOR(S)
 - + LOCATION
 - + TASTES OF CONSUMERS
 - + ETC.

PRINCIPAL - AGENT PROBLEM



PRINCIPAL WANTS AGENT TO ACT IN ACCORDANCE W/
PRINCIPAL'S BEST INTEREST.

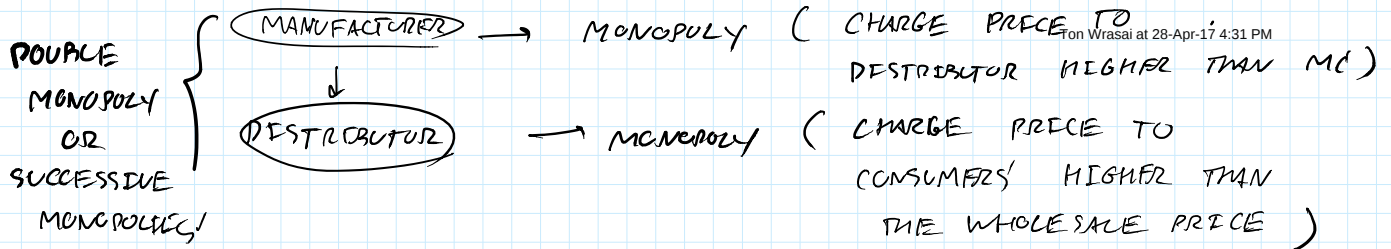
FREE-RIDER PROBLEM ARISES.

EX: DISTRIBUTOR'S MAY ADVERTISE LESS THAN IT REQUIRED IN THE CONTRACT.

VR USED TO SOLVE PROBLEM IN DISTRIBUTION

FOUR PROBLEMS ARISE WHEN DISTRIBUTION IS COSTLY.

① DOUBLE MONOPOLY MARKUP



RESULTS ① VERY EXPENSIVE TO FINAL USERS

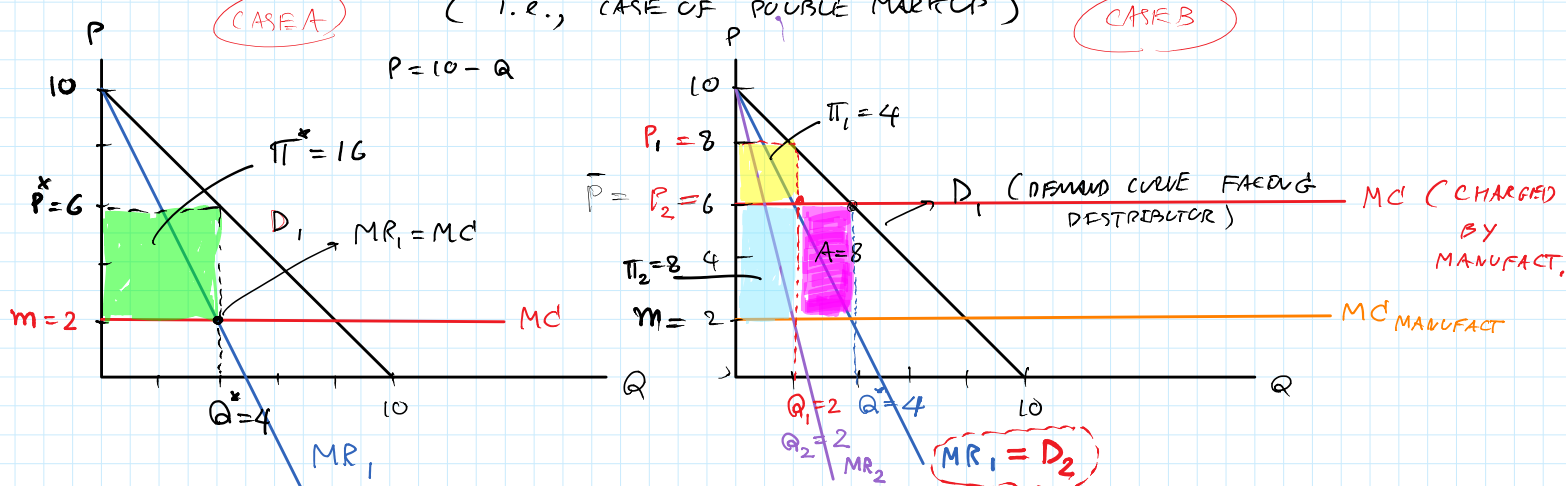
② DOUBLE MONOPOLY MARKUP LOWERS THE JOINT PROFITS OF MANUFACTURER & DISTRIBUTOR

LEADS TO "INCENTIVE" FOR BOTH TO DO EITHER VI OR VR.

LET'S COMPARE PROFITS OF INTEGRATED MANU - DISTRIBUTOR w/

PROFITS OF SUCCESSIVE MONOPOLIES (CASE B) (CASE A)

(i.e., CASE OF DOUBLE MARKUP)



NOTE: ASSUME THAT THE COSTS OF DISTRIBUTION ARE ZERO, FOR SIMPLICITY.

P_2 = WHOLESALE PRICE MANUFACTURER CHARGES TO DISTRIBUTOR.
(IT BECOMES DISTRIBUTOR'S MARGINAL COST)

Q_1 = PROFIT MAXIMIZING OUTPUT LEVEL OF DISTRIBUTOR
(WHERE $MR_1(Q_1) = MC = P_2$)

$MR_1 = D_2$ (DEMAND CURVE FACING MANUFACTURER)

Q_2 = PROFIT-MAXIMIZING OUTPUT LEVEL THAT MANUFACTURER PRODUCES AND SELLS TO DISTRIBUTOR (YOGURT)

- MANUFACTURER PRODUCES $Q_2 = 2$ AND CHARGES $P_2 = 6$ TO DISTRIBUTOR (i.e., SUPERMARKET) → FIRST MARKUP.

$$\pi_2 = (P_2 - m) \cdot Q_2 = (6 - 2) \cdot 2 = 8 \text{ RAHIT / TIME PERIOD}$$

- DISTRIBUTOR SELLS $Q_2 = 2$ AND CHARGES $P_1 = 8$ TO THE BUYERS → SECOND MARKUP

$$\pi_1 = (P_1 - P_2) \cdot Q_1 = (8 - 6) \cdot 2 = 4 \text{ RAHIT / TIME PERIOD}$$

- JOINT PROFITS = $\pi_1 + \pi_2 = 4 + 8 = 12$ RAHIT / TIME PERIOD
(SUPERMARKET) (YOGURT FIRM)

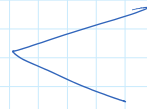
WHICH IS LOWER THAN π OF THE INTEGRATED YOGURT-SUPERMARKET.

THE LOSS OF $\pi = -4$ RAHIT / TIME PERIOD

NOTE π UNDER DOUBLE MARKUP IS 25% LOWER THAN π UNDER VI

- CONSUMERS PAY 30% HIGHER UNDER TWO SUCCESSIVE MONOPOLIES

$P^* = 6$
(VI CASE)



$P_1 = 8$
(DOUBLE MARKUP CASE)

- SUMMARY, UNDER TWO SUCCESSIVE MONOPOLIES, BOTH CONSUMERS AND PRODUCERS ARE WORSE OFF



INCENTIVE TO DO VI OR VR

* YOGURT FIRM DOES NOT WANT SUPERMARKET TO DO MARKUP AS IT GAINS NOTHING FROM THIS ACTION.

IF SUPERMARKET CHARGES 6 RAHIT (THE WHOLESALE) PRICE TO BUYERS, OUTPUT WOULD INCREASE TO $Q = 4$ AND $\pi_{\text{YOGURT FIRM}}$ WOULD BE HIGHER!

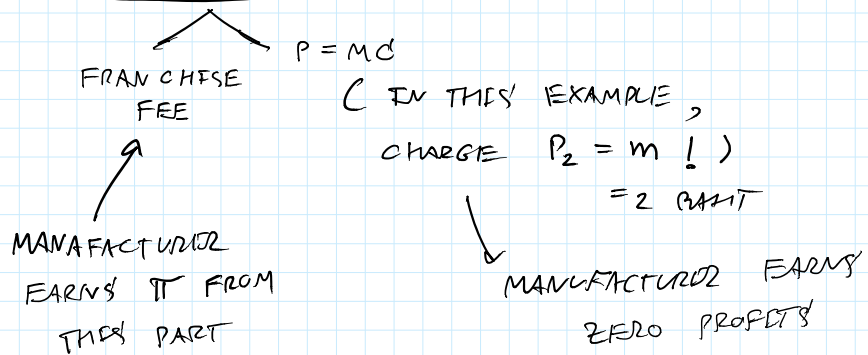
IN OTHER WORDS, YOGURT FIRM WOULD LOVE TO SEE COMPETITION AT DISTRIBUTION LEVEL

(CHARGE BUYERS AT WHOLESALE PRICE)

- IF THE CONTRACT SETS PRICE THAT SUPERMARKET MUST SELL TO BUYER ($\bar{p}$) = 6, SUPERMARKET WILL BEHAVE LIKE A COMPETITIVE SUPERMARKET, SELL $Q^* = 4$. THEN OUTCOME WILL BE THE SAME AS VI CASE!

- OTHER METHODS → QUANTITY FORCING: DISTRIBUTOR MUST SELL A MINIMUM AMOUNT OF OUTPUTS! GIVEN THIS, TO MEET A TARGET, DISTRIBUTOR MAY HAVE TO LOWER THE PRICES

→ TWO-PART TARIFF CAN BE APPLIED



(THEN WE GOT THE SAME RESULT AS VI CASE!)