

Panel Data Regression Models

Simulated Data

Simulated Data with Fixed Effects

```

set more off
clear all
set obs 10
g id=_n

*Generate Fixed Effects
g fe=int(100*runiform())

*Generate x1 that correlated with FE and error term with FE component
forvalue i=1(1)12 {
  g x1`i'=50+5*fe+rnormal(500,100)
  g u`i'=4*fe+rnormal(0,10)
}

*Generate y
forvalue i=1(1)12 {
  g y`i'=1+0.1*x1`i'+u`i'
}

```

```

*Transform data to be panel data
reshape long x1 u y, i(id) j(month)

```

(note: j = 1 2 3 4 5 6 7 8 9 10 11 12)

Data	wide	->	long
Number of obs.	10	->	120
Number of variables	38	->	6
j variable (12 values)		->	month
xij variables:			
	x11 x12 ... x112	->	x1
	u1 u2 ... u12	->	u
	y1 y2 ... y12	->	y

```

. xtset id month
      panel variable:  id (strongly balanced)
      time variable:  month, 1 to 12
              delta:  1 unit

```

```

. reg y x1

```

Source	SS	df	MS	Number of obs	=	120
Model	865133.963	1	865133.963	F(1, 118)	=	248.54
Residual	410739.424	118	3480.84257	Prob > F	=	0.0000
Total	1275873.39	119	10721.6251	R-squared	=	0.6781
				Adj R-squared	=	0.6753
				Root MSE	=	58.999

	y	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
	x1	.5703078	.0361751	15.77	0.000	.4986712 .6419443
	_cons	-182.4773	28.51509	-6.40	0.000	-238.9449 -126.0096

```
. xtreg y x1, fe
```

```
Fixed-effects (within) regression
Group variable: id
```

```
Number of obs   =      120
Number of groups =      10
```

```
R-sq:
```

```
  within = 0.4078
  between = 0.9744
  overall = 0.6781
```

```
Obs per group:
```

```
    min =      12
    avg  =     12.0
    max  =      12
```

```
corr(u_i, Xb) = 0.7786
```

```
F(1,109)      =     75.06
Prob > F      =     0.0000
```

```
-----+-----
           y |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-----+-----
       x1 |   .0896361   .010346     8.66   0.000   .0691306   .1101416
      _cons |  189.5934   8.063686    23.51   0.000   173.6114   205.5753
-----+-----
sigma_u |  96.881565
sigma_e |  10.31783
   rho  |  .98878508   (fraction of variance due to u_i)
-----+-----
```

```
F test that all u_i=0: F(9, 109) = 416.58                Prob > F = 0.0000
```

```
. predict uhat, u
```

```
. corr y fe x1 u
(obs=120)
```

```
-----+-----
           |      y      fe      x1      u
-----+-----
       y |   1.0000
       fe |   0.9919   1.0000
       x1 |   0.8235   0.7797   1.0000
       u |   0.9957   0.9937   0.7674   1.0000
```

Example

1. Panel Least Squares

The model can be stated as:

$$GPP_{it} = \beta_0 + \beta_1 G_{it} + \beta_2 LOAN_{it} + \beta_3 AGRI_{it} + u_{it} \quad (1)$$

where:

GPP_{it} = Gross of provincial product of province i at time t .

G_{it} = Government spending on province i at time t .

$LOAN_{it}$ = Loan outstanding of province i at time t .

$AGRI_{it}$ = Agricultural production of province i at time t .

u_{it} = Disturbance term of province i at time t .

To estimate the model using STATA, we begin by setting the data set to be panel data setting.

```
. xtset id year
      panel variable:  id (strongly balanced)
      time variable:  year, 0 to 9
              delta:  1 year
```

The model without any problems

```
. xtgls gpp g loan agri
```

Cross-sectional time-series FGLS regression

Coefficients: generalized least squares
Panels: homoskedastic
Correlation: no autocorrelation

Estimated covariances	=	1	Number of obs	=	80
Estimated autocorrelations	=	0	Number of groups	=	8
Estimated coefficients	=	4	Time periods	=	10
			wald chi2(3)	=	748.54
Log likelihood	=	-779.4455	Prob > chi2	=	0.0000

	gpp	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
	g	1.920918	.8032843	2.39	0.017	.3465095 3.495326
	loan	.5097789	.046617	10.94	0.000	.4184112 .6011465
	agri	-53.35561	14.93147	-3.57	0.000	-82.62075 -24.09048
	_cons	11683.41	1378.756	8.47	0.000	8981.096 14385.72

The model with Heteroskedasticity

```
. xtgls gpp g loan agri, igls panels(heteroskedastic)
```

Iteration 1: tolerance = .41982167

...

Iteration 22: tolerance = 6.777e-08

Cross-sectional time-series FGLS regression

Coefficients: generalized least squares

```

Panels:      heteroskedastic
Correlation: no autocorrelation

Estimated covariances      =      8      Number of obs      =      80
Estimated autocorrelations =      0      Number of groups   =      8
Estimated coefficients     =      4      Time periods       =     10
Log likelihood             = -721.8528   Wald chi2(3)        =    1140.96
                               Prob > chi2      =      0.0000

```

	gpp	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
	g	-.1485432	.2537412	-0.59	0.558	-.6458667	.3487803
	loan	.6368605	.0246414	25.85	0.000	.5885644	.6851567
	agri	-12.99571	2.658269	-4.89	0.000	-18.20582	-7.785598
	_cons	6153.178	344.0983	17.88	0.000	5478.757	6827.598

Model with Heteroskedasticity and Cross-sectional Correlation

```
. xtgls gpp g loan agri, panels(correlated)
```

Cross-sectional time-series FGLS regression

```

Coefficients: generalized least squares
Panels:      heteroskedastic with cross-sectional correlation
Correlation: no autocorrelation

Estimated covariances      =     36      Number of obs      =     80
Estimated autocorrelations =      0      Number of groups   =      8
Estimated coefficients     =      4      Time periods       =     10
Log likelihood             = -669.5133   Wald chi2(3)        =    2262.05
                               Prob > chi2      =      0.0000

```

	gpp	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
	g	1.50661	.3003486	5.02	0.000	.9179374	2.095282
	loan	.508701	.0178062	28.57	0.000	.4738015	.5436004
	agri	-42.39837	3.959852	-10.71	0.000	-50.15954	-34.6372
	_cons	10721.04	388.408	27.60	0.000	9959.776	11482.31

Model with Heteroskedasticity, Cross-sectional Correlation, and Autocorrelation

```
. xtgls gpp g loan agri, panels(correlated) corr(ar1)
```

Cross-sectional time-series FGLS regression

```

Coefficients: generalized least squares
Panels:      heteroskedastic with cross-sectional correlation
Correlation: common AR(1) coefficient for all panels (0.8532)

Estimated covariances      =     36      Number of obs      =     80
Estimated autocorrelations =      1      Number of groups   =      8
Estimated coefficients     =      4      Time periods       =     10
Log likelihood             = -610.0246   Wald chi2(3)        =     265.49
                               Prob > chi2      =      0.0000

```

	gpp	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
	g	-.2611345	.3368487	-0.78	0.438	-.9213458	.3990767
	loan	.518529	.0439935	11.79	0.000	.4323034	.6047546
	agri	.4994303	1.297904	0.38	0.700	-2.044414	3.043275
	_cons	8643.839	311.1028	27.78	0.000	8034.088	9253.589

2. Fixed Effect Model

The model can also be applied as fixed effect model:

$$GPP_{it} = \beta_0 + \beta_1 G_{it} + \beta_2 LOAN_{it} + \beta_3 AGRI_{it} + u_{it} \quad (2)$$

```
. xtreg gpp g loan agri, fe
```

```
Fixed-effects (within) regression      Number of obs   =      80
Group variable (i): id                Number of groups =       8

R-sq:  within = 0.7585                Obs per group:  min =      10
      between = 0.8963                      avg   =     10.0
      overall  = 0.8346                      max   =      10

corr(u_i, xb) = 0.8353                F(3,69)         =     72.25
                                      Prob > F          =     0.0000
```

	gpp	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
	g	1.442314	.2248462	6.41	0.000	.993758	1.89087
	loan	.1171806	.0358101	3.27	0.002	.0457415	.1886197
	agri	11.94431	5.654815	2.11	0.038	.6632614	23.22536
	_cons	12472.26	667.2543	18.69	0.000	11141.12	13803.4
	sigma_u	10363.779					
	sigma_e	906.01137					
	rho	.99241554	(fraction of variance due to u_i)				

```
F test that all u_i=0:      F(7, 69) =    226.72      Prob > F = 0.0000
```

```
. estimates store fixed
```

```
. predict gpp_fe, xbu
```

To compute fixed effect, use the following command:

```
. predict ai, u
. table id, c(mean ai)
```

ID	mean(ai)
1	21100.33
2	2711.693
3	5643.245
4	-10611.55
5	2260.344
6	-6132.393
7	-7620.03
8	-7351.638

3. Random Effect Model

The model can also be specified as random effect model:

$$GPP_{it} = \beta_0 + \beta_1 G_{it} + \beta_2 LOAN_{it} + \beta_3 AGRI_{it} + u_{it} \quad (3)$$

and $u_{it} = v_i + w_t + \varepsilon_{it}$

where: v_i = cross-section random effect

w_t = time random effect

ε_{it} = residual term

```
. xtreg gpp g loan agri, re
```

```
Random-effects GLS regression           Number of obs   =       80
Group variable (i): id                 Number of groups  =        8

R-sq:  within = 0.6104                  Obs per group: min =       10
       between = 0.9007                  avg           =      10.0
       overall = 0.8840                  max           =       10

Random effects u_i ~ Gaussian           wald chi2(3)      =      246.85
corr(u_i, X) = 0 (assumed)              Prob > chi2       =      0.0000
```

gpp	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
g	.4391357	.4329641	1.01	0.310	-.4094584	1.28773
loan	.4686367	.045272	10.35	0.000	.3799053	.5573682
agri	4.008584	11.51057	0.35	0.728	-18.55171	26.56888
_cons	8736.887	1368.123	6.39	0.000	6055.414	11418.36
sigma_u	1009.6082					
sigma_e	906.01137					
rho	.55392236	(fraction of variance due to u_i)				

```
. estimates store random
```

```
. predict gpp_re, xbu
```

To compute random effect, use the following command:

```
. predict ri, u
```

```
. table id, c(mean ri)
```

ID	mean(ri)
1	5131.64
2	4695.539
3	6389.667
4	-6270.812
5	624.1134
6	-3240.626
7	-3939.543
8	-3389.978

To compute perform Hausman test, use the following command:

```
. hausman random fixed
```

	---- Coefficients ----		(b-B) Difference	sqrt(diag(V_b-V_B)) S.E.
	(b) random	(B) fixed		
g	.4391357	1.442314	-1.003178	.3700028
loan	.4686367	.1171806	.3514562	.0276982
agri	4.008584	11.94431	-7.935725	10.02578

b = consistent under H_0 and H_a ; obtained from xtreg
 B = inconsistent under H_a , efficient under H_0 ; obtained from xtreg

Test: H_0 : difference in coefficients not systematic

```
chi2(3) = (b-B)'[(V_b-V_B)^(-1)](b-B)
        =      285.14
Prob>chi2 =      0.0000
```

```

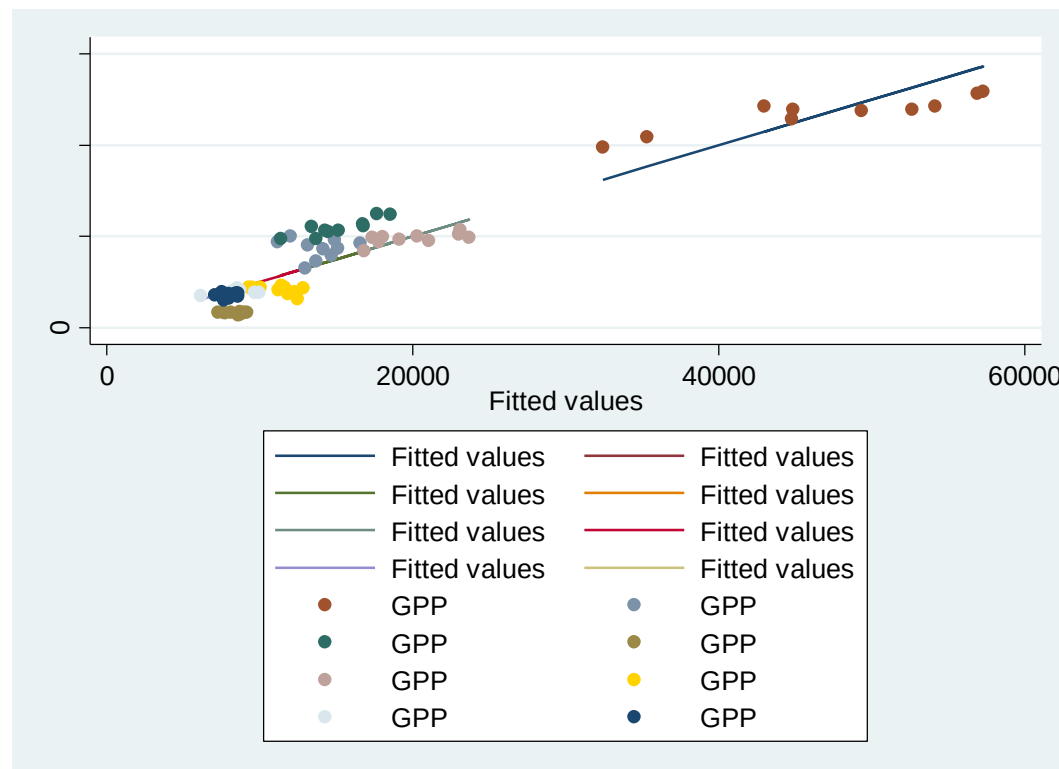
. twoway (line gpp_gls gpp_gls if id==1) (line gpp_gls gpp_gls if id==2) (line
gpp_gls gpp_gls if id==3) (line gpp_gls gpp_gls if id==4) (line gpp_gls gpp_gls
if id==5) (line gpp_gls gpp_gls if id==6) (line gpp_gls gpp_gls if id==7) (line
gpp_gls gpp_gls if id==8) (scatter gpp gpp_gls if id==1) (scatter gpp gpp_gls if
id==2) (scatter gpp gpp_gls if id==3) (scatter gpp gpp_gls if id==4) (scatter gpp
gpp_gls if id==5) (scatter gpp gpp_gls if id==6) (scatter gpp gpp_gls if id==7)
(scatter gpp gpp_gls if id==8)

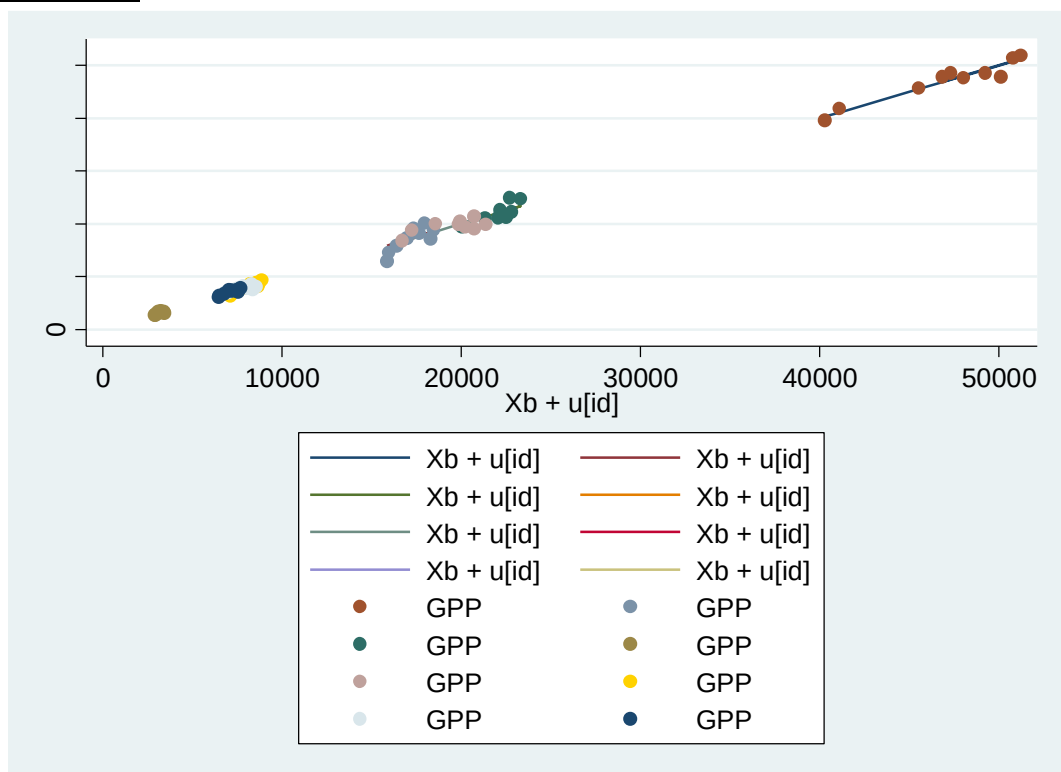
. twoway (line gpp_fe gpp_fe if id==1) (line gpp_fe gpp_fe if id==2) (line gpp_fe
gpp_fe if id==3) (line gpp_fe gpp_fe if id==4) (line gpp_fe gpp_fe if id==5)
(line gpp_fe gpp_fe if id==6) (line gpp_fe gpp_fe if id==7) (line gpp_fe gpp_fe
if id==8) (scatter gpp gpp_fe if id==1) (scatter gpp gpp_fe if id==2) (scatter
gpp gpp_fe if id==3) (scatter gpp gpp_fe if id==4) (scatter gpp gpp_fe if id==5)
(scatter gpp gpp_fe if id==6) (scatter gpp gpp_fe if id==7) (scatter gpp gpp_fe
if id==8)

. twoway (line gpp_re gpp_re if id==1) (line gpp_re gpp_re if id==2) (line gpp_re
gpp_re if id==3) (line gpp_re gpp_re if id==4) (line gpp_re gpp_re if id==5)
(line gpp_re gpp_re if id==6) (line gpp_re gpp_re if id==7) (line gpp_re gpp_re
if id==8) (scatter gpp gpp_re if id==1) (scatter gpp gpp_re if id==2) (scatter
gpp gpp_re if id==3) (scatter gpp gpp_re if id==4) (scatter gpp gpp_re if id==5)
(scatter gpp gpp_re if id==6) (scatter gpp gpp_re if id==7) (scatter gpp gpp_re
if id==8)

```

Pooled GLS



Fixed EffectRandom Effect