

1. a.) Estimation Regression for $\log(\text{salary}_i)$

$$\log(\text{salary}_i) = 4.5881 + 0.2592 \log(\text{sales}_i) + 0.0112 \text{ROE}_i + 0.1580 \text{finance}_i + 0.1809 \text{consprod}_i - 0.2830 \text{utility}_i$$

Interpret B_1 : If sales_i increases by 1%, salary_i will rise by 4.5881%.

1. b.) Overall Significance Level

$H_0: B_i = 0$; Every independent variables has no relationship with dependent var.
 $H_1: B_i \neq 0$; At least 1 independent variable has relationship with dependent var.

$\text{Prob.} > F = 0.000$ means that p-value equals zero.

P-value $< \alpha$; $0.000 < 0.05$

We can reject H_0 and cannot conclude that

every independent variables has no relationship with dependent variable.

• Individual Test

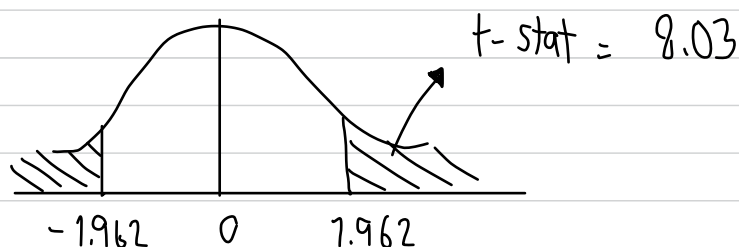
For B_1 ($\log \text{sales}_i$)

$H_0: B_1 = 0$; Sales has no impact on $\log \text{salary}_i$

H_1 : Otherwise; Sales has an impact on $\log \text{salary}_i$

t-stat = 8.03

t-Cri = $t_{0.05, 209-6} = t_{0.05, 203} = 1.962$



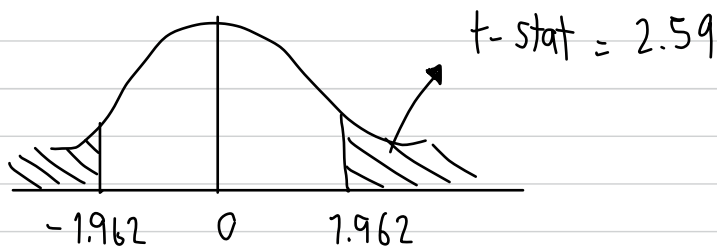
$\therefore$ We can reject H_0 . Sales has an impact on $\log \text{salary}_i$ at significance level 0.05.

For B_2 (ROE)

$H_0: B_2 = 0$; ROE has no impact on $\ln \text{salary}_i$
 H_1 : Otherwise ; ROE has an impact on $\ln \text{salary}_i$

$$t\text{-stat} = 2.59$$

$$t\text{-Cri} = t_{0.05, 209-6} = t_{0.05, 203} = 1.962$$



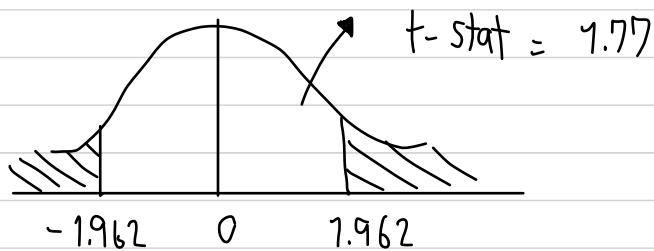
$\therefore$ We can reject H_0 . ROE has an impact on $\ln \text{salary}_i$ at significance level 0.05.

For B_3 (finance)

$H_0: B_3 = 0$; Finance has no impact on $\ln \text{salary}_i$
 H_1 : Otherwise ; Finance has an impact on $\ln \text{salary}_i$

$$t\text{-stat} = 1.77$$

$$t\text{-Cri} = t_{0.05, 209-6} = t_{0.05, 203} = 1.962$$



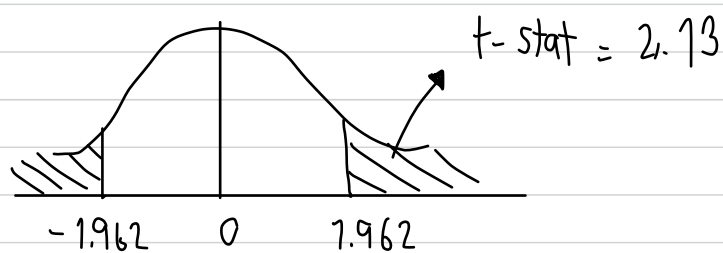
$\therefore$ We can't reject H_0 . Finance has no impact on $\ln \text{salary}_i$ at significance level 0.05.

For B4

$H_0: B_4 = 0$; Consprod has no impact on $\ln \text{salary}_i$
 H_1 : Otherwise ; Consprod has an impact on $\ln \text{salary}_i$

$$t\text{-stat} = 2.13$$

$$t\text{-Cri} = t_{0.05, 209-6} = t_{0.05, 203} = 1.962$$



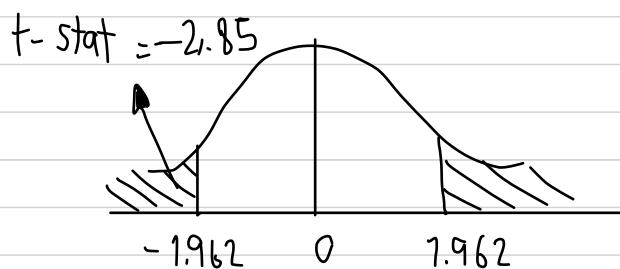
$\therefore$ We can reject H_0 . Consprod has an impact on $\ln \text{salary}_i$ at significance level 0.05.

For B5

$H_0: B_5 = 0$; Utility has no impact on $\ln \text{salary}_i$
 H_1 : Otherwise ; Utility has an impact on $\ln \text{salary}_i$

$$t\text{-stat} = -2.85$$

$$t\text{-Cri} = t_{0.05, 209-6} = t_{0.05, 203} = 1.962$$



$\therefore$ We can reject H_0 . Utility has an impact on $\ln \text{salary}_i$ at significance level 0.05.

1. c.) -0.283005%

1. d.) It's not possible. There will be no observations.

In this case, we can have at most z dummy variables.

There must have a baseline / reference to compare.

1. e.) Interaction variable is beneficial, since it causes an additional effect which can tell effect of two attributes considered individually.

t-test from model 2.1

2. d.) $H_0: \beta_1 = 0$ (Smoking has no impact on birth weight)
 $H_1: \beta_1 \neq 0$ (Smoking has an impact on birth weight)

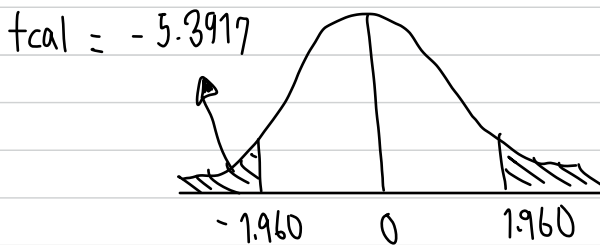
$$\text{Find } t_{\text{cal}} = \frac{\hat{\beta}_1 - \beta_1}{\text{S.E.}\hat{\beta}_1} = \frac{-0.5877 - 0}{0.1090} = -5.3917$$

$$t_{\text{critical}} : \text{d.f.} = n - k = 1191 - 3 = 1188$$

$\alpha = 0.05$

$$\text{Warning } t = -1.960, 1.960$$

Conclude the test:



$\therefore$ we can reject H_0 , and we can say that Smoking has effect on birth weight. #

2. b.) Construct 99% CI of β_2

$$t_{\frac{\alpha}{2}, \text{d.f.}} = t_{\frac{0.01}{2}, 1188} = t_{0.005, 1188} = 2.581$$

$$\hat{\beta}_2 - (t_{\frac{\alpha}{2}, \text{d.f.}})(\text{S.E.}\hat{\beta}_2) < \beta_2 < \hat{\beta}_2 + (t_{\frac{\alpha}{2}, \text{d.f.}})(\text{S.E.}\hat{\beta}_2)$$

$$0.0625 - 2.581(0.0324) < \beta_2 < 0.0625 + 2.581(0.0324)$$
$$-0.0213 < \beta_2 < 0.1462 \quad \#$$

From Model 2.2

2. c.) $H_0 : B_1 = 0$ (Smoking has no impact on birth weight)

$H_1 : B_1 \neq 0$ (Smoking has an impact on birth weight)

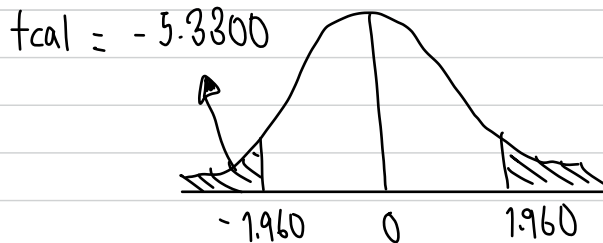
$$\text{Find } t_{\text{cal}} = \frac{B_1 - B_0}{\text{S.E.} \hat{\beta}_1} = \frac{-0.5895 - 0}{0.1106} = -5.3300$$

$$T_{\text{critical}} : \text{d.f.} = n - k = 1191 - 5 = 1186$$

$$\alpha = 0.05$$

$$L \rightarrow = -1.960, 1.960$$

Conclude the test:



$\therefore$ we can reject H_0 , and we can say that Smoking has effect on birth weight. #

The result in 2.a) will be unchanged.

from model 2.2

2.d.) • Overall Significance

$$H_0 : \beta_1 = 0$$

$$H_1 : \beta_1 \neq 0$$

Use F-Stat = 10.05

$$\text{Prob.} > F = 0.000$$

$$F\text{-stat} > F\text{-critical}$$

$$10.05 > F_{4, 1186}$$

∴ We can reject H_0 and we can say that there's at least 1 independent variable that has relationship with dependent variable.

- Individual Test from 2.c for $\beta_1 \Rightarrow$ we can reject H_0 ,
and 2.e for β_3 & $\beta_4 \Rightarrow$ we can't reject H_0 .

For β_2 : $H_0 : \beta_2 = 0$ family income has no impact
 $H_1 : \beta_2 \neq 0$ otherwise

$$t\text{-stat} = \frac{\hat{\beta}_2 - \beta_2}{S.E.\hat{\beta}_2} = \frac{0.0538254 - 0}{0.0366502} = 1.4686$$

$$T_{\text{critical}} : \text{d.f.} = n - k = 1191 - 5 = 1186$$

$$\alpha = 0.05$$

$$\hookrightarrow = -1.960, 1.960$$

$t\text{-stat} < |t_{\text{cal}}|$
∴ We can't reject H_0

2.e.) $H_0 : \beta_3 = 0$ father edu has no impact
 $H_1 : \beta_3 \neq 0$ otherwise

$H_0 : \beta_4 = 0$ mother.
 $H_1 : \beta_4 \neq 0$ has no impact otherwise

$$t\text{-stat} = \frac{\hat{\beta}_3 - \beta_3}{S.E.\hat{\beta}_3} = \frac{0.4937 - 0}{0.2833} = 1.7427$$

$$t\text{-stat} = \frac{\hat{\beta}_4 - \beta_4}{S.E.\hat{\beta}_4} = \frac{-0.4379 - 0}{0.3197} = -1.3697$$

$$T_{\text{critical}} : \text{d.f.} = n - k = 1191 - 5 = 1186$$

$$\alpha = 0.05$$

$$\hookrightarrow = -1.960, 1.960$$

$$T_{\text{critical}} : \text{d.f.} = n - k = 1191 - 5 = 1186$$

$$\alpha = 0.05$$

$$\hookrightarrow = -1.960, 1.960$$

Conclude: We cannot reject H_0 , we can say that both father and mother's education have no effect on birth weight.

3. a.) d.f. a. All variables - 1 dependent variable = $7 - 1 = 6$
 b. No. of obs. - all variables (k) = $428 - 7 = 421$
 c. No. of obs. - 1 = $428 - 1 = 427$

3. b.) Find sum square : $TSS = ESS + RSS$

$$F\text{-Stat} = \frac{MSE}{MSR} = \frac{g}{h}$$

$$13.19 = \frac{MSE}{0.4465}$$

$$\therefore MSE = 5.8897$$

from the model,

$$\therefore MSR = 0.4465$$

$$MSE = \frac{ESS}{d.f.}$$

$$5.8897 = \frac{ESS}{6}$$

$$\therefore ESS = 35.3381 \quad (e.)$$

$$MSR = \frac{RSS}{d.f.}$$

$$0.4465 = \frac{RSS}{421}$$

$$\therefore RSS = 187.9876 \quad (f.)$$

$$\therefore MST = MSE + MSR = 6.3362$$

Source	SS	df	MS
Model	35.3381	6	5.8897
Residual	187.9876	421	.446526442
Total	223.327441	427	6.3362

Number of obs = 428
 F(____,____) = 13.19
 Prob > F = 0.0000
 R-squared R^2 = 0.1582
 Adj R-squared = 0.1462
 Root MSE = .66823

lwage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
exper	.039819	.013393	2.97	0.003	.0134936 .0661444
expersq	-.0007812	.0004022	-1.94	0.053	-.0015718 9.37e-06
educ	.1078319	.0144021	7.49	0.000	.079523 .1361409
age	-.0014653	.0052925	-0.28	0.782	-.0118682 .0089377
kidslt6	-.0607106	.0887626	-0.68	0.494	-.2351836 .1137625
kidsge6	-.014591	.0278981	-0.52	0.601	-.069428 .0402459
_cons	-.4209078	.316905	-1.33	0.185	-1.043821 .2020053

3. c.) from the model, $R^2 = 0.1582$

$$\text{Adjusted } R^2 \quad (\bar{R}^2) = 1 - \frac{(1 - R^2)(n-1)}{(n-k)}$$

$$\bar{R}^2 = 1 - \frac{(1 - 0.1582)(428-1)}{(428-7)}$$

$$\bar{R}^2 = 1 - 0.853797$$

$$\therefore \bar{R}^2 = 0.1462 \quad \#$$

3. d.) Maximum R^2 will be less than 0.1582

3. e.) Age is not significance and I believe that this make an economic sense. Elderly may work at low wage for example senior construction worker $\text{คนงานก่อสร้างอาวุโส}$ And teenagers may work at high wage such as $\text{อายุช่วยรับจ้าง หรือคนงานวัยใส}$.