1 (30 points) You are conducting an econometric model to explain the new passenger cars sold in the United States using the yearly data from Business Statistics, 1986, A Supplement to the Current Survey of Business, U.S Department of Commerce from 1971 to 1986. Estimate the model Eq.1 reports in the Table 1.1

$$\ln(\mathrm{Y})_i = \beta_1 + \beta_2 \ln(\mathrm{X2})_i + \beta_3 \ln(\mathrm{X3})_i + \beta_4 \ln(\mathrm{X4})_i + \beta_5 \ln(\mathrm{X5})_i + \beta_6 \ln(\mathrm{X6})_i \tag{Eq.1}$$

where

Y = new passenger cars sold (Thousands), seasonally unadjusted.

X2 = new cars, Consumer Price Index, 1967=100, seasonally unadjusted.

X3 = Consumer Price Index (CPI), all urban consumers, 1967 = 100, seasonally unadjusted.

X4 = the personal disposable income (PDI), billions of dollars, unadjusted for seasonal variation.

X5 = the interest rate, percent, finance company paper placed directly.

X6 = the employed civilian labor force (thousands), unadjusted for seasonal variation.

The estimation result model Eq.1 is reported as below:

Table 1.1 The Regression Result of Model Eq.1

```
.
. regress ln_y ln_x2 ln_x3 ln_x4 ln_x5 ln_x6
```

Source	SS	df	MS			
Model	.183346202	5	.03666924	Number of obs	=	16
Residual	.031143181	10	.003114318	F(5, 10)	=	11.77
				Prob > F	=	0.0006
Total	.214489383	15	.014299292	R-squared	=	0.8548
				Adj R-squared	=	0.7822
				Root MSE	=	.05581

ln_y	Coef.	Std. Err.	t	P>|t|	[95% Conf.	Interval]
ln_x2	1.790195	.8732533	2.05	0.068	-.1555348	3.735924
ln_x3	-4.108607	1.5997	-2.57	0.028	-7.672961	-.5442541
ln_x4	2.127265	1.257849	1.69	0.122	-.6753965	4.929926
ln_x5	-.0304413	.1218489	-0.25	0.808	-.3019375	.2410549
ln_x6	.2776846	2.036986	0.14	0.894	-4.261003	4.816372
_cons	3.255855	19.11665	0.17	0.868	-39.33869	45.8504

1.1 (5 points) Report the regression equation for model Eq.1 in the standard format.

1.2 (10 points) Based on Table 1.1, Is there evidence of multicollinearity in the data? How do you know? Explain your answers in detail and state the critical value for hypothesis testing to receive fully points. If there is the multicollinearity problem, what remedial action, if any, would you take?

Table 1.2 the Correlation Matrix

```
. corr ln_x2 ln_x3 ln_x4 ln_x5 ln_x6
(obs=16)
```

	ln_x2	ln_x3	ln_x4	ln_x5	ln_x6
ln_x2	1.0000				
ln_x3	0.9958	1.0000			
ln_x4	0.9931	0.9960	1.0000		
ln_x5	0.5850	0.6187	0.5850	1.0000	
ln_x6	0.9737	0.9740	0.9868	0.5995	1.0000

Table 1.3 Variance Inflation Factors and Tolerance (VIF)

```
. vif
```

Variable	VIF	1/VIF
ln_x4	1525.71	0.000655
ln_x3	1524.39	0.000656
ln_x2	243.46	0.004107
ln_x6	194.98	0.005129
ln_x5	7.72	0.129573
Mean VIF	699.25	

1.3 (15 points) Apply the correlation matrix and Variance Inflation Factors and Tolerance (VIF) given in Table 1.2 and 1.3 to detect the multicollinearity. If there is the multicollinearity problem, what remedial action, if any, would you take?

2. (40 points) This empirical illustration is based on the data on the copper industry. The data were collected by Gary R. Smith from sources such as American Metal Market, and U.S. Department of Commerce publications. The Data are time series data with 30 yearly observations from 1951 to 180 on the following variables :

C: = 12-month average U.S. domestic price of copper (cents per pound);
G: = annual gross national product ($, billions) ;
I: = 12-month average index of industrial production;
L: = 12-month average London Metal Exchange price of copper (pounds sterling);
H: = number of housing starts per year (thousands of units);
A: = 12-month average price of aluminum (cents per pound);

The model used to explain U.S. domestic price of copper is a linear regression model which is represented as:

$$ln(C_t) \quad = \quad \beta_1 + \beta_2 ln(G_t) + \beta_3 ln(I_t) + \beta_4 ln(L_t) + \beta_5 ln(H_t) + \beta_6 ln(A_t) + u_i \qquad \text{(Eq.2)}$$

The estimation result is reported as below:

Table 2.1 The regression result of the U.S. domestic price of copper

```
reg ln_c ln_g ln_i ln_h ln_a
```

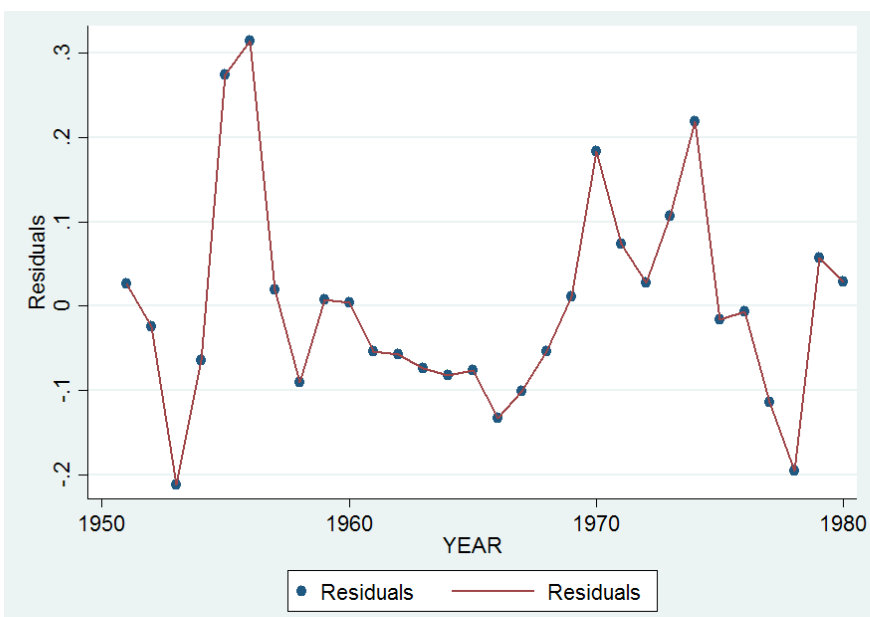
Source	SS	df	MS			
				Number of obs	=	30
				F(4, 25)	=	75.61
Model	5.35560316	4	1.33890079	Prob > F	=	0.0000
Residual	.442711453	25	.017708458	R-squared	=	0.9236
				Adj R-squared	=	0.9114
Total	5.79831462	29	.199941883	Root MSE	=	.13307

ln_c	Coef.	Std. Err.	t	P>|t|	[95% Conf.	Interval]
ln_g	.3444082	.364575	0.94	0.354	-.4064481	1.095265
ln_i	.3846288	.4442729	0.87	0.395	-.5303684	1.299626
ln_h	-.1115663	.1641585	-0.68	0.503	-.4496571	.2265244
ln_a	.2620905	.2593886	1.01	0.322	-.2721303	.7963114
_cons	-.3591806	1.274879	-0.28	0.780	-2.984842	2.266481

2.1 (5 points) Based on the regression result of the U.S. domestic price of copper on table 2.1, interpret carefully each of the slope coefficient estimates β_2 and β_6.

Now, consider the following stata command:

predict uhat,resid
two-way (scatter that year) (line that year)
Figure 2.1



2.2 (5 points) From the Figure 2.1, is there the problem of autocorrelation? If yes, positive or negative autocorrelation ? Briefly explain how you detect it.

Test 2.1 Detect the AR(1) in the disturbance terms Eq.2

```
.
. reg uhat L1.uhat,noconstant
```

Source	SS	df	MS
Model	.083576661	1	.083576661
Residual	.358444716	28	.012801597
Total	.442021377	29	.015242116

Number of obs	=	29
F(1, 28)	=	6.53
Prob > F	=	0.0163
R-squared	=	0.1891
Adj R-squared	=	0.1601
Root MSE	=	.11314

uhat	Coef.	Std. Err.	t	P>|t|	[95% Conf.	Interval]
uhat						
L1.	.4349081	.1702108	2.56	0.016	.0862471	.783569

2.3 (10 points) Based on the Test 2.1, Is there positive serial correlation in the disturbances at the 5 percent level of significance? Show your work to receive full credits.

Test 2.2 Detect the AR(1) in the disturbance terms Eq.2

```
. estat dwatson

Durbin-Watson d-statistic(  5,    30) =  1.128376
```

2.3 (10 points) Based on the Test 2.2, Is there positive serial correlation in the disturbances at the 5 percent level of significance? Show your work to receive full credits.

2.4 (10 points) Given Durbin-Watson result on Test 2.2, is it necessary to fix the problem of positive serial correlation in the disturbances ? Why? What is your recommendation to resolve this problem?

The End of Exam

1 (18 points) You are conducting an empirical investigation into the median prices of houses in 506 communities of a large metropolitan area. The sample data consist of 506 observations on the following observable variables:

P_i = the median house price in community i, in dollars;

NOX_i = the level of nitrous oxide in the air of community i, in parts per 100 million;

$DIST_i$ = the weighted distance of community i from 5 employment centers, in miles;

$ROOMS_i$ = the average number of rooms per house in community i;

$STRAT_i$ = the average student-teacher ratio of schools in community i.

Your research assistant estimates the following model of median house prices on the sample of N = 506 observations. The OLS estimation results for the model are given below (with standard errors given in parentheses below coefficient estimates).

$$\ln(\mathrm{P})_i = \beta_1 + \beta_2 \ln(\mathrm{NOX})_i + \beta_3 \ln(\mathrm{DIST})_i + \beta_4 \mathrm{ROOMS}_i + \beta_5 \mathrm{START}_i + u_i \quad \text{(Eq.1)}$$

OLS Estimates of Equation Eq.1:

$$\hat{\beta}_1 = 11.08 \quad \hat{\beta}_2 = -0.9535 \quad \hat{\beta}_3 = -0.1343 \quad \hat{\beta}_4 = 0.2545 \quad \hat{\beta}_5 = -0.05245$$
$$(0.3181) \quad (0.1167) \quad (0.04310) \quad (0.01853) \quad (0.005897)$$

$$\mathrm{RSS} = \sum_{i=1}^{N} \hat{u}_i^2 = 35.1835; \quad \mathrm{TSS} = \sum_{i=1}^{N} \left(\ln P_i - \overline{\ln P}\right)^2 = 84.5822; \quad N = 506$$

NOTE: standard errors in parentheses below coefficient estimates.
RSS is the Residual Sum-of-Squares and TSS is the total Sum-of-Squares from OLS estimation of regression equation Eq.1.

1.1(3 points) Interpret each of the slope coefficient estimates $\hat{\beta}_2$ and $\hat{\beta}_4$ in regression equationEq.1; that is, explain in words what the numerical values of the slope coefficient estimates $\hat{\beta}_2$ and $\hat{\beta}_4$ mean.

1.2(4 points) Use the estimation results for regression equation Eq.1 to test the individual significance of each of the slope coefficient estimates $\hat{\beta}_2$ for ln(NOX) and $\hat{\beta}_4$ for ROOMS. For each test, state the null and alternative hypotheses, show how you calculate the required test statistic, and draw the conclusion. Which of these two slope coefficient estimates are individually significant at the 5 percent significance level?

1.3(5 points) Use the estimation results for regression equation Eq.1 to test the joint significance of all the slope coefficient estimates at the 1 percent significance level (i.e., for significance level $\alpha = 0.01$). State the null and alternative hypotheses, show how you calculate the required test statistic, and state the decision rule you use, and the conclusion you would draw from the test.

1.4(6 points) Use the estimation results for regression equation Eq.1 to test the proposition that $\beta_2 = \beta_3$, i.e., the marginal effect of ln(NOX) on ln(P) equals the marginal effect of ln(DIST) on ln(P).

Explain in words what this proposition means. Perform the test at the 1 percent significance level.

State the null hypothesis H_0 and the alternative hypothesis H_1. Write the restricted regression equation implied by the null hypothesis H_0.

OLS estimation of this **restricted regression equation** yields a **Residual Sum-of-Squares value of RSS = 41.9532**. Use this information, together with the results from OLS estimation of equation Eq.1, to calculate the required test statistic, and state the decision rule you use, and the conclusion you would draw from the test.

2 (18 points) Consider the log monthly earnings equation as follows:

$$\begin{aligned}\log(\text{wage})_i &= \beta_1 + \beta_2\text{educ}_i + \beta_3\text{exper}_i + \beta_4\text{tenure}_i + \beta_5\text{married}_i \\ &\quad \beta_6\text{black}_i + \beta_7\text{south}_i + \beta_8\text{urban}_i + u_i\end{aligned} \tag{Eq.2}$$

where educ, exper, and tenure are all relevant productivity characteristics. Married, black, south, and urban are qualitative variables.

$\log(\text{wage})_i$ =natural log of wage

educ_i =years of education

exper_i =years of work experience

tenure_i =years with current employer

Married_i =1 if married,

black_i = 1 if black,

south_i =1 if living in the south,

urban_i =1 if living in urban.

The estimation result model Eq.2 is reported as below:
Table 2.1 the regression result of model Eq.2

Source	SS	df	MS
Model	41.8377619	7	5.97682312
Residual	123.818521	927	.133569063
Total	165.656283	934	.177362188

Number of obs	= 935
F(7, 927)	= 44.75
Prob > F	= 0.0000
R-squared	= 0.2526
Adj R-squared	= 0.2469
Root MSE	= .36547

lwage	Coef.	Std. Err.	t	P>|t|	[95% Conf.	Interval]
educ	.0654307	.0062504	10.47	0.000	.0531642	.0776973
exper	.014043	.0031852	4.41	0.000	.007792	.020294
tenure	.0117473	.002453	4.79	0.000	.0069333	.0165613
married	.1994171	.0390502	5.11	0.000	.1227801	.276054
black	-.1883499	.0376666	-5.00	0.000	-.2622717	-.1144281
south	-.0909036	.0262485	-3.46	0.001	-.142417	-.0393903
urban	.1839121	.0269583	6.82	0.000	.1310056	.2368185
_cons	5.395497	.113225	47.65	0.000	5.17329	5.617704

2.1 (2 points) Write out the regression equation for log monthly earning based on model Eq.2.

2.2 (4 points) Which of the coefficients are individually statistically significant at the 5 percent level of significance? State the critical value for hypothesis testing to receive full points.

2.3 (5 points) Holding other factors fixed, what is the approximate difference in monthly earnings between black and nonblacks? Is this difference statistically significant?

Next, we extend the original model to allow the interaction term between the married variable and the black variable by adding the "$\text{married}_i \text{black}_i$" to the equation. The new model is

$$\begin{aligned} \log(\text{wage})_i &= \gamma_1 + \gamma_2 \text{educ}_i + \gamma_3 \text{exper}_i + \gamma_4 \text{tenure}_i + \gamma_5 \text{married}_i \\ & \gamma_6 \text{black}_i + \gamma_7 \text{south}_i + \gamma_8 \text{urban}_i + \gamma_9 \text{married}_i \text{black}_i + u_i \end{aligned} \quad \text{(Eq.3)}$$

The estimation result is reported as below:

Table 2.2 the regression result of model ??

Source	SS	df	MS
Model	41.8849359	8	5.23561699
Residual	123.771347	926	.133662362
Total	165.656283	934	.177362188

Number of obs =	935
F(8, 926) =	39.17
Prob > F =	0.0000
R-squared =	0.2528
Adj R-squared =	0.2464
Root MSE =	.3656

lwage	Coef.	Std. Err.	t	P>|t|	[95% Conf.	Interval]
educ	.0654751	.006253	10.47	0.000	.0532034	.0777469
exper	.0141462	.003191	4.43	0.000	.0078837	.0204087
tenure	.0116628	.0024579	4.74	0.000	.006839	.0164866
married	.1889147	.0428777	4.41	0.000	.1047659	.2730635
black	-.24082	.0960229	-2.51	0.012	-.4292677	-.0523723
south	-.0919894	.0263212	-3.49	0.000	-.1436455	-.0403333
urban	.1843501	.0269778	6.83	0.000	.1314053	.2372948
marriedblack	.0613537	.1032747	0.59	0.553	-.1413259	.2640333
_cons	5.403793	.1141222	47.35	0.000	5.179825	5.627762

Note: marriedblack = married*black

2.4 (4 points) Write out the regression equation for log monthly earning based on model **??**. Does there appear to be a significant interaction effect among the new terms? Assess this with respect to both the black dummy variable and their interaction term and explained the results. What is the conditional expectation of $\log(\text{wage})_i$ for married blacks?

2.5 (3 points) What is the estimated wage differential between married blacks and married nonblacks?

3 (18 points) To assess the feasibility of a guaranteed annual wage (negative income tax), the Rand Corporation conducted a study to assess the response of labor supply (average hours of work) to increasing hourly wages.The data for this study were drawn from a national sample of 6,000 households with a male head earning less than \$ 15,000 annually. The data were divided into 39 demographic groups for analysis. Because data for four demographic groups were missing for some variables, the data given in this example refer to only 35 demographic groups. Estimate the model **??** reports in the Table 3.1

$$\begin{aligned} \text{Hours}_i &= \beta_1 + \beta_2\text{rates}_i + \beta_3\text{ERSP}_i + \beta_4\text{ERNO}_i + \beta_5\text{NEIN}_i \\ &\quad \beta_6\text{asset}_i + \beta_7\text{age}_i + \beta_8\text{DEP}_i + \beta_9\text{school}_i + u_i \end{aligned} \tag{Eq.4}$$

where

Hours_i = average hours worked during the year

rate_i = average hourly wage (dollars)

ERSP_i = average yearly earnings of spouse (dollars)

ERNO_i = average yearly earnings of other family members (dollars)

NEIN_i = average yearly nonearned income

assets_i = average family asset holdings (bank account, etc.) (dollars)

age_i = average age of respondent

DEP_i = average number of dependents

school_i = average highest grade of school completed

The estimation result model **??** is reported as below:
Table 3.1 the regression result of model ??

Source	SS	df	MS
Model	115385.114	8	14423.1393
Residual	24381.6287	26	937.754952
Total	139766.743	34	4110.78655

Number of obs	=	35
F(8, 26)	=	15.38
Prob > F	=	0.0000
R-squared	=	0.8256
Adj R-squared	=	0.7719
Root MSE	=	30.623

hrs	Coef.	Std. Err.	t	P>|t|	[95% Conf.	Interval]
rate	-93.75259	47.14499	-1.99	0.057	-190.6605	3.155329
ersp	.0002254	.0382548	0.01	0.995	-.0784084	.0788592
erno	-.2149663	.0979392	-2.19	0.037	-.4162832	-.0136495
nein	.1572073	.5164059	0.30	0.763	-.9042802	1.218695
asset	.0155724	.0254048	0.61	0.545	-.0366479	.0677928
age	-.3486302	3.72233	-0.09	0.926	-7.999989	7.302729
dep	20.72802	16.88047	1.23	0.230	-13.97029	55.42633
school	37.32565	22.66518	1.65	0.112	-9.263304	83.9146
_cons	1904.577	251.9332	7.56	0.000	1386.721	2422.433

3.1 (2 points) Write out the regression equation for model **??**.

Table 3.2 the correlation matrix

	rate	ersp	erno	nein	asset	age	dep	school
rate	1.0000							
ersp	0.5717	1.0000						
erno	0.0590	-0.0410	1.0000					
nein	0.7018	0.2344	0.3591	1.0000				
asset	0.7789	0.2741	0.2922	0.9875	1.0000			
age	0.0442	-0.0153	0.7755	0.5024	0.4171	1.0000		
dep	-0.6014	-0.6929	0.0502	-0.5208	-0.5136	-0.0484	1.0000	
school	0.8813	0.5491	-0.2986	0.5392	0.6309	-0.3311	-0.6026	1.0000

3.2 (8 points) Is there evidence of multicollinearity in the data? How do you know? Explain your answers in detail and state the critical value for hypothesis testing to receive fully points. If there is the multicollinearity problem, what remedial action, if any, would you take?

Table 3.3 Variance Inflation Factors and Tolerance (VIF

Variable	VIF	1/VIF
asset	192.57	0.005193
nein	180.51	0.005540
school	25.40	0.039367
rate	17.08	0.058540
age	9.72	0.102869
dep	4.53	0.220992
ersp	3.50	0.285841
erno	3.14	0.318680
Mean VIF	54.55	

3.3 (3 points) Explain the outcome of Variance Inflation Factors and Tolerance (VIF).

3.4 State with reason whether the following statement are true or false.

a. (2.5 points) Despite perfect multicollinearity, OLS estimators are BLUE.

b. (2.5 points) In case of high multicollinearity, it is not possible to assess the individual significance of one or more partial regression coefficients.

4. (18 points) Consider Method of Generalized Least Square (GLS).

Through Ordinary Least Square (OLS), we minimize

$$\sum_{i=1}^{n} \hat{u}_i^2 = \sum_{i=1}^{n} (Y_i - \hat{\beta}_1 - \hat{\beta}_2 X_i)^2.$$

Through Generalized Least Square (GLS), we minimize

$$\sum_{i=1}^{n} w_i \hat{u}_i^2 = \sum_{i=1}^{n} w_i (Y_i - \hat{\beta}_1^* - \hat{\beta}_2^* X_i)^2.$$

where $w_i = \frac{1}{\sigma_i^2}$

4.1 (5 points) Explain a rationale on the method of generalized least square (GLS). In other words; explain why GLS is **superior or more appropriate** than OLS in the presence of heteroscedasticity.

You are conducting an empirical investigation into the air quality in California for 2015. The sample data consists of 30 standard metropolitan statistical areas (SMSAs) on the following variables:

airq = indicator for air quality **(the lower the better)**;

vala = value added of companies (in 1000 US $);

rain = amount of rain (in inches);

coas = dummy variable, 1 for SMSAs at the coast; 0 for others;

dens = population density (per square mile);

medi = average income per head (in US $).

Your research assistant estimates a following regression model of air quality in California on the sample of N = 30 observations

$$\begin{aligned} \text{airq}_i &= \beta_1 + \beta_2\text{vala}_i + \beta_3\text{rain}_i + \beta_4\text{coas}_i + \beta_5\text{dens}_i \\ &\quad \beta_6\text{medi}_i + u_i \end{aligned} \qquad \text{(Eq.5)}$$

The estimation results for the model **??** are given below.

Table 4.1 the regression result of model ??

```
. regress airq vala rain coas dens medi

      Source |       SS           df       MS      Number of obs   =        30
-------------+----------------------------------   F(  5,     24)  =      2.98
       Model |  8723.84625         5  1744.76925   Prob > F        =    0.0313
    Residual |  14058.4538        24  585.768906   R-squared       =    0.3829
-------------+----------------------------------   Adj R-squared   =    0.2544
       Total |     22782.3        29  785.596552   Root MSE        =    24.203

------------------------------------------------------------------------------
        airq |      Coef.   Std. Err.      t    P>|t|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
        vala |   .0008834   .0022562     0.39   0.699    -.0037731    .0055399
        rain |   .2506988   .3435183     0.73   0.473     -.458288    .9596857
        coas |   -33.3983   10.45752    -3.19   0.004    -54.98156   -11.81504
        dens |  -.0010734   .0016233    -0.66   0.515    -.0044237    .0022769
        medi |   .0005545   .0008503     0.65   0.521    -.0012003    .0023093
       _cons |   111.9347   15.33179     7.30   0.000     80.29141    143.5779
------------------------------------------------------------------------------

.
```

4.2 (3 points) From the table 4.1, interpret each of the slope coefficient estimates $\hat{\beta}_2$ and $\hat{\beta}_4$ in regression model **??**.

Now, consider the following Stata command:

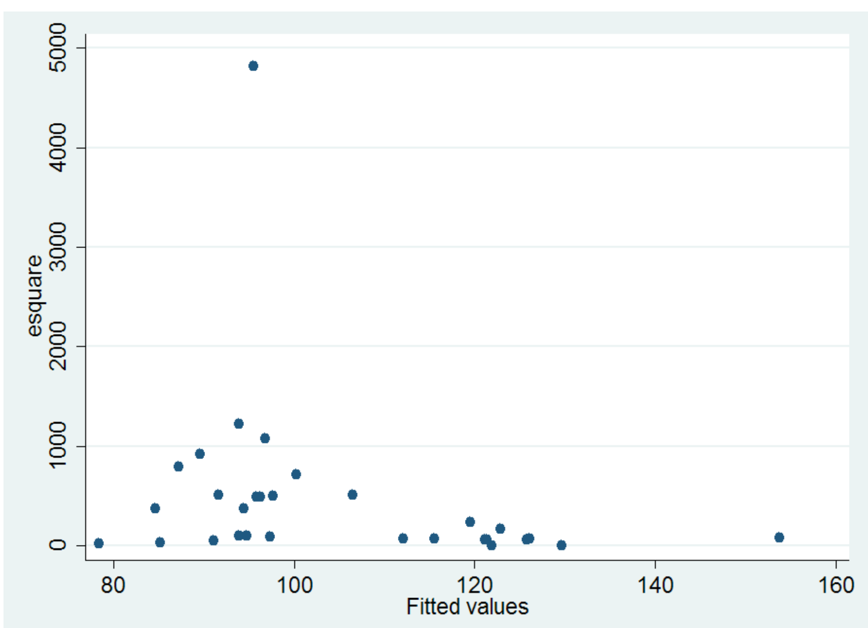
predict yhat if e(sample)

predict e if e(sample), resid

gen esquare = e^2

scatter esquare yhat

Figure 4.1 The relationship between u_i^2 and $\hat{Y}_i$ from the regression results of ??



4.3 (2 points) From the figure 4.1 , is there any problem of Heteroskedasticity? Why or Why not?

Now, consider the following tests:

Test 1: Bruech-Pagan test

```
. predict e,resid

. predict yhat
(option xb assumed; fitted values)

. gen esquare =e^2

. scatter esquare yhat

. regress esquare vala rain coas dens medi
```

Source	SS	df	MS
Model	2406263.41	5	481252.682
Residual	20571541	24	857147.543
Total	22977804.4	29	792338.084

Number of obs =	30
F(5, 24) =	0.56
Prob > F =	0.7284
R-squared =	0.1047
Adj R-squared =	-0.0818
Root MSE =	925.82

esquare	Coef.	Std. Err.	t	P>|t|	[95% Conf.	Interval]
vala	.0001125	.0863058	0.00	0.999	-.1780138	.1782389
rain	-1.001573	13.14058	-0.08	0.940	-28.12239	26.11925
coas	570.1359	400.0307	1.43	0.167	-255.4869	1395.759
dens	-.0406206	.0620955	-0.65	0.519	-.1687795	.0875383
medi	-.004736	.0325247	-0.15	0.885	-.0718637	.0623917
_cons	220.2809	586.4857	0.38	0.711	-990.166	1430.728

4.4 (4 points) According to Bruech-Pagan test , does heteroskedasticity arise? Conduct F-test for checking heteroscedasticity at the 5 percent significance level (i.e., for significance level $\alpha = 0.05$)

Test 2: White-test

```
. estat imtest,white

White's test for Ho: homoskedasticity
         against Ha: unrestricted heteroskedasticity

         chi2(19)      =      8.61
         Prob > chi2   =    0.9795

Cameron & Trivedi's decomposition of IM-test
```

Source	chi2	df	p
Heteroskedasticity	8.61	19	0.9795
Skewness	2.32	5	0.8028
Kurtosis	0.81	1	0.3673
Total	11.74	25	0.9885

4.5 (4 points) According to White-test , does heteroskedasticity arise? Conduct LM-test for checking heteroscedasticity at the 5 percent significance level (i.e., for significance level $\alpha = 0.05$)

5. (18 points) This empirical illustration is based on one of the funding articles on autocorrelation, viz. Hildreth and Lu (1960). The data used in this study are time series data with 30 four-weekly observations from 18 March 1951 to 11 July 1953 on the following variables :

consump: consumption of ice cream per head (in pints);
income: average family income per week (in US Dollars);
price: price of ice cream (per pint);
temp: average temperature (in Fahrenheit).

The model used to explain consumption of ice cream is a linear regression model which is represented as:

$$ln(consump_t) \quad = \quad \beta_1 + \beta_2 income_t + \beta_3 ln(price_t) + \beta_4 temp_t + u_i \tag{Eq.6}$$

The estimation result is reported as below:

Table 5.1 the regression result of the demand for ice cream

```
. tsset time
       time variable:  time, 1 to 30
               delta:  1 unit

. gen ln_consump =ln(cons)

. gen ln_price=ln(price)

. regress ln_consump income ln_price temp
```

Source	SS	df	MS
Model	.678880551	3	.226293517
Residual	.237165841	26	.009121763
Total	.916046392	29	.031587807

Number of obs =	30
F(3, 26) =	24.81
Prob > F =	0.0000
R-squared =	0.7411
Adj R-squared =	0.7112
Root MSE =	.09551

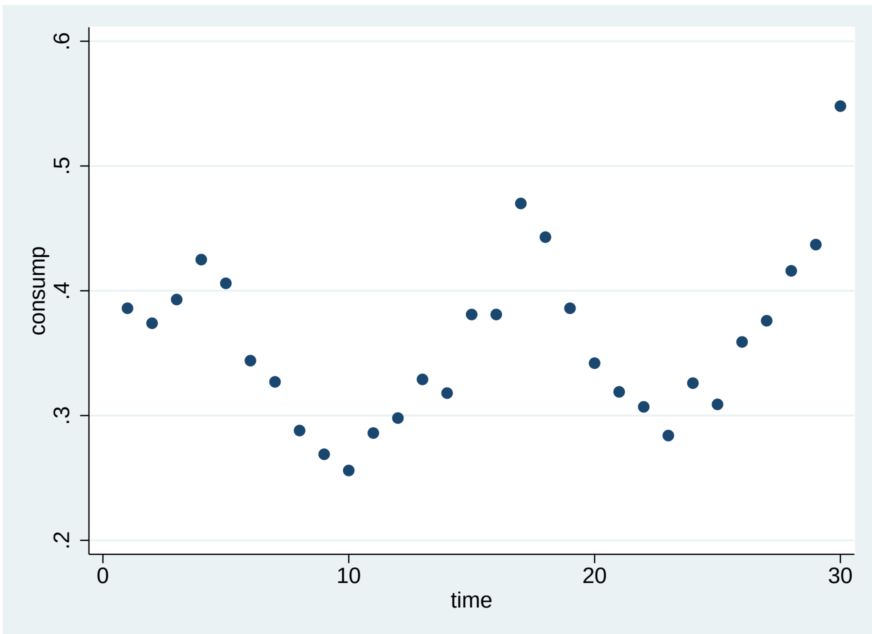
ln_consump	Coef.	Std. Err.	t	P>|t|	[95% Conf.	Interval]
income	.0093556	.0030391	3.08	0.005	.0031086	.0156026
ln_price	-.5954412	.5953848	-1.00	0.326	-1.819272	.6283898
temp	.0095892	.0011554	8.30	0.000	.0072142	.0119643
_cons	-3.069371	.7714954	-3.98	0.000	-4.655203	-1.48354

5.1 (4 points) Based on the regression result of the demand for ice cream on table 5.1, interpret carefully each of the slope coefficient estimates β_2 and β_3.

Now, consider the following stata command:

scatter consump time

Figure 5.1



5.2 (4 points) From the Figure 5.1, is there the problem of autocorrelation? If yes, positive or negative autocorrelation ? Briefly explain how you detect it.

Test 5.1 Durbin-Watson test on model ??

```
. estat dwatson

Durbin-Watson d-statistic(  4,    30) =  .9826207

.
```

5.3 (5 points) Based on the Test 5.1, Is there positive serial correlation in the disturbances at the 5 percent level of significance? Show your work to receive full credits.

Table 5.2

```
. newey ln_consump income ln_price temp,lag(1)

Regression with Newey-West standard errors          Number of obs  =        30
maximum lag: 1                                      F(  3,     26)  =     25.05
                                                    Prob > F       =    0.0000
```

ln_consump	Coef.	Newey-West Std. Err.	t	P>|t|	[95% Conf.	Interval]
income	.0093556	.0033274	2.81	0.009	.0025161	.0161951
ln_price	-.5954412	.6017979	-0.99	0.332	-1.832454	.6415722
temp	.0095892	.0011416	8.40	0.000	.0072427	.0119358
_cons	-3.069371	.6683789	-4.59	0.000	-4.443244	-1.695499

5.4 (5 points) Given Durbin-Watson result on Test 5.1, is it necessary to perform the regression in Table 5.2 instead of Table 5.1? Why? What is the limitation of using the technique in table 5.2?

The End of Exam