

Exercise 2B. Consider a function that relates tax revenues  $R$ , in billions of dollars, to the average tax rate  $t$  such that  $R = 350t - 500t^2$ .

(a) What tax rate(s) is consistent with raising tax revenues equal to \$60 billion?

(b) What tax rate(s) is consistent with raising tax revenues equal to \$61.25 billion?

(c) What tax rate is consistent with the maximum tax revenue?

$$\begin{aligned} \text{a)} \quad & 350t - 500t^2 = 60 \\ & -500t^2 + 350t - 60 = 0 \\ & 50t^2 - 35t + 6 = 0 \\ & t = 0.3, 0.4 \end{aligned}$$

Tax rate of 30% and 40% will yield 60M government revenue. #

$$\begin{aligned} \text{b)} \quad & 350t - 500t^2 = 61.25 \\ & -500t^2 + 350t - 61.25 = 0 \\ & t = 0.35 \end{aligned}$$

Tax rate of 35% will yield 60M government revenue. #

c) Maximize government revenue:

$$\begin{aligned} & \frac{\partial R}{\partial t} = 0 \\ & \frac{\partial (350t - 500t^2)}{\partial t} = 0 \\ & 350 - 1,000t = 0 \\ & t = \frac{350}{1,000} \\ & = 0.35 \end{aligned}$$

Tax rate that maximize the government revenue is 35 percent. #