

EE431 Economics of Financial Markets and Institutions

Exercise 4: Capital Asset Pricing Model (CAPM), Hint and Correction

Correction :

Question 2 : Company X has a beta of 1.45. The expected risk-free rate of interest is 2.5% and the expected return on the market as a whole is 10%. Using the CAPM, what is **Stock X**'s expected return?

Question 3 C : What is the beta of stock A?

Hint: By definition, $\beta_A = \frac{r_{A,m}\sigma_A\sigma_m}{\sigma_m^2} = \frac{COV(R_A, R_m)}{\sigma_m^2}$.

Find $COV(R_A, R_m)$.

$$\begin{aligned}
 COV(R_A, R_m) &= E[(R_A - E(R_A))(R_m - E(R_m))] \\
 &= E([(R_A - E(R_A))(w_A R_A + w_B R_B - w_A E R_A - w_B E R_B)]) \\
 &= E([(R_A - E(R_A))\{(w_A R_A - w_A E R_A) + (w_B R_B - w_B E R_B)\}]) \\
 &= E[w_A(R_A - E(R_A))^2 + w_B(R_A - E R_A)(R_B - E R_B)] \\
 &= w_A \sigma_A^2 + w_B COV(R_A, R_B) \\
 &= w_A \sigma_A^2 + w_B r_{AB} \sigma_A \sigma_B
 \end{aligned}$$

After this calculation, you can find the beta of stock A.

Note : We may realize that given all the statistical data of stock A and stock B. We can find covariance between return on stock A with any portfolio comprising stock A and stock B.