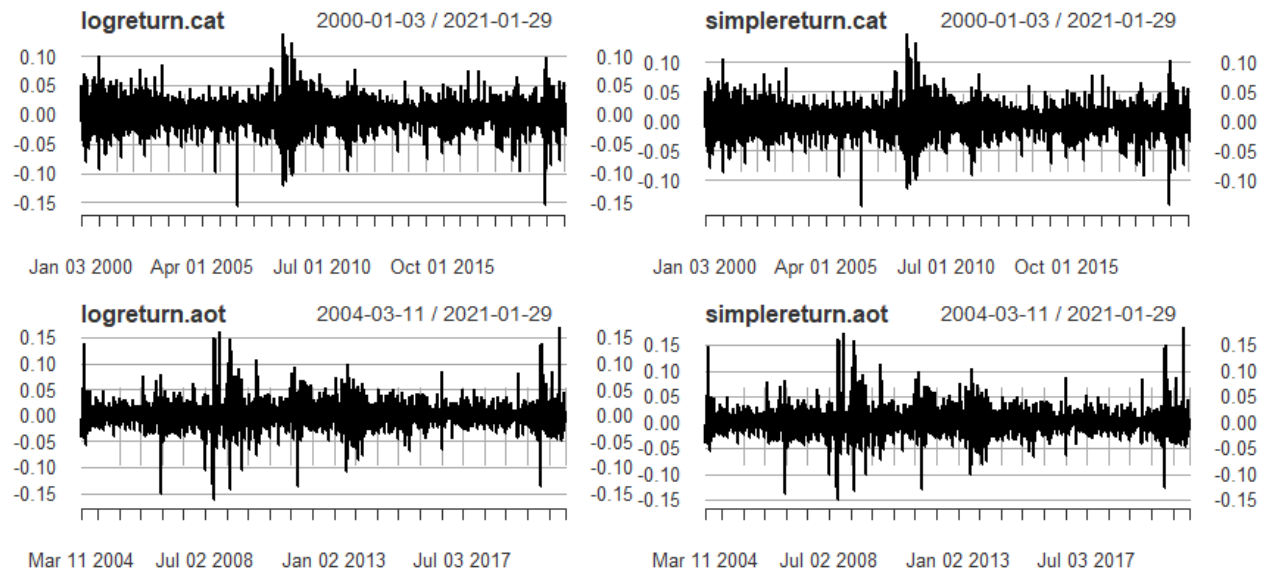


1.a)

```
par(mfrow=c(2,2))
plot(logreturn.cat,type='l')
plot(simplereturn.cat)
plot(logreturn.aot,type='l')
plot(simplereturn.aot)
```



```
newlogreturn.cat <- logreturn.cat[2:nrow(logreturn.cat),]
newsimplereturn.cat <- simplereturn.cat[2:nrow(simplereturn.cat),]
newlogreturn.aot <- logreturn.aot[2:nrow(logreturn.aot),]
newsimplereturn.aot <- simplereturn.aot[2:nrow(simplereturn.aot),]
```

1.b)

For Simple return of CAT,

```
table.Stats(simplereturn.cat)
```

##	CAT.Adjusted
## Observations	5302.0000
## NAs	1.0000
## Minimum	-0.1452
## Quartile 1	-0.0095
## Median	0.0005
## Arithmetic Mean	0.0007 (Sample Mean)
## Geometric Mean	0.0005
## Quartile 3	0.0110
## Maximum	0.1472
## SE Mean	0.0003
## LCL Mean (0.95)	0.0001

```
## UCL Mean (0.95)      0.0013
## Variance             0.0004
## Stdev                0.0205 (Standard Deviation)
## Skewness             0.0197
## Kurtosis             4.5480 (Excess Kurtosis)
```

For Simple return of AOT,

```
table.Stats(simplereturn.aot)
```

```
##                AOT.BK.Adjusted
## Observations      4158.0000
## NAs                1.0000
## Minimum          -0.1505
## Quartile 1       -0.0093
## Median            0.0000
## Arithmetic Mean   0.0010 (Sample Mean)
## Geometric Mean    0.0007
## Quartile 3        0.0103
## Maximum           0.1834
## SE Mean           0.0003
## LCL Mean (0.95)   0.0003
## UCL Mean (0.95)   0.0016
## Variance          0.0005
## Stdev             0.0213 (Standard Deviation)
## Skewness          0.5443
## Kurtosis          10.0827 (Excess Kurtosis)
```

1.c)

Normality Test:  $H_0$ : simple return of CAT is normally distributed.

$H_1$ : simple return of CAT is not normally distributed.

```
jarque.bera.test(newssimplereturn.cat)
```

```
##
## Jarque Bera Test
##
## data: newssimplereturn.cat
## X-squared = 4569.9, df = 2, p-value < 2.2e-16
```

The p-value < 0.05; hence, the computed chi-squared

Falls into rejection region.  $H_0$  is rejected at 0.05 level of significance.

That is, the simple return of CAT is **not** normally distributed.

1.d)

For log return of CAT,

```
table.Stats(logreturn.cat)

##                CAT.Adjusted
## Observations      5302.0000
## NAs                1.0000
## Minimum           -0.1569
## Quartile 1        -0.0095
## Median             0.0005
## Arithmetic Mean    0.0005 (Sample Mean)
## Geometric Mean     0.0003
## Quartile 3         0.0110
## Maximum            0.1373
## SE Mean            0.0003
## LCL Mean (0.95)   -0.0001
## UCL Mean (0.95)    0.0010
## Variance           0.0004
## Stdev              0.0205 (Standard deviation)
## Skewness           -0.1836
## Kurtosis           4.6982 (Excess Kurtosis)
```

For log return of AOT,

```
table.Stats(logreturn.aot)

##                AOT.BK.Adjusted
## Observations      4158.0000
## NAs                1.0000
## Minimum           -0.1632
## Quartile 1        -0.0093
## Median             0.0000
## Arithmetic Mean    0.0007 (Sample Mean)
## Geometric Mean     0.0005
## Quartile 3         0.0102
## Maximum            0.1684
## SE Mean            0.0003
## LCL Mean (0.95)    0.0001
## UCL Mean (0.95)    0.0014
## Variance           0.0004
## Stdev              0.0212 (Standard Deviation)
## Skewness           0.1746
## Kurtosis           9.6096 (Excess Kurtosis)
```

1.e)

Ho: E (log return of CAT) = 0

H1: E (log return of CAT)  $\neq$  0

```
t.test(newlogreturn.cat)
```

```
## One Sample t-test
##
## data: newlogreturn.cat
## t = 1.7296, df = 5301, p-value = 0.08377
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -6.513168e-05 1.041069e-03
## sample estimates:
## mean of x
## 0.0004879685
```

p-value > 0.05; the computed t-value < 2 not falling into rejection region. We fail to reject H0 at 0.05 level of significance. That is, the expected log return of CAT is equal to 0.

Ho: E (log return of AOT) = 0

H1: E (log return of AOT)  $\neq$  0

```
t.test(newlogreturn.aot)
```

```
## One Sample t-test
##
## data: newlogreturn.aot
## t = 2.2696, df = 4157, p-value = 0.02328
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## 0.0001016629 0.0013915769
## sample estimates:
## mean of x
## 0.0007466199
```

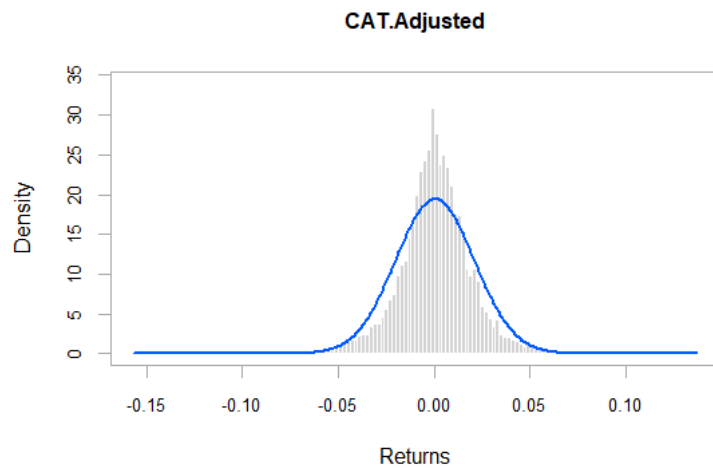
p-value < 0.05; the computed t-value > 2 falling into rejection region. H0 is rejected at 0.05 level of significance. That is, expected log return of AOT is not equal to 0.

1.f)

```
par(mfrow=c(1,1))
```

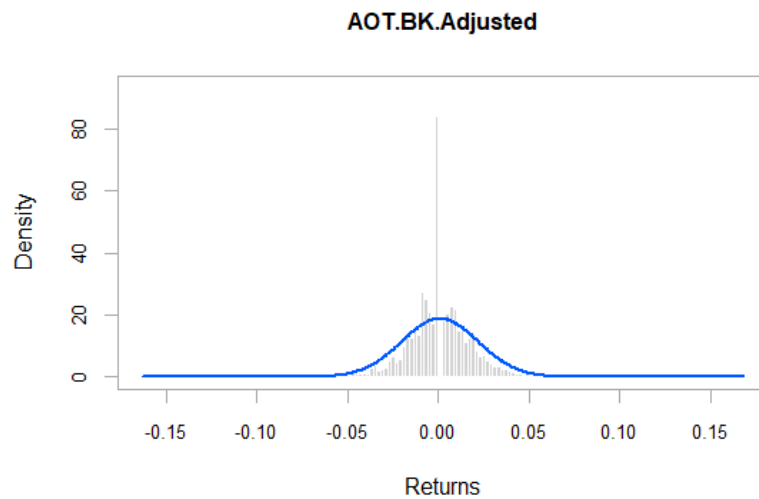
```
hist(logreturn.cat, breaks=100, col="slateblue")
```

```
chart.Histogram(logreturn.cat, methods = c("add.normal"))
```



```
hist(logreturn.aot, breaks=100, col="slateblue")
```

```
chart.Histogram(logreturn.aot, methods = c("add.normal"))
```



1.g)

```
t.test(newlogreturn.cat)
```

```
## One Sample t-test
##
## data: newlogreturn.cat
## t = 1.7296, df = 5301, p-value = 0.08377
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -6.513168e-05 1.041069e-03
## sample estimates:
## mean of x
## 0.0004879685
```

95% confidence interval of log return of CAT is between  $-6.513168e-05$  and  $1.041069e-03$  or  $[-6.513168e-05, 1.041069e-03]$

1.h)

### **Skewness test of CAT**

```
#CAT
T=length(newlogreturn.cat)
m3=skewness(newlogreturn.cat)
tst=m3/sqrt(6/T)
tst
## [1] -5.458812
pv=2*pnorm(tst)
pv
## [1] 4.793299e-08
```

H0:  $m_3 = 0$

H1:  $m_3 \neq 0$

The p-value  $< 0.05$ . The computed value fall into rejection region. H0 is rejected at 0.05 level of significance. That is,  $m_3 \neq 0$ , namely, the skewness of CAT return is not equal to zero.

### **Skewness test of AOT**

```
#AOT
T=length(newlogreturn.aot)
m3=skewness(newlogreturn.aot)
tst=m3/sqrt(6/T)
tst
```

```
## [1] 4.596526  
pv=2*(1-pnorm(tst))  
pv  
## [1] 4.29594e-06
```

H0:  $m_3 = 0$

H1:  $m_3 \neq 0$

The p-value  $< 0.05$ . The computed value fall into rejection region. H0 is rejected at 0.05 level of significance. That is,  $m_3 \neq 0$ , namely, the skewness of AOT return is not equal to zero.

1.i)

### **Kurtosis test of CAT**

```
#CAT  
T=length(newlogreturn.cat)  
s4=kurtosis(newlogreturn.cat) #excess kurtosis  
K=s4+3 #kurtosis  
tst=(K-3)/sqrt(24/T)  
tst
```

```
## [1] 69.83078  
pv=2*(1-pnorm(tst))  
pv  
## [1] 0
```

H0:  $K=3$

H1:  $K \neq 3$

The p-value  $< 0.05$ . The computed value fall into rejection region. H0 is rejected at 0.05 level of significance. That is,  $K \neq 3$ , namely, the kurtosis of CAT return is not equal to 3.

### **Kurtosis test of AOT**

```
#AOT  
T=length(newlogreturn.aot)  
s4=kurtosis(newlogreturn.aot) #excess kurtosis  
K=s4+3 #kurtosis  
tst=(K-3)/sqrt(24/T)  
tst
```

```
## [1] 126.4855  
pv=2*(1-pnorm(tst))  
pv
```

## [1] 0

H0:  $K=3$

H1:  $K \neq 3$

The p-value  $< 0.05$ . The computed value fall into rejection region. H0 is rejected at 0.05 level of significance. That is,  $K \neq 3$ , namely, the kurtosis of AOT return is not equal to 3.