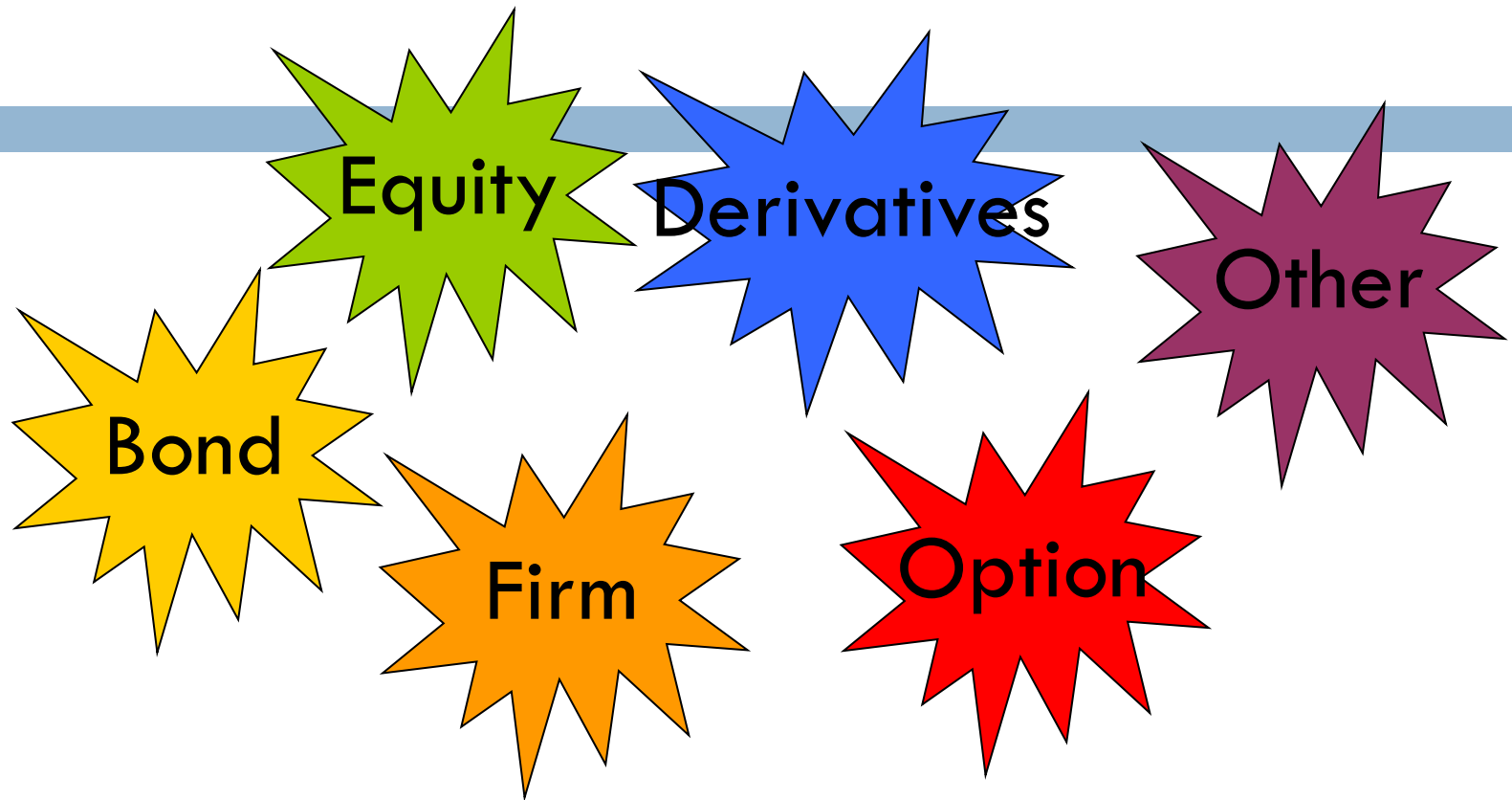




FN 201 BUSINESS FINANCE



Lecture 7 Asset Valuation



(Any) Financial products are valued as sum of discounted (expected) cash flow

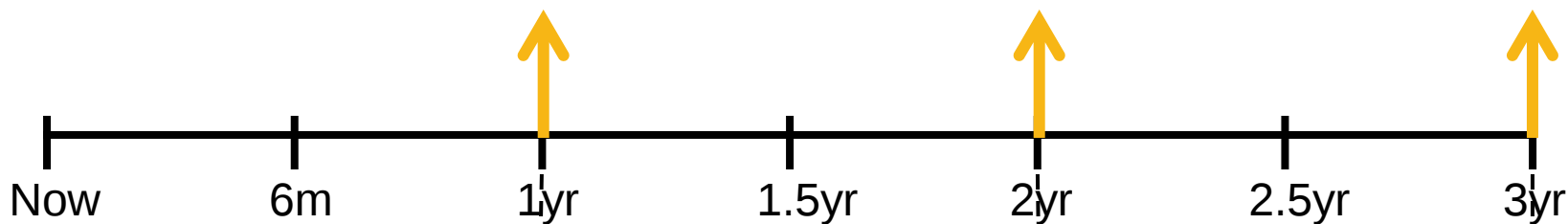
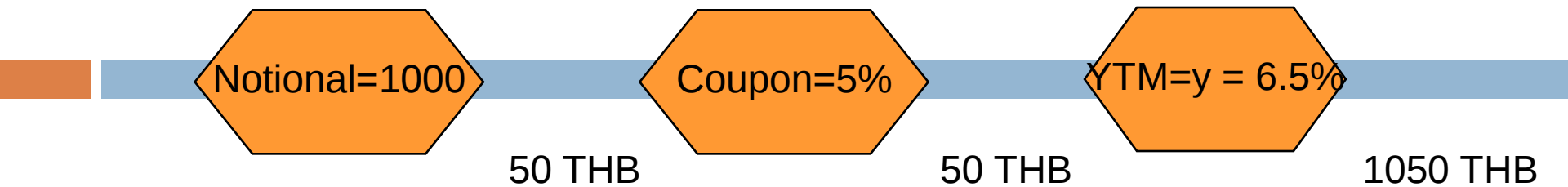
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Bond Valuation

What is Bond?

- Bond is Legal contract that specifies the rights and obligations of the bond issuer and the bond holders
- Debt instrument that pay pre-determined interest rate (coupon rate) over the life until maturity
- It becomes an important source of funding for firms in addition to bank loan
- Bond Features:
 - ▣ Face or Par Value
 - ▣ Coupon rate
 - ▣ Frequency of coupon payment
 - ▣ Maturity
 - ▣ Others covenants (rules and restrictions on the bond issuer and holders)





$$PV = 50 / (1+y)^1 =$$

+

$$PV = 50 / (1+y)^2 =$$

+

$$PV = 1,050 / (1+y)^3 =$$

Bond Price = PV of coupons + PV of par value

$$\text{Bond Price} = \sum_{t=1}^T \frac{C}{(1+y)^t} + \frac{\text{Par value}}{(1+y)^T}$$

Bond Price = $C \cdot \text{Annuity factor}(y, T) + \text{Par} \cdot \text{discount factor}(y, T)$

Yield to Maturity (YTM)

- Yield to maturity (YTM) is the rate of return (or yield) if bond is hold until maturity
- It is the single discount rate that is used to calculate the present value of cash flows, and therefore used to calculate the bond price.
- There is 1:1 relationship between bond price and yield to maturity.
- This is how bond price get quoted in the market.

Bond Quote

Treasury Bills	Government Bonds	State Owned Enterprise Bonds	State Agency Bonds	Corporate Bonds	Foreign Bonds
State Owned Enterprise Bonds Quoted Yields			Historical Quoted Yield >> 08/09/2008		Go! (dd/mm/yyyy)
08 September 2008					
Bond	Coupon	Maturity	TTM (Yrs.)	Quoted Date	Quoted Yield(%)
BMTA08DA	3.85	15/12/2008	0.27	08/09/2008	3.882471
BMTA08NA	3.78	04/11/2008	0.16	08/09/2008	3.880473
BMTA09DA	4.14	04/12/2009	1.24	08/09/2008	4.084864
BMTA09QA	4.225	28/10/2009	1.14	08/09/2008	4.046865
BMTA10DA	5.86	13/12/2010	2.26	08/09/2008	4.232227
BMTA10NA	4.53	04/11/2010	2.16	08/09/2008	4.216950
BMTA10QA	4.6	15/10/2010	2.10	08/09/2008	4.209115
BMTA111A	5.325	25/01/2011	2.38	08/09/2008	4.255625
BMTA11DA	6	13/12/2011	3.26	08/09/2008	4.385197
BMTA11QA	4.72	15/10/2011	3.10	08/09/2008	4.360696
BMTA122A	5.345	08/02/2012	3.42	08/09/2008	4.431282
BMTA128A	4.598	29/08/2012	3.98	08/09/2008	4.502289
BMTA12DA	4.77	13/12/2012	4.27	08/09/2008	4.549463
BMTA131A	4.95	25/01/2013	4.38	08/09/2008	4.581162
BMTA133A	4.1	26/03/2013	4.55	08/09/2008	4.622401
BMTA136A	3.4968	01/06/2013	4.73	08/09/2008	4.655081
BMTA136B	3.8668	14/06/2013	4.77	08/09/2008	4.661422
BMTA13DA	4.967	17/12/2013	5.28	08/09/2008	4.722664
BMTA13QA	4.738	29/10/2013	5.14	08/09/2008	4.708707
BMTA144A	4.17	10/04/2014	5.59	08/09/2008	4.764885
BMTA144B	4.12	24/04/2014	5.63	08/09/2008	4.772772
BMTA146A	3.808	07/06/2014	5.75	08/09/2008	4.799477
BMTA14DA	4.83	13/12/2014	6.27	08/09/2008	4.858313
BMTA152A	4.79	08/02/2015	6.42	08/09/2008	4.866520
BMTA156A	3.6468	01/06/2015	6.73	08/09/2008	4.882792
BMTA156B	4.03	14/06/2015	6.77	08/09/2008	4.884663
BMTA15QA	4.94	29/10/2015	7.14	08/09/2008	4.895778

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Source : thaibma.or.th

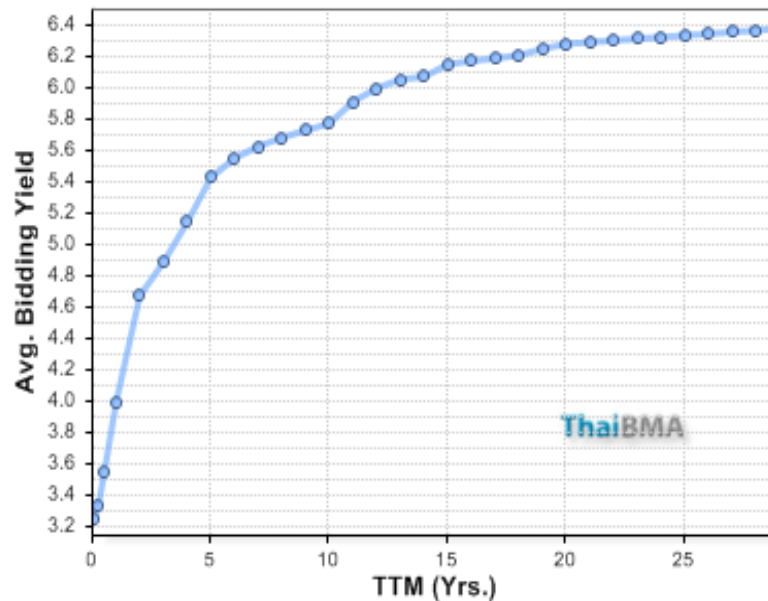
Curve from Thai BMA



ThaiBMA
THE THAI BOND MARKET ASSOCIATION

ThaiBMA Government Bond Yield Curve

As of 11 Jul 2008



(dd/mm/yyyy)

TTM (Yrs.)	Yield (%)
0.08	3.26
0.25	3.35
0.50	3.56
1	4.01
2	4.68
3	4.90
4	5.15
5	5.43
6	5.56
7	5.63
8	5.69
9	5.73
10	5.78
11	5.92
12	6.00
13	6.06
14	6.07
15	6.15
16	6.17
17	6.19
18	6.21
19	6.25
20	6.28
21	6.20

Ex.1

- A government bond issued in Germany has a coupon rate of 5%, face value of euros 100 and maturing in five years. The interest payments are made annually. Calculate the price of the bond (in euros) if the yield to maturity is 3.5%.
 - a. 100
 - b. 106.77
 - c. 106.33
 - d. None of the above

Ex. 2:

- 8% coupon, 30-yr maturity bond with par value of \$1,000 paying 60 semiannual coupon of \$40 each.
- If YTM is 8% annually, or 4% per 6-month period, what is the price of this bond?
- If YTM is 10% annually, or 5% per 6-month period, what is the price of this bond?

Ex.3 : What can you get out from this result?

- Bond prices at different interest rates
- 8% coupon bond with par value of \$1,000, coupons paid semiannually

Bond Price at Given Market Interest Rates					
Time to Maturity	4%	6%	8%	10%	12%
1 yr	1038.83	1029.13	1000.00	981.41	963.33
10 yr	1327.03	1148.77	1000.00	875.35	770.6
20 yr	1547.11	1231.15	1000.00	828.41	699.07
30 yr	1695.22	1276.76	1000.00	810.71	676.77

Ex. 4: True or False

- Which of the following statements about the relationship between interest rates and bond prices is true?
 - I) There is an inverse relationship between bond prices and interest rates
 - II) There is a direct relationship between bond prices and interest rates
 - III) The price of short-term bonds fluctuates more than the price of long-term bonds for a given change in interest rates. (Assuming that coupon rate is the same for both)
 - IV) The price of long-term bonds fluctuates more than the price of short-term bonds for a given change in interest rates. (Assuming that the coupon rate is the same for both)

Ex. 5

- What would you expect the market price of the following bond to be? Which bond has higher price?
- 1) Notional = 100, 1 yr maturity, 8% annual coupon
 - ▣ 1.1) When the yield available on comparable bonds is 8%
 - ▣ 1.2) When the yield available on comparable bonds is 5%
- 2) Notional = 100, 7yr maturity, 8% annual coupon
 - ▣ 1.3) When the yield available on comparable bonds is 8%
 - ▣ 1.4) When the yield available on comparable bonds is 5%
- 3) Notional = 100, 7yr maturity, zero coupon
 - ▣ 1.5) When the yield available on comparable bonds is 8%
 - ▣ 1.6) When the yield available on comparable bonds is 5%

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Bond Price through Times

Bond Pricing

Bond Price = PV of coupons + PV of par value

$$\text{Bond Price} = \sum_{t=1}^T \frac{C}{(1+y)^t} + \frac{\text{Par value}}{(1+y)^T}$$

Bond Price = $C \cdot \text{Annuity factor}(y, T) + \text{Par} \cdot \text{discount factor}(y, T)$

Where return comes from?

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- Bond
 - ▣ Coupon payment & Capital gains (losses)

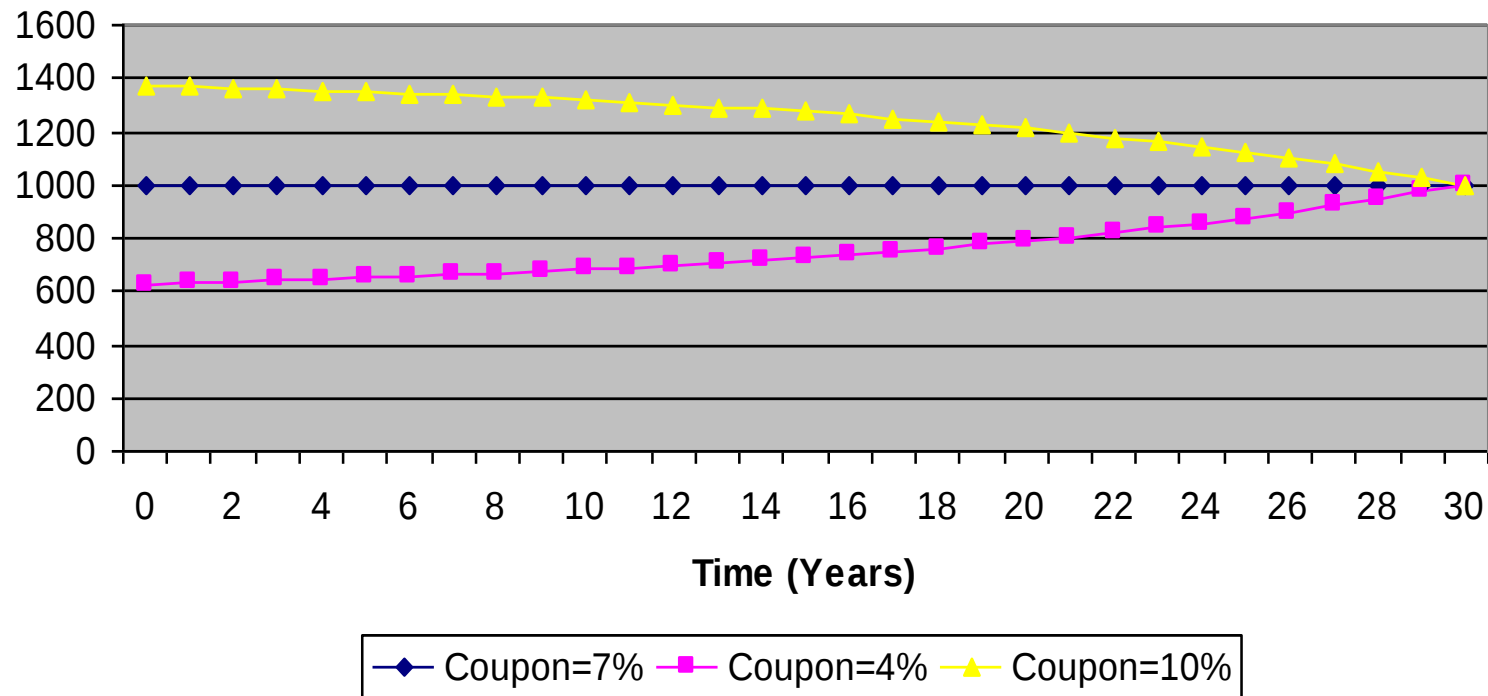
- Stock
 - ▣ Dividends & Capital gains (losses)

Bond Price Through Time

- Find price of bond with coupon C (THB 70) paid annually, 30 yrs maturity, yield to maturity is 4%
- At time 0: Bond Price = $C * \text{Annuity factor}(4\%, 30) + \text{Par} * \text{discount factor}(4\%, 30)$
- At time 1: Bond Price = $C * \text{Annuity factor}(4\%, 29) + \text{Par} * \text{discount factor}(4\%, 29)$
- At time 2: Bond Price = $C * \text{Annuity factor}(4\%, 28) + \text{Par} * \text{discount factor}(4\%, 28)$
-
- At time 30: Bond Price = $C * \text{Annuity factor}(4\%, 0) + \text{Par} * \text{discount factor}(4\%, 0) = \text{face value}$

Price determined by YTM – Same YTM Diff Coupon

Prices over time of 30 year maturity, YTM = 7%,
for different coupon . Bond price approaches
par value as maturity approaches



How can bond with coupon 4% and 10% give same return of 7%?

Face	1000
Coupon	

Coupon=7
%

Coupon=4
%

Coupon=1
0%

7%

4%

10%

YTM=7%

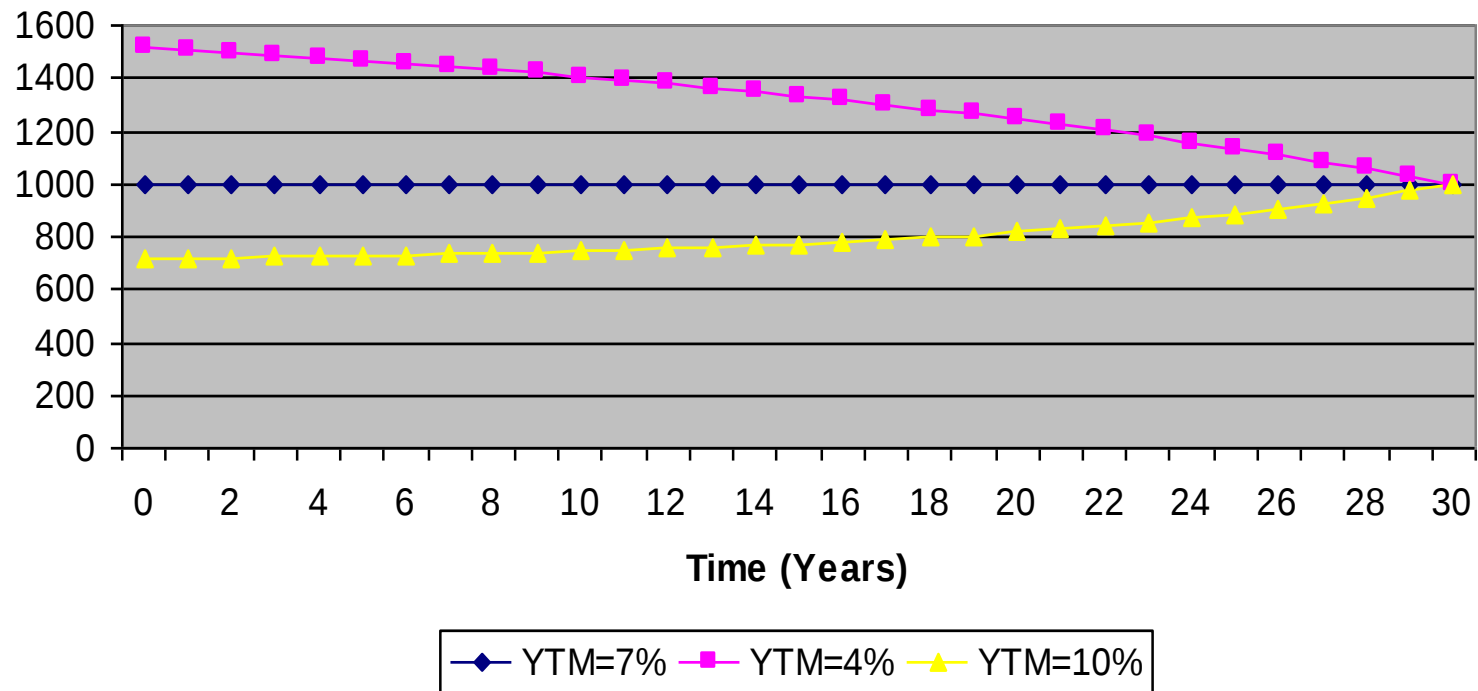
YTM=7%

YTM=7%

Time	TTM (Yrs)	Formula 7%	Hold and Sell	Return	Formula 7%	Hold and Sell	Return	Formula 7%	Hold and Sell	Return
0	30	1000.00			627.73			1372.27		
1	29	1000.00	1070	7%	631.67	672	7%	1368.33	1468	7%
2	28	1000.00	1070	7%	635.89	676	7%	1364.11	1464	7%
3	27	1000.00	1070	7%	640.40	680	7%	1359.60	1460	7%
4	26	1000.00	1070	7%	645.23	685	7%	1354.77	1455	7%
5	25	1000.00	1070	7%	650.39	690	7%	1349.61	1450	7%
6	24	1000.00	1070	7%	655.92	696	7%	1344.08	1444	7%
7	23	1000.00	1070	7%	661.83	702	7%	1338.17	1438	7%
8	22	1000.00	1070	7%	668.16	708	7%	1331.84	1432	7%
9	21	1000.00	1070	7%	674.93	715	7%	1325.07	1425	7%
10	20	1000.00	1070	7%	682.18	722	7%	1317.82	1418	7%
11	19	1000.00	1070	7%	689.93	730	7%	1310.07	1410	7%
12	18	1000.00	1070	7%	698.23	738	7%	1301.77	1402	7%
13	17	1000.00	1070	7%	707.10	747	7%	1292.90	1393	7%
14	16	1000.00	1070	7%	716.60	757	7%	1283.40	1383	7%
15	15	1000.00	1070	7%	726.76	767	7%	1273.24	1373	7%
16	14	1000.00	1070	7%	737.64	778	7%	1262.36	1362	7%
17	13	1000.00	1070	7%	749.27	789	7%	1250.73	1351	7%
18	12	1000.00	1070	7%	761.72	802	7%	1238.28	1338	7%
19	11	1000.00	1070	7%	775.04	815	7%	1224.96	1325	7%
20	10	1000.00	1070	7%	789.29	829	7%	1210.71	1311	7%
21	9	1000.00	1070	7%	804.54	845	7%	1195.46	1295	7%
22	8	1000.00	1070	7%	820.86	861	7%	1179.14	1279	7%
23	7	1000.00	1070	7%	838.32	878	7%	1161.68	1262	7%
24	6	1000.00	1070	7%	857.00	897	7%	1143.00	1243	7%
25	5	1000.00	1070	7%	876.99	917	7%	1123.01	1223	7%
26	4	1000.00	1070	7%	898.38	938	7%	1101.62	1202	7%
27	3	1000.00	1070	7%	921.27	961	7%	1078.73	1179	7%
28	2	1000.00	1070	7%	945.76	986	7%	1054.24	1154	7%
29	1	1000.00	1070	7%	971.96	1012	7%	1028.04	1128	7%
30	0	1000.00	1070	7%	1000.00	1040	7%	1000.00	1100	7%

Price determined by YTM (2) – Same Coupon Diff Yield

Prices over time of 30 year maturity, 7% coupon bond, for different YTM. Bond price approaches par value as maturity approaches



How can bond with coupon 7% give different return of 4% and 10%?

Face	1000
Coupon	7%

		YTM=7%			YTM=4%			YTM=10%		
		%			%			%		
Time	TTM (Yrs)	Formula 7%	Hold and Sell	Return	Formula 4%	Hold and Sell	Return	Formula 10%	Hold and Sell	Return
0	30	1000.00			1518.76			717.19		
1	29	1000.00	1070	7%	1509.51	1580	4%	718.91	789	10%
2	28	1000.00	1070	7%	1499.89	1570	4%	720.80	791	10%
3	27	1000.00	1070	7%	1489.89	1560	4%	722.88	793	10%
4	26	1000.00	1070	7%	1479.48	1549	4%	725.17	795	10%
5	25	1000.00	1070	7%	1468.66	1539	4%	727.69	798	10%
6	24	1000.00	1070	7%	1457.41	1527	4%	730.46	800	10%
7	23	1000.00	1070	7%	1445.71	1516	4%	733.50	804	10%
8	22	1000.00	1070	7%	1433.53	1504	4%	736.85	807	10%
9	21	1000.00	1070	7%	1420.87	1491	4%	740.54	811	10%
10	20	1000.00	1070	7%	1407.71	1478	4%	744.59	815	10%
11	19	1000.00	1070	7%	1394.02	1464	4%	749.05	819	10%
12	18	1000.00	1070	7%	1379.78	1450	4%	753.96	824	10%
13	17	1000.00	1070	7%	1364.97	1435	4%	759.35	829	10%
14	16	1000.00	1070	7%	1349.57	1420	4%	765.29	835	10%
15	15	1000.00	1070	7%	1333.55	1404	4%	771.82	842	10%
16	14	1000.00	1070	7%	1316.89	1387	4%	779.00	849	10%
17	13	1000.00	1070	7%	1299.57	1370	4%	786.90	857	10%
18	12	1000.00	1070	7%	1281.55	1352	4%	795.59	866	10%
19	11	1000.00	1070	7%	1262.81	1333	4%	805.15	875	10%
20	10	1000.00	1070	7%	1243.33	1313	4%	815.66	886	10%
21	9	1000.00	1070	7%	1223.06	1293	4%	827.23	897	10%
22	8	1000.00	1070	7%	1201.98	1272	4%	839.95	910	10%
23	7	1000.00	1070	7%	1180.06	1250	4%	853.95	924	10%
24	6	1000.00	1070	7%	1157.26	1227	4%	869.34	939	10%
25	5	1000.00	1070	7%	1133.55	1204	4%	886.28	956	10%
26	4	1000.00	1070	7%	1108.90	1179	4%	904.90	975	10%
27	3	1000.00	1070	7%	1083.25	1153	4%	925.39	995	10%
28	2	1000.00	1070	7%	1056.58	1127	4%	947.93	1018	10%
29	1	1000.00	1070	7%	1028.85	1099	4%	972.73	1043	10%
30	0	1000.00	1070	7%	1000.00	1070	4%	1000.00	1070	10%

Actual return might be higher / lower if sell before maturity

- If sell it before maturity for extra capital gain / loss
- YTM implies return in case of holding until maturity
(as the name suggests)

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Bond Special Features

Bond Special Features

- Who gains from these features? Who should be compensated?
- Callable
 - ▣ Provisions allowing issuer to repurchase the bond at a specified (call) price before maturity date
- Puttable
 - Provisions allowing holder to reclaim principal at a specified (put) price before maturing date
- Convertible
 - ▣ Provisions allowing holder to converted bond into stocks at fixed price on fixed date

Bond Special Features

□ Asset-Backed Bond :

- ▣ Coupon rate tied with performance of asset
- ▣ Walt Disney -> performance of its films
- ▣ David Bowie Bond -> royalties on his album

□ Index Bond :

- ▣ Payment tied to a general price index or commodity
- ▣ US -> Treasury Inflation Protected Securities (TIPS)
- ▣ Mexico -> 20 yrs bonds with payments depend on oil price

□ Inverse Floaters :

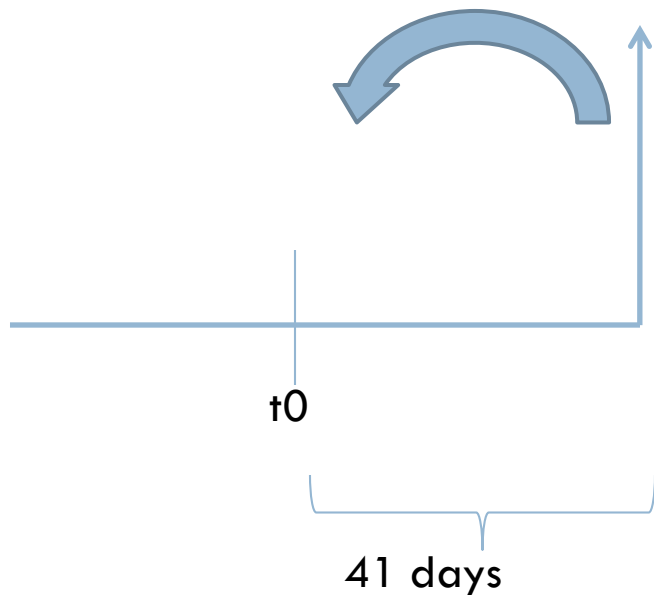
- ▣ Let's double the risk
- ▣ Coupon rate falls when rate rises -> suffer or gain doubly

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Bond Pricing in Practice

Ex6: Treasury Bill (TB)

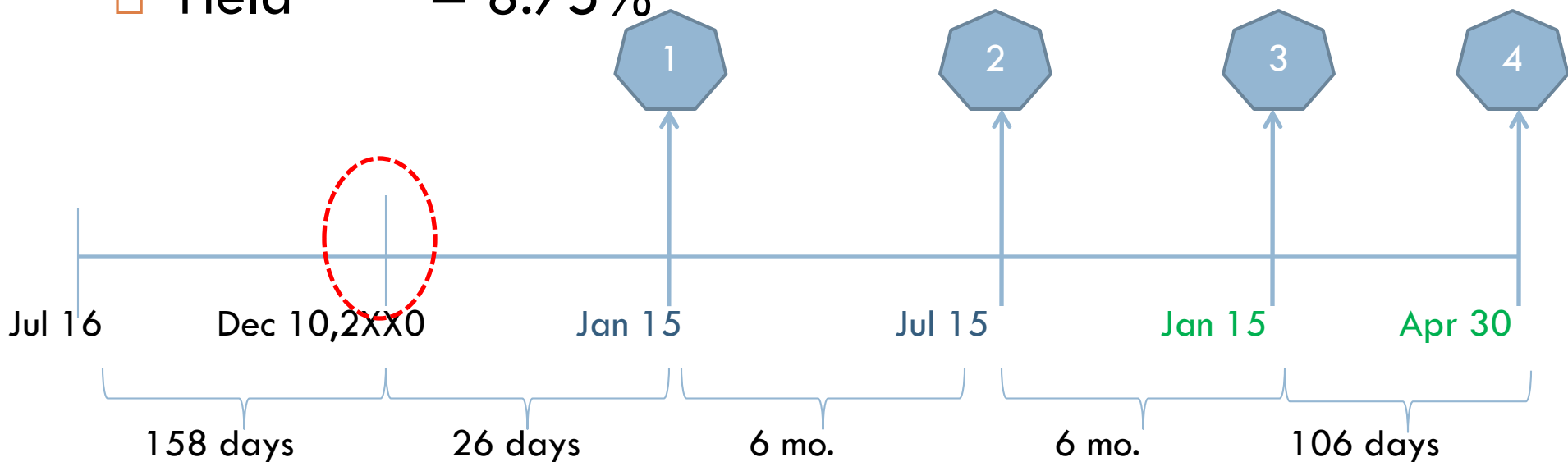
- Maturity = 41 days
- Yield = 6.41%
- Face = B100
- What is the price? (Hint: TB sold at discount)



- $P * (1 + 6.41\% * 41 / 365) = 100$
- $P = 100 / (1 + 6.41\% * 41 / 365)$
- $P = 99.2851$

Ex7: Coupon Bond

- Bond pay interest every 6 months (Jul & Jan 15)
- Today = Dec 10, 2XX0, Maturity = Apr 30, 2XX2
- Face = B100
- Coupon = 11.25%
- Yield = 8.75%



- CF1 discount 26 days
- CF2 discount 6mo. + 26 days
- CF3 discount 12mo. + 26 days
- CF4 discount 12mo. + 26 days + 106 days
- Yield = 4.375% / 6 mo. Or 182.5 days
- We use actual / 365 days count convention

$$\blacksquare \text{ PV-CF1} = 5.625 / (1 + 4.375\%)^{26/182.5} = 5.5908$$

$$\blacksquare \text{ PV-CF2} = 5.625 / (1 + 4.375\%)^{1 + 26/182.5} = 5.3564$$

- ▣ $PV-CF3 = 5.625 / (1 + 4.375\%)^{2 + 26/182.5} = 5.1319$
- ▣ $PV-CF4 = 100 + 3.2671 / (1 + 4.375\%)^{2 + 132/182.5} = 91.9006$
- ▣ $Price = \underline{PV-CF1} + \underline{PV-CF2} + \underline{PV-CF3} + \underline{PV-CF4}$
- ▣ $Price = 107.9798$

- ▣ Gross (Dirty) Price = 107.9798
- ▣ But the first 158 days of interest belongs to first holder
- ▣ If this is dirty price, what is the clean price?

Accrues interest – Coupon bonds

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Prices

- But the first 158 days of interest belongs to first holder
- If that is dirty price, what is the clean price (price net of accrued interest)?
- **Accrued interest:** The portion of the coupon payment accrued between the last coupon payment and the settlement day

Dirty price (full price) = Clean price + Accrued interest

$$AI = \frac{INT}{2} \times \frac{\text{Actual number of days since last coupon payment}}{\text{Actual number of days in coupon period}}$$

Dirty vs Clean price

- ▣ Clean Price = Gross (Dirty / full) Price – Accrued IR
- ▣ Clean Price = $107.9798 - 5.625 \times 158 / 182.5$
- ▣ Clean Price = $107.9798 - 4.8699 = 103.109$
- ▣ Clean / Quoted price = 103.109
- ▣ Dirty / Gross / Full price = 107.9798

□ Now we want to use Annuity Factor, and it should be exactly the same

□ **Gross Price** = $\text{Disc.Factor}(4.375\%, 26 \text{ days}) * CF1$
+ $\text{Disc.Factor}(4.375\%, 26 \text{ days}) * C * \text{annuity factor}(4.375\%, 2)$
+ $\text{Disc.Factor}(4.375\%, 2 + 132/182.5 \text{ days}) * \text{Face}$

□ $\text{Disc.Factor} = 1 / (1 + 4.375\%)^{26/182.5} = 0.9939$

□ $(1) = 0.9939 * 5.625 = 5.5908$

□ $(2) = 0.9939 * 5.625 * 1/r * (1 - 1/(1+r)^2) = 10.4884$

□ $(3) = 100 + 5.625 / (1 + 4.375\%)^{2 + 132/182.5} = 91.9006$

□ **Gross Price** = $5.5908 + 10.4884 + 91.9006 = 107.9798$

